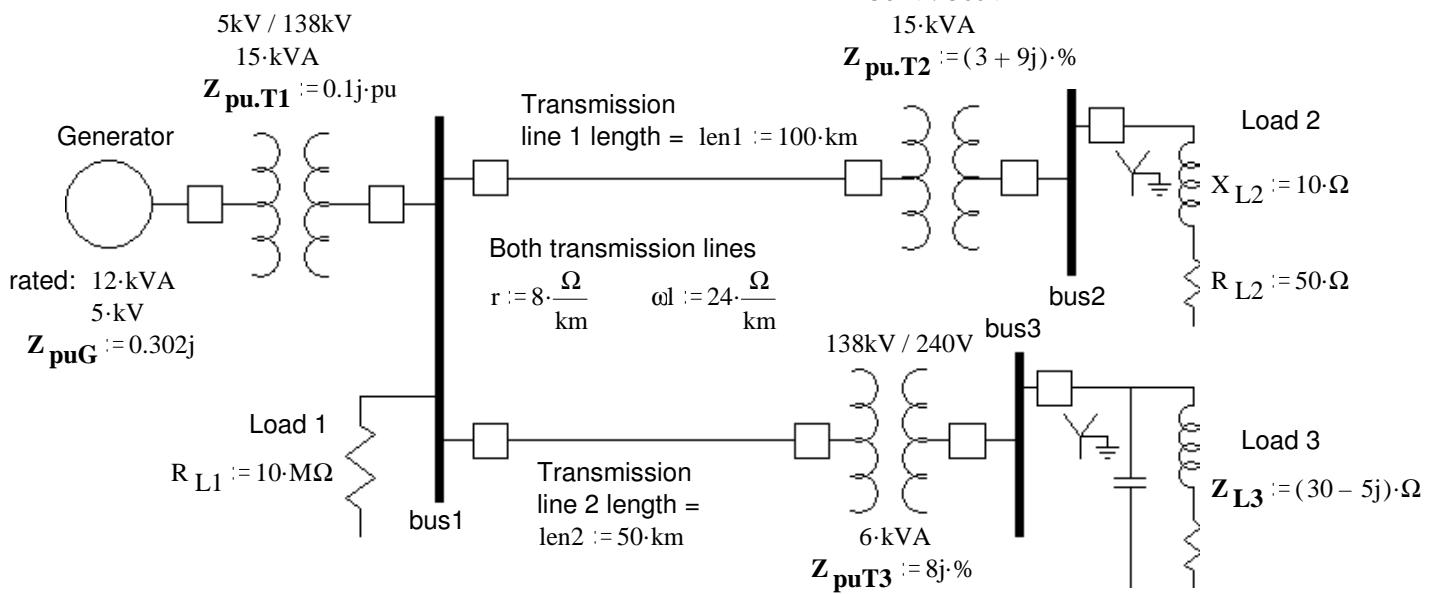


ECE 3600 Per-Unit Example

Like problem 4 on homework

A one-line diagram of a 3 ϕ system is shown below. Manufacturer's information is shown for the generator and each transformer.



a) Choose an S_{base} to minimize the per-unit base conversions. Then choose regions and a V_{base} for each region.

$$S_{base} := 15 \cdot \text{kVA}$$

Region 1 The generator

$$V_{base1} := 5 \cdot \text{kV}$$

Region 2 Bus1, Load 1 and the transmission lines $V_{base2} := 138 \cdot \text{kV}$

Region 3 Bus2 and Load 2 $V_{base3} := 360 \cdot \text{V}$

Region 4 Bus2 and Load 3 $V_{base4} := 240 \cdot \text{V}$

b) Find I_{base} and Z_{base} in each of the regions.

