

# Entropic Analysis of Spectrum Sensing for Cognitive Radio

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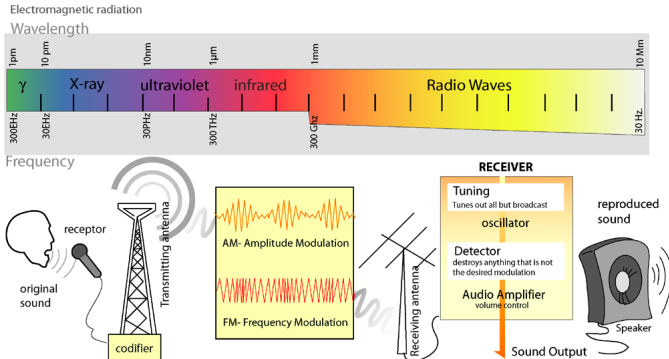
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Undergraduate Research Symposium

# Outline

- 1 Introduction
  - Fixed Spectrum Access
  - Opportunistic Spectrum Access
  - Problem Statement
- 2 Methods
  - GNU Radio/USRP
  - Software Defined Spectrum Analyzer
  - Analysis
- 3 Progress
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  - Progress
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# Wireless Communications



# FCC Frequency Allocation

## UNITED STATES FREQUENCY ALLOCATIONS THE RADIO SPECTRUM

**RADIO SERVICES COLOR LEGEND**

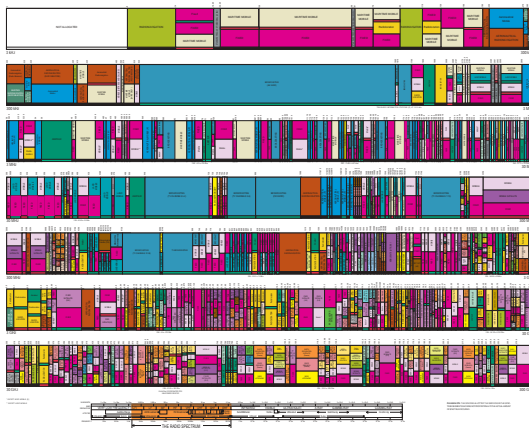
AM	FM	TV	Mobile
Commercial	Public Safety	Fixed	Mobile
... (many more entries)	...	...	...

**ACTIVITY CODE**

- Red: Broadcasting
- Green: Communication
- Black: Government

**ALLOCATION USER DESIGNATION**

UNITED STATES DEPARTMENT OF COMMERCE  
NATIONAL BUREAU OF STANDARDS



# Spatio-Temporal Variances In Spectrum Access

- FCC Study<sup>1</sup>: Utilization Varied From 15% To 85%
- Spatial Variances: Salt Lake City vs. Green River
- Temporal Variances: Business Hours vs. Late Evening
- If Only This Could Be Exploited. . .

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<sup>1</sup>[FCC, 2003]

# Fixed Spectrum Access

- Fixed Licensing Is Problematic
  - Crowded: No More Usuable Bands Available
  - Expensive: 90Mhz Recently Sold<sup>2</sup> For \$13 Billion!
  - Under Utilized: Spatio-Temporal Variances
- We Need Something Better!

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<sup>2</sup>[FCC, 2007]

# Case Study: Public Safety Band Usage<sup>3</sup>

- Channels: 23
- Channel BW: 25KHz
- Total BW: 20MHz
- $F_C$ : 856-869MHz

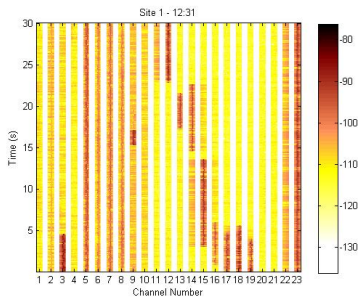


Figure: PSB Usage

<sup>3</sup>[Jones, 2007]

# Cognitive Radio

## Definition <sup>4</sup>

A "Cognitive Radio" is a radio that can change its transmitter parameters based on interaction with the environment in which it operates.

Adaptive Transmitter Parameters:

- Power Level
- Modulation Type
- Center Frequency

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<sup>4</sup>[Haykin, 2002]



# Hidden Terminal Problem

- Both Nodes Sense CR
- Can't Sense Each Other
- This Causes Interference

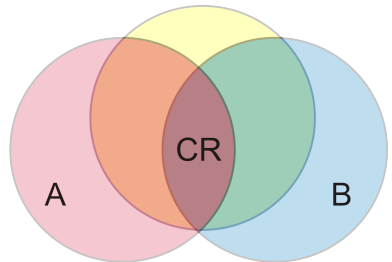


Figure: Hidden Terminals

# Collaborative Spectrum Sensing

## Pros

- Two Heads Are Better Than One!
  - i.e. More CR Nodes  $\implies$  More Accurate Detection <sup>5</sup>
- Solves Hidden Terminal Problem

## Cons

- Some BW Wasted On Control Channel
- How Much?

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<sup>5</sup>[Ghasemi, 2005]

# Information Entropy<sup>6</sup>

## Definition

The entropy of a discrete random variable  $X$  is a function of its PMF and is defined by

$$H(X) = - \sum_{i=1}^N p_i \log p_i$$

- The Number Of Bits Required By A Control Channel
- A Similiar Metric, Entropy *Rate*, Gives Bit Rate
- Need Only Know The PMF Of Primary User Activity

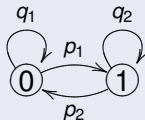
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<sup>6</sup>[Shannon, 1948]

# Widely Held Hypothesis

## Hypothesis

Primary User Activity is a Markovian Process.



