

## Antenna Theory and Design

(homework 5)

4.5-1) given frequency  $f = 1.62 \text{ GHz}$ ;  $R = 1500 \text{ km}$

$$\text{Gain} = 29 \text{ dB}$$

$$\text{Receiver Power } P_r = -100 \text{ dBm}$$

$$G_r = 10 \text{ dB}$$

We have Friis Transmission Formula as

$$P_r(\text{dBm}) = P_t(\text{dBm}) + G_t(\text{dB}) + G_r(\text{dB}) - 20 \log R(\text{km}) - 20 \log f(\text{MHz}) - 32.44$$

$$-100 = P_t(\text{dBm}) + 29 + 10 - 20 \log 1500 - 20 \log (1.620) - 32.44$$

$$-100 = P_t(\text{dBm}) + 30 - 63.52 - 64.19 - 32.44$$

$$-100 = P_t(\text{dBm}) - 130.15$$

$$P_t(\text{dBm}) = 30.15 \text{ dBm}$$

4.5-2) given frequency  $f = 85 \text{ MHz}$

$$G_t = 10 \text{ dB}$$

$$P_t = 20 \text{ W}$$

$$G_r = 3 \text{ dB}$$

$$R = 20 \text{ km}$$

Calculating  $P_r$

Converting  $P_t = 20\text{W}$  to  $P_t(\text{dBm})$

$$P(\text{dBm}) = 10 \log_{10} \left( \frac{P(\text{watt})}{1 \text{ watt}} \right) + 30$$

$$= 10 \log_{10} \left( \frac{20}{1} \right) + 30$$

$$= 10(1.301) + 30$$

$$P_t(\text{dBm}) = 43.01 \text{ dBm}$$

Using same formulae, we used in 4.5.1)

$$P_{\text{br}}(\text{dBm}) = P_t(\text{dBm}) + G_T(\text{dB}) + G_R(\text{dB}) \\ - 20 \log R(\text{km}) - 20 \log f(\text{MHz}) - 32.44$$

$$P_{\text{br}}(\text{dBm}) = 43.01 + 10 + 3 - 20 \log 20 \\ - 20 \log 850 - 32.44$$

$$= 43.01 + 10 + 3 - 26.02 - 58.5 - 32.44$$

$$= -60.95 \text{ dBm}$$

$P_{\text{br}}$  in watts can be given by

$$P(\text{watts}) = 1\text{W} \cdot 10^{[(\text{dBm}) - 30]/10}$$

$$P_{\text{br}} = 1\text{W} \cdot 10^{[-60.95 - 30]/10}$$

$$P_{\text{br}}(\text{watts}) = 1.88 \times 10^{-10} \text{ watts}$$