$$\text{Region 1 } I_{base1} := \frac{S_{base}}{\sqrt{3} \cdot V_{base1}} \quad I_{base1} = 1.732 \cdot \text{A} \quad Z_{base1} := \frac{V_{base1}^2}{S_{base}} \quad Z_{base1} = 1.667 \cdot \text{k}\Omega$$

$$\text{Region 2 } I_{base2} := \frac{S_{base}}{\sqrt{3} \cdot V_{base2}} \quad I_{base2} = 0.063 \cdot \text{A} \quad Z_{base2} := \frac{V_{base2}^2}{S_{base}} \quad Z_{base2} = 1.27 \cdot 10^3 \cdot \text{k}\Omega$$

$$\text{Region 3 } I_{base3} := \frac{S_{base}}{\sqrt{3} \cdot V_{base3}} \quad I_{base3} = 24.056 \cdot \text{A} \quad Z_{base3} := \frac{V_{base3}^2}{S_{base}} \quad Z_{base3} = 8.64 \cdot \Omega$$

$$\text{Region 4 } I_{base4} := \frac{S_{base}}{\sqrt{3} \cdot V_{base4}} \quad I_{base4} = 36.084 \cdot \text{A} \quad Z_{base4} := \frac{V_{base4}^2}{S_{base}} \quad Z_{base4} = 3.84 \cdot \Omega$$

c) Make the necessary per-unit S_{base} conversions.

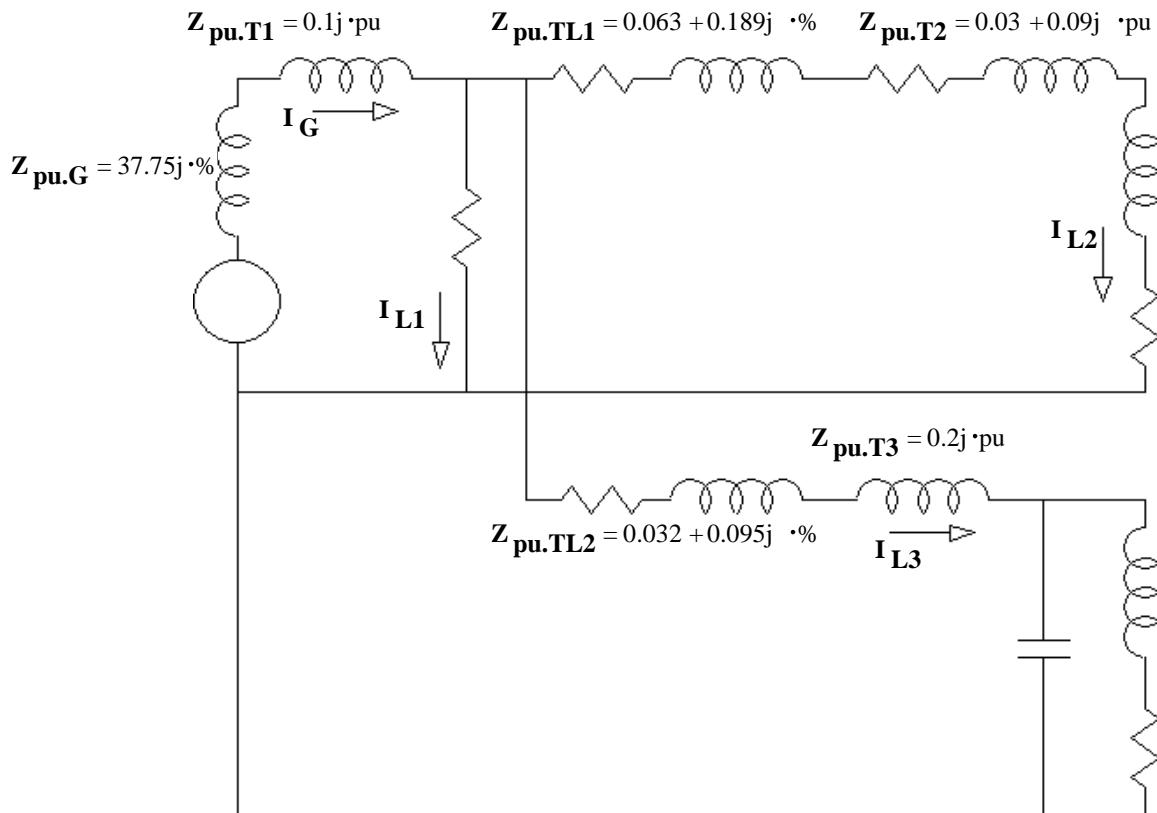
$$Z_{pu.G} := Z_{puG} \cdot \frac{S_{base}}{12 \cdot \text{kVA}} \quad Z_{pu.G} = 0.378j \cdot \text{pu} \quad Z_{pu.T3} := Z_{puT3} \cdot \frac{S_{base}}{6 \cdot \text{kVA}} \quad Z_{pu.T3} = 0.2j \cdot \text{pu}$$

d) Find the impedances of the two transmission lines and convert to pu.

