

FREQUENCY DOMAIN AND FDTD

WHEN INTERESTED IN RESULTS AT A PARTICULAR FREQUENCY, WE CAN RUN A SIMULATION USING A SINUSOIDAL EXCITATION AT THE FREQUENCY OF INTEREST, OR WE CAN FEED THE SYSTEM WITH AN IMPULSE (APPROXIMATED USING A NARROW GAUSSIAN PULSE) AND THEN CONVERT THE RESULTS TO FREQUENCY DOMAIN AND ANALYSE THE POINT AND FREQUENCY OF INTEREST.

IF WE WANT TO CALCULATE THE FOURIER TRANSFORM OF THE E FIELD $\bar{E}(t)$ AT A FREQUENCY f , WE CAN USE:

$$\bar{E}(f) = \int_0^{t_T} \bar{E}(t) \cdot e^{-j2\pi f t} dt$$

0 ← IMPLYING OUR SIGNALS ARE CAUSAL

REWRITING USING THE FINITE DIFFERENCE APPROXIMATION,

$$\bar{E}(f) = \sum_{i=0}^n \bar{E}(i \cdot \Delta t) e^{-j2\pi f (i \Delta t)}$$

WHERE n IS OUR CURRENT TIME STEP NUMBER, SEPARATING REAL AND IMAGINARY PARTS,

$$\bar{E}(f) = \sum_{i=0}^n \bar{E}(i \Delta t) \cdot \cos(2\pi f \Delta t i) - j \sum_{i=0}^n \bar{E}(i \Delta t) \sin(2\pi f \Delta t i)$$

IN TERMS OF COMPUTER CODE, FOR OUR 1D CASE,

$$\begin{cases} \text{REAL_PART}(m, k) = \text{REAL_PART}(m, k) + E_x(k) * \cos(2 * \pi * \text{FREQ}(m) * dt * n) \\ \text{IMAG_PART}(m, k) = \text{IMAG_PART}(m, k) + E_x(k) * \sin(2 * \pi * \text{FREQ}(m) * dt * n) \end{cases}$$

WHERE

k INDICATES POSITION

m INDICATES INDEX INSIDE FREQUENCY VECTOR $\text{FREQ}()$

AMPLITUDE AND PHASE FOR EACH POINT AND FREQUENCY ARE:

$$\begin{cases} \text{AMPLITUDE}(m, k) = \sqrt{\text{REAL_PART}(m, k)^2 + \text{IMAG_PART}(m, k)^2} \\ \text{PHASE}(m, k) = \text{ATAN2}(\text{IMAG_PART}(m, k) / \text{REAL_PART}(m, k)) \end{cases}$$

OR $\text{PHASE}(m, k) = \text{ATAN2}(\text{IMAG_PART}(m, k), \text{REAL_PART}(m, k))$