

GAUSS'S LAW FOR MAGNETIC FIELDS ~~(LAW)~~

B FIELD (MAGNETIC FLUX DENSITY, OR MAGNETIC INDUCTION)

① DEFINED AS THE MAGNETIC FORCE EXPERIENCED BY A MOVING CHARGED PARTICLE.

FROM THE LORENTZ EQUATION

$$\vec{F} = q [\vec{E} + (\vec{v} \times \vec{B})] \quad \leftarrow \text{LORENTZ EQUATION}$$

AND

$$\vec{F}_B = q (\vec{v} \times \vec{B}) \quad \boxed{\text{EXAMPLES: RAILGUN}}$$

WHERE \vec{F}_B IS THE MAGNETIC FORCE, q IS THE PARTICLE CHARGE, \vec{v} IS THE PARTICLE VELOCITY WITH RESPECT TO \vec{B} , AND \vec{B} IS THE MAGNETIC FIELD.

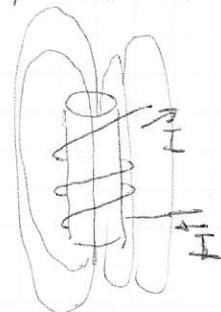
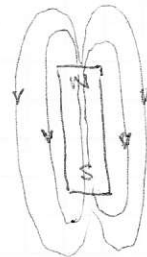
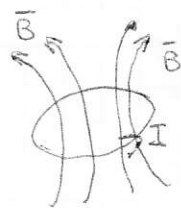
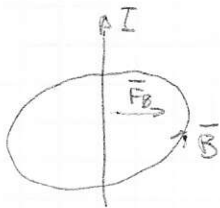
② \vec{B} HAS UNITS OF $\frac{N}{C \text{ (m/s)}} = \frac{Vs}{m^2} = \frac{N}{Am} = \frac{Kg}{Cs} = T$

③ COMPARING $\vec{F}_E = q\vec{E}$ AND $\vec{F}_B = q(\vec{v} \times \vec{B})$,

- \vec{F}_E IS PARALLEL TO THE ~~FORCE~~ ^{FIELD}, \vec{F}_B IS PERPENDICULAR TO THE \vec{B} FIELD.
- WITH \vec{B} , WE NEED TO CONSIDER THE SPEED AND DIRECTION OF THE PARTICLE.
- THE COMPONENT OF \vec{F}_B IN THE DIRECTION OF DISPLACEMENT OF THE PARTICLE IS ZERO. THEN, A \vec{B} FIELD CANNOT DO WORK ON A CHARGED PARTICLE.
- ELECTROSTATIC FIELDS ARE PRODUCED BY ELECTRIC CHARGES, BUT MAGNETOSTATIC FIELDS ARE PRODUCED BY ELECTRIC CURRENTS.

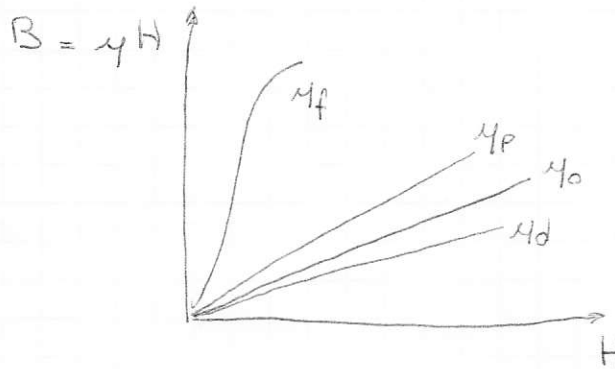
④ MAGNETIC FIELDS MAY BE REPRESENTED BY LINES.

⑤ THE NET MAGNETIC FIELD AT A GIVEN POINT IS THE VECTOR SUM OF ALL MAGNETIC FIELDS PRESENT AT THAT POINT. BECAUSE OF THAT, MAGNETIC FIELD LINES NEVER CROSS.



MAGNETIC PERMEABILITY (μ_0)

MEASURES THE ABILITY OF A MATERIAL TO SUPPORT THE FORMATION OF A MAGNETIC FIELD WITHIN ITSELF, THE DEGREE OF MAGNETIZATION INSIDE THE MATERIAL IN RESPONSE TO AN APPLIED B FIELD.