$$Z_{\text{TL1}} := (8 + 24j) \cdot \frac{\Omega}{\text{km}} \cdot \text{len1} \quad Z_{\text{TL1}} = 0.8 + 2.4j \cdot \text{k}\Omega \quad Z_{\text{pu.TL1}} := \frac{Z_{\text{TL1}}}{Z_{\text{base2}}} \quad Z_{\text{pu.TL1}} = 0.063 + 0.189j \cdot \%$$

$$Z_{\text{TL2}} := (8 + 24j) \cdot \frac{\Omega}{\text{km}} \cdot \text{len2} \quad Z_{\text{TL2}} = 0.4 + 1.2j \cdot \text{k}\Omega \quad Z_{\text{pu.TL2}} := \frac{Z_{\text{TL2}}}{Z_{\text{base2}}} \quad Z_{\text{pu.TL2}} = 0.032 + 0.095j \cdot %$$

e) Draw the per-phase diagram showing all the per-unit numbers found or given so far.



ALL calculations made to this point **ONLY need to be made ONCE** for this system and S_{base} !!

f) Find the pu values of the 3 loads and add that information to the per-phase diagram.

$$R_{pu.L1} := \frac{R_{L1}}{Z_{base2}}$$

$$R_{pu.L1} = 7.876 \cdot pu$$

$$R_{pu.L2} := \frac{R_{L2}}{Z_{base3}}$$

$$R_{pu.L2} = 5.787 \cdot pu$$

$$X_{pu.L2} := \frac{X_{L2}}{Z_{base3}}$$

$$X_{pu.L2} = 1.157 \cdot pu$$

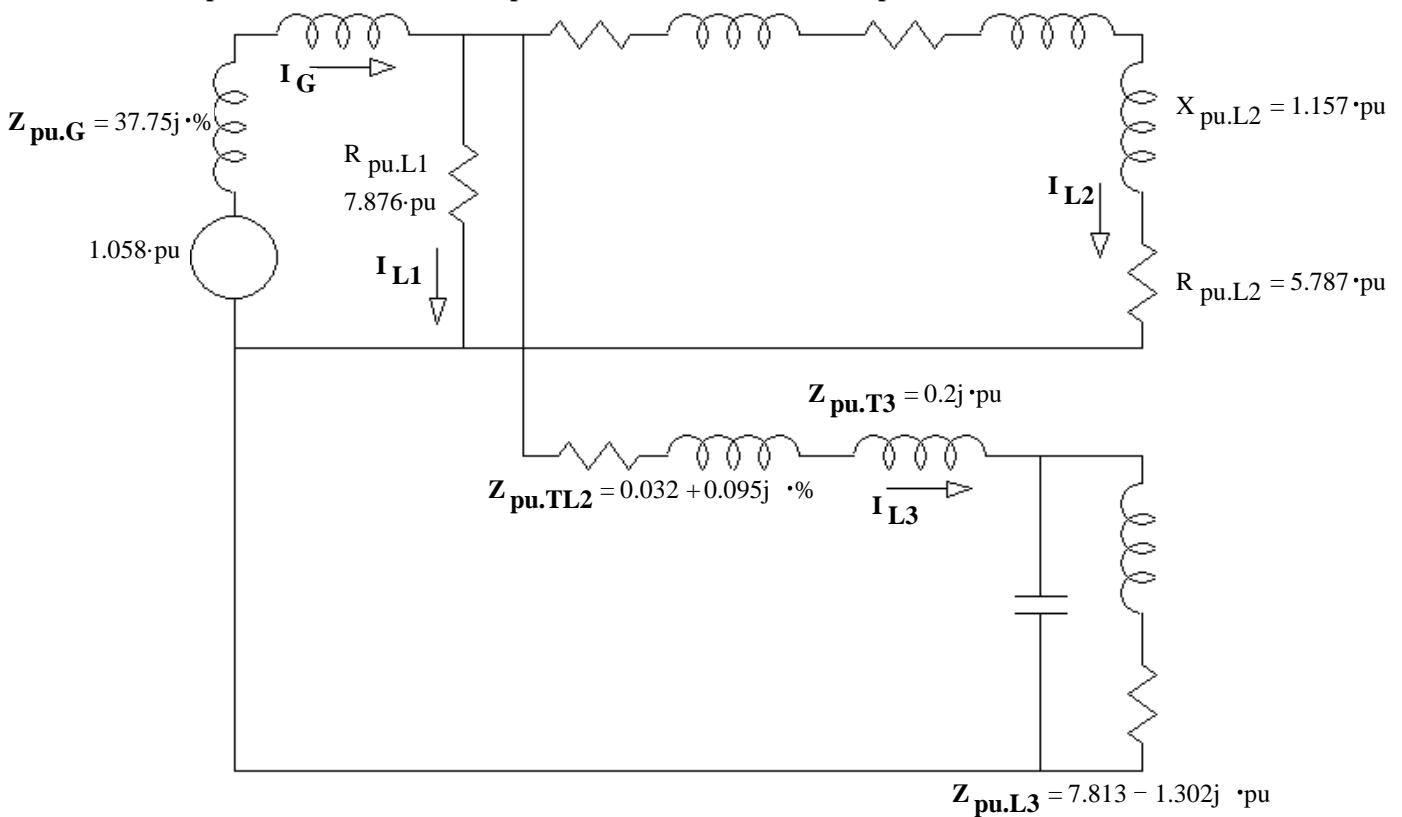
$$Z_{pu.L3} := \frac{Z_{L3}}{Z_{base4}}$$

