List 1

| 0 | 0000 |
| :---: | :---: |
| 4 | 0100 |
| 8 | 1000 |
| 10 | 1010 |
| 12 | 1100 |
| 11 | 1011 |
| 13 | 1101 |
| 15 | 1111 |

List 2

| 0,4 | 0 | x | 0 | 0 |
| :---: | :---: | :---: | :---: | :---: |
|  | $\checkmark$ |  |  |  |
| 0,8 | x | 0 | 0 | 0 |
| $\checkmark$ |  |  |  |  |
| 8,10 | 1 | 0 | x | 0 |
|  |  |  |  |  |
| 4,12 | x | 1 | 0 | 0 |
|  | $\checkmark$ |  |  |  |
| 8,12 | 1 | x | 0 | 0 |
| 10,11 | 1 | 0 | 1 | x |
| 12,13 | 1 | 1 | 0 | x |
| 11,15 | 1 | x | 1 | 1 |
| 13,15 | 1 | 1 | x | 1 |

List 3


Figure 4.36. Generation of prime implicants for $f=\sum m(0,4,8,10,11,12,13,15)$.

| Prime implicant | Minterm |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 0 | 4 | 8 | 10 | 11 | 12 | 13 | 15 |
| $p_{1}=10 \times 0$ |  |  | $\checkmark$ | $\checkmark$ |  |  |  |  |
| $p_{2}=1001 \mathrm{x}$ |  |  |  | $\checkmark$ | $\checkmark$ |  |  |  |
| $p_{3}=1100 \mathrm{x}$ |  |  |  |  |  | $\checkmark$ | $\checkmark$ |  |
| $p_{4}=1 \times 11$ |  |  |  |  | $\checkmark$ |  |  | $\checkmark$ |
| $p_{5}=1 \begin{array}{llll}1 & \mathrm{x} & 1\end{array}$ |  |  |  |  |  |  | $\checkmark$ | $\checkmark$ |
|  | $\checkmark$ | $\checkmark$ | $\checkmark$ |  |  | $\checkmark$ |  |  |

(a) Initial prime implicant cover table

| Prime <br> implicant | Minterm |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
| $p_{1}$ | 11 | 13 | 15 |  |
| $p_{2}$ | $\checkmark$ |  |  |  |
| $p_{3}$ |  | $\checkmark$ |  |  |
| $p_{4}$ |  |  | $\checkmark$ |  |
| $p_{5}$ |  | $\checkmark$ |  | $\checkmark$ |
|  |  |  | $\checkmark$ | $\checkmark$ |

(b) After the removal of essential prime implicants

| Prime <br> implicant | Minterm |  |  |  |
| :--- | :---: | :---: | :---: | :---: |
| $p_{2}$ | $\checkmark$ | $\checkmark$ |  |  |
| $p_{4}$ |  | $\checkmark$ |  | $\checkmark$ |
| $p_{5}$ |  |  | $\checkmark$ | $\checkmark$ |

(c) After the removal of dominated rows

Figure 4.37. Selection of a cover.

List 1

| 0 | 0000 |
| :---: | :---: |
| 1 | 0001 |
| 2 | 0010 |
| 8 | 1000 |
| 5 | 0101 |
| 6 | 0110 |
| 9 | 1001 |
| 12 | 1100 |
| 7 | 0111 |
| 13 | 1101 |
| 15 | 1111 |

List 2


List 3

| $0,1,8,9$ | x 00 | 0 | x |  |
| :--- | :--- | :--- | :--- | :--- |
| $1,5,9,13$ | x x x | 0 | 1 |  |
| $8,9,12,13$ | 1 | $x$ | 0 | x |
| $5,7,13,15$ | x 1 | 1 | x | 1 |

Figure 4.38. Generation of prime implicants for $f=\sum m(0,2,5,6,7,8,9,13)+D(1,12,15)$.

(a) Initial prime implicant cover table

| Prime implicant | Minterm |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 0 | 2 | 5 | 6 | 7 | 8 |
| $p_{1}=00 \times 0$ | $\checkmark$ | $\checkmark$ |  |  |  |  |
| $p_{2}=0 \times 10$ |  | $\checkmark$ |  | $\checkmark$ |  |  |
| $p_{3}=0 \begin{array}{llll}0 & 1\end{array}$ |  |  |  | $\checkmark$ | $\checkmark$ |  |
| $p_{4}=\mathrm{x} 000 \mathrm{x}$ | $\checkmark$ |  |  |  |  | $\checkmark$ |
| $p_{5}=\mathrm{x} \times \mathrm{x} 01$ |  |  | $\checkmark$ |  |  |  |
| $p_{6}=1 \mathrm{x} 0 \mathrm{x}$ |  |  |  |  |  | $\checkmark$ |
| $p_{7}=\mathrm{x} 11 \mathrm{x} 1$ |  |  | $\checkmark$ |  | $\checkmark$ |  |

(b) After the removal of columns 9 and 13

(c) After the removal of rows $p_{5}$ and $p_{6}$

(d) After including $p_{4}$ and $p_{7}$ in the cover

Figure 4.39. Selection of a cover.

| Prime <br> implicant |  |  | Minterm |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $p_{1}$ | $=$ | 0 | 0 | x | x | $\checkmark$ | $\checkmark$ |  |  |
| $p_{2}$ | $=$ | x | 0 | x | 0 | $\checkmark$ |  | $\checkmark$ |  |
| $p_{3}$ | $=$ | x | 0 | 1 | x |  | $\checkmark$ | $\checkmark$ |  |
| $p_{4}$ | $=$ | x | x | 1 | 1 |  | $\checkmark$ |  | $\checkmark$ |
| $p_{5}$ | $=$ | 1 | x | 1 | x |  |  |  |  |

(a) Initial prime implicant cover table

| Prime <br> implicant | Minterm <br> 0 |  |
| :---: | :---: | :---: |
| $p_{1}$ | $\checkmark$ |  |
| $p_{2}$ | $\checkmark$ |  |
| $p_{4}$ |  | $\checkmark$ |
| $p_{5}$ |  | $\checkmark$ |

(b) After including $p_{2}$ in the cover

| Prime | Minterm |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
| implicant | 0 | 3 | 10 | 15 |
| $p_{1}$ | $\checkmark$ | $\checkmark$ |  |  |
| $p_{2}$ | $\checkmark$ |  | $\checkmark$ |  |
| $p_{4}$ |  | $\checkmark$ |  | $\checkmark$ |
| $p_{5}$ |  |  | $\checkmark$ | $\checkmark$ |

(c) After excluding $p_{2}$ from the cover

Figure 4.40. Selection of a cover for the function in Figure 4.15.