- PU Activity Depends Only On Previous State(s)
- This Is The PMF We Could Use To Measure BW Loss
- But Is This Hypothesis Correct?

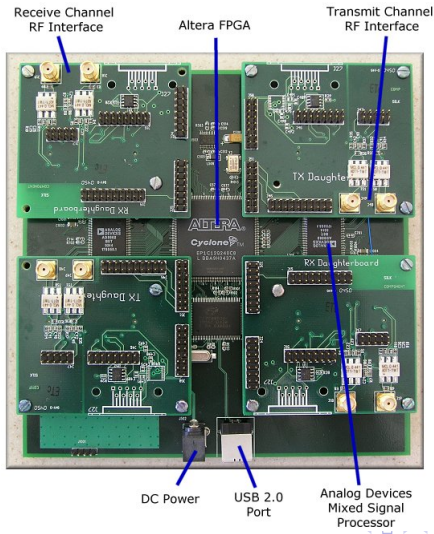
# Problem Statement

## Problem Statement

We Wish to Measure The Bandwidth Required of a Collaborative Sensing, Cognitive Radio Control Channel.

- Cognitive Radio Needs Collaborative Spectrum Sensing
- This Will Require a Control Channel
- Control Channel Wastes Some BW
- We Assume The Markovian Hypothesis (For Now)

# Universal Software Radio Peripheral



# GNU Radio

- GNU General Public License
- Python Wrapper For C++
- Object Orientated Approach
- Software Radios Defined In Terms Of Graphs
  - 1 Define Source (USRP)
  - 2 Define Signal Processing Unit (Spectrum Analyzer)
  - 3 Define Sink (File Format)
  - 4 Connect!

# Class Definition

```
class my_graph(gr.flow_graph):  
    def __init__(self, min_freq, max_freq):  
        gr.flow_graph.__init__(self)  
        self.u = usrp.source_c(...)  
  
        s2v = gr.stream_to_vector(...)  
        c2mag = gr.complex_to_mag_squared(...)  
        stats = gr.bin_statistics_f(...)  
  
        self.connect(self.u, s2v, c2mag, stats)
```



# File Format

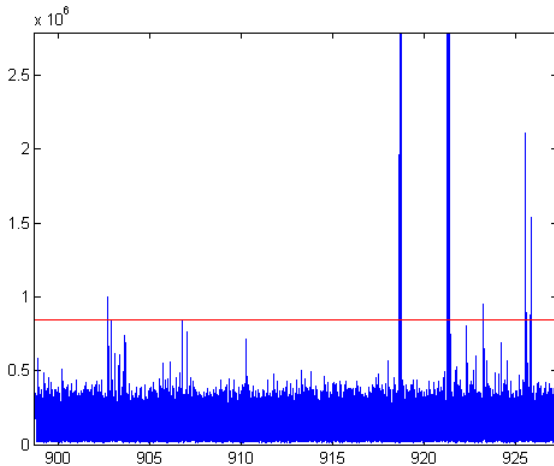
TimeDate Stamp	Frequency	Complex Samples
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10/29/07 05:56 PM	898750000	56953 32489 ...
10/29/07 05:56 PM	900250000	322640 358258 ...
10/29/07 05:56 PM	901750000	284045 303849 ...
10/29/07 05:56 PM	903250000	46261 40136 ...

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# Sampled ISM Band



# Public Safety Band Revisited<sup>7</sup>

- Count State Transitions
- Divide By Sample Count
- We Then Have Our PMF

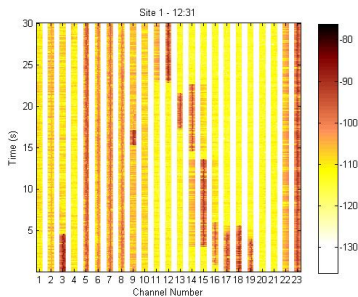


Figure: PSB Usage

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<sup>7</sup>[Jones, 2007]

# Challenges

## A Lot to Learn

- DSP, Embedded Systems, Information Theory
- BASH, Python, Linux System Administration
- Deciphering Professor's Code!

## A Lot of Obstacles

- Non-linear AGC and CIC Filters
- Calibrating USRP
- Minimal Documentation





# Progress

- Software Defined ISM Band Spectrum Analyzer
- Matlab Scripts to Analyze Data
- BASH Scripts to Automate Data Collection
- Debian Domain Controller to Share USRP Access
- Custom File Format

# Future Work

- Finish Statistical Analysis
- Mobile Spectrum Sensing
- Emulab Data Collection
- Online Database of Samples
- Investigate Cyclostationary Feature Detection

# Questions?

-  FCC, *ET Docket No 03-222, Notice Of Proposed Rule Making And Order*, Dec. 2003
-  Committee on Energy and Commerce, House of Representatives, "Commercial Spectrum Enhancement Act", *Report to Congress on Agency Plans for Spectrum Relocation Funds*, Feb. 2007
-  Jones, S., et. al., "Characterization of Spectrum Activities in the U.S. Public Safety Band for Opportunistic Spectrum Access", *New Frontiers in Dynamic Spectrum Access Networks*, 2007, pp.137-146
-  Haykin, S., et. al., "Cognitive Radio: Brain-Empowered Wireless Communications", *Selected Areas in Communications*, Vol. 23, No.2, Feb. 2002
-  Ghasemi, A., et. al., "Collaborative Spectrum Sensing for Opportunistic Access in Fading Environments," *Proc. Symposium on Dynamic Spectrum Access Networks*, Nov. 2005.
-  Shannon, C., "A Mathematical Theory of Communication", *The Bell System Technical Journal*, Vol. 27, pp. 370-423, 623-656, July, Oct., 1948.