

UNIVERSITY OF UTAH  
ELECTRICAL AND COMPUTER ENGINEERING DEPARTMENT

ECE 5324/6324

HOMEWORK ASSIGNMENT  
Problems 31-39

Spring 2012

31. a. Write a computer program to calculate the pattern factor  $F(\theta)$  from page 6 of the Class Notes for a center-fed dipole of length  $L$ .
- b. Using this computer program, calculate and plot the variation of power density  $S/S_{\max} = F^2(\theta)/F^2(\theta)_{\max}$  for the following dipoles.
1.  $L/\lambda = 1.6$
  2.  $L/\lambda = 2.0$
- for angles  $1^\circ < \theta < 179^\circ$  in steps of  $\Delta\theta = 2^\circ$ .
- c. Calculate the directivity  $D$  of the above two antennas using the expression for directivity  $D$  given on page 6 of the Class Notes. Use Fig. 5-5 on p. 170 of the Text to get  $R_a$  of these dipoles.
- d. Compare the angles of maximum radiation and the directivities of the  $L = 1.6\lambda$  and  $L = 2.0\lambda$  antennas with those calculated for a  $L = 1.5\lambda$  dipole in Fig. 5-4 of the Text.
32. Calculate the gain and input impedance of a  $0.625\lambda$  slot antenna at 1000 MHz. Take the width  $W$  of the slot to be 1.0 cm and the equivalent radius "a" of the complementary  $0.625\lambda$  dipole to be  $0.25 W$  (see p. 173 Fig. 5-8 of the text).
33. Calculate the gain of a slot antenna of dimensions  $29 \text{ cms} \times 2.0 \text{ cms}$  for use at a frequency of 500 MHz. Calculate the center-feed-point impedance for this antenna.
34. Similar to a dipole in Fig. 5-19 of the text, a **slot antenna** of length  $L = 0.475\lambda$  may be fed off-center to obtain an input impedance  $Z_s$  of the slot to be 50 ohms. Assuming that the feed point impedance of the complementary  $0.475\lambda$  dipole is  $70 + j0$  ohms if it were fed in the center, calculate the distance  $Z_f$  to use to obtain  $Z_s = 50\Omega$  for a signal frequency  $f = 1000$  MHz.
35. a. Calculate and plot the normalized  $\rho'/a$  profiles of the parabolic reflector antennas from Eq. 7-182 of the textbook

$$(\rho')^2 = 4F(F - z_f) \qquad 7-182$$

for the two different values of  $F/D = 0.45, 0.65$ . Note that  $D = 2a$  is the diameter of the parabolic antenna. Plot the profile of the reflector antennas in the  $yz$  plane for  $0 \leq \rho'/a \leq 1$ .

- b. Calculate the angle  $\theta_0$  in Fig. 7-25b subtended by the parabolic antenna at the focal point for the two parabolic antennas of part a. Compare your results with the table given in Fig. 7-26 of the text.
36. a. Design a pyramidal horn antenna to obtain half-power beam widths in E- and H- planes that are one half of the angle  $2\theta_0$  subtended by the parabolic antenna of  $F/D = 0.65$  at the focal point.
- b. Using Eqs. 7-58(a) and 7-58(b), calculate and plot for the horn antenna the variation of  $F_H$  and  $F_E$  as functions of  $\theta$  for  $0 \leq \theta \leq \theta_0$  where  $\theta_0$  is the angle calculated for  $F/D = 0.65$  parabolic antenna in Problem 33.
  - c. Calculate the edge illumination factor  $C$  defined on p. 320 of the text for this horn antenna used for the  $F/D = 0.65$  parabolic antenna.
  - d. Can you modify the dimensions  $A$  and  $B$  of the horn antenna to obtain an edge illumination of  $C_{dB} = -12$  dB?
  - e. For the optimum design of part d, compare the aperture fields  $E_a$  vs.  $\rho'$  with  $n = 1$  and  $n = 2$  type parabolic variations of illumination functions given on p. 320 of the text.
37. A 12.5 GHz microwave communication link uses a parabolic transmitting antenna of diameter 9 feet. Calculate the power density at a receiving site a distance of 25 miles away for a transmitter power of 10W.

What is the attenuation in decibels of the microwave link if an identical antenna is used for the receiver?

Assume  $m = 1$  distribution of excitation for transmitting and receiving antennas.

38. Calculate the power received from the DBS by a parabolic antenna of specifications given in the following:

$$D = 1.5'$$

$$f/D = 0.45$$

$$\text{Frequency} = 12.1 - 12.7 \text{ GHz (center frequency} = 12.4 \text{ GHz)}$$

It is given that the DBS radiates a power of 100 W per channel and the effective area of the transmitting antenna is  $3.5 \text{ m}^2$ . The DBS is in a synchronous orbit at a distance of 40,000 km from the receiving site.

Account for the atmospheric loss in your calculations assuming an effective atmospheric height of 20 km.

What is the signal-to-noise ratio of the received signal if  $T_o = 300^\circ \text{K}$ ;  $F_n = 2.5$  for the receiver?

39. A radar antenna is to be designed to provide a “viewing” range of 100 miles for a 250 KW, 11,000 MHz transmitter. The above range is desired for target cross sections as small as  $20 \text{ m}^2$  (this is a typical cross section for an aircraft). The radar receiver has a noise figure of 6.0 dB and a bandwidth of 4 MHz and the minimum signal-to-noise ratio for reliable detection is 5.

Calculate the gain needed for the radar antenna.