~~μ_0 IS MEASURED IN~~

μ_0 VALUE IS $4\pi \times 10^{-7}$ $\left[\frac{H}{m} = \frac{N}{A^2} \right]$

MATERIALS CAN BE CLASSIFIED DEPENDING ON THEIR PERMEABILITY IN:

- ① FERROMAGNETIC: μ_f MATERIAL BECOMES PERMANENTLY MAGNETIZED BY EXTERNAL FIELD (UNTIL).
- ② PARAMAGNETIC: $\mu_p > 1$. WEAK MAGNETIZATION IN MATERIAL IN THE PRESENCE OF EXTERNAL MAGNETIC FIELD.
- ③ DIAMAGNETIC: $\mu < 1$. WEAK EFFECT, BUT STRONG IN SUPER CONDUCTORS. MATERIAL CREATES A INTERNAL MAGNETIC FIELD OPPOSING THE EXTERNAL FIELD.

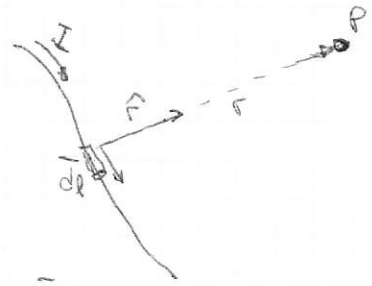
μ VARIES WITH POSITION, FREQUENCY, HUMIDITY, TEMPERATURE, ETC.

BECAUSE OF THIS, COMPLEX PERMITTIVITY IS USED SOMETIMES AT HIGH-FREQUENCY FREQ. DOMAIN TREATMENTS TO ACCOUNT FOR LAG (AS PHASE), AND SOME OTHER TIMES μ IS MODELED AS A RANK 2 TENSOR TO ACCOUNT FOR ANISOTROPIC MEDIUM.

BIOT-SAVART LAW

$$d\vec{B} = \frac{\mu_0}{4\pi} \frac{I d\vec{l} \times \hat{r}}{r^2}$$

WHERE μ_0 IS THE MAGNETIC PERMEABILITY OF FREE SPACE, I IS THE CURRENT THROUGH THE SMALL ELEMENT, $d\vec{l}$ IS THE DIFFERENTIAL VECTOR WITH THE LENGTH OF A CURRENT ELEMENT IN THE DIRECTION OF THE CURRENT, \hat{r} POINTS TO THE POINT IN WHICH \vec{B} IS TO BE DETERMINED, AND r IS THE DISTANCE BETWEEN $d\vec{l}$ AND P .



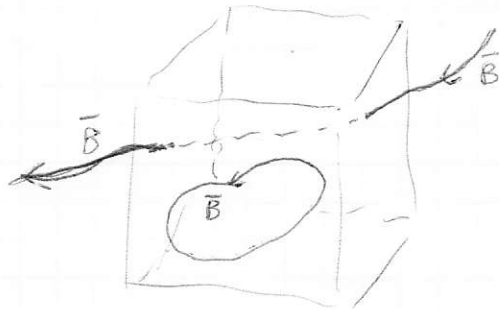
\vec{B} FIELD AT P IS DETERMINED BY ADDING ALL THE DIFFERENTIAL CONTRIBUTIONS.

GAUSS'S LAW FOR MAGNETIC FIELDS (INTEGRAL)

$$\oint_S \vec{B} \cdot \hat{n} ds = 0$$

THE TOTAL MAGNETIC FLUX PASSING THROUGH ANY CLOSED SURFACE IS ZERO.

THIS IS DUE TO THE FACT THAT FOR EVERY LINE ENTERING THE CLOSED SURFACE THERE IS A FIELD LINE EXITING THE SURFACE (LINES FORM CLOSED LOOPS).



Φ_B = MAGNETIC FLUX THROUGH A SURFACE.

Φ_B IS A SCALAR QUANTITY, MEASURED IN $Wb = T m^2$.

FOR AN ARBITRARY SURFACE,

$$\Phi_B = \int_S \vec{B} \cdot \hat{n} ds \quad [Wb]$$