$$Z_{pu.L3} = 7.813 - 1.302j \cdot pu$$

$$Z_{pu.T1} = 0.1j \cdot pu$$

$$Z_{pu.TL1} = 0.063 + 0.189j \cdot \%$$

$$Z_{pu.T2} = 0.03 + 0.09j \cdot pu$$



g) The line voltage at bus1 is measured and found to be $V_{bus1} := 146 \cdot kV$. Assume a phase angle of 0° for the pu value.

Find all 3 load line-current magnitudes and the magnitude of the generator line-current. Please remember that you can't add magnitudes, so may need some complex values.

$$V_{pu.bus1} := \frac{146 \cdot kV}{V_{base2}}$$

$$V_{pu.bus1} = 1.058 \cdot pu$$

$$I_{pu.L1} := \frac{V_{pu.bus1}}{R_{pu.L1}}$$

$$I_{pu.L1} = 0.134 \cdot pu$$

$$|I_{pu.L1}| \cdot I_{base2} = 8.429 \cdot mA$$

$$I_{pu.L2} := \frac{V_{pu.bus1}}{Z_{pu.TL1} + Z_{pu.T2} + (R_{pu.L2} + X_{pu.L2} \cdot j)}$$

$$I_{pu.L2} = 0.174 - 0.037j \cdot pu$$

$$|I_{pu.L2}| \cdot I_{base3} = 4.277 \cdot A$$

$$I_{pu.L3} := \frac{V_{pu.bus1}}{Z_{pu.TL2} + Z_{pu.T3} + Z_{pu.L3}}$$

$$I_{pu.L3} = 0.133 + 0.019j \cdot pu$$

$$|I_{pu.L3}| \cdot I_{base4} = 4.839 \cdot A$$

$$I_{pu.G} := I_{pu.L1} + I_{pu.L2} + I_{pu.L3}$$

$$I_{pu.G} = 44.094 - 1.862j \cdot \%$$

$$|I_{pu.G}| \cdot I_{base1} = 0.764 \cdot A$$

h) Find the power delivered to Load 2, both in pu and in kW.

$$P_{pu,L2} := (|I_{pu,L2}|)^2 \cdot R_{pu,L2} \quad P_{pu,L2} = 0.183 \cdot pu \quad P_{L2} := P_{pu,L2} \cdot S_{base} \quad P_{L2} = 2.744 \cdot kW$$

i) Find the line voltage at Load 2 (magnitude).

$$V_{Load2} := |I_{pu,L2}| \cdot \sqrt{R_{pu,L2}^2 + X_{pu,L2}^2} \cdot V_{base3} \quad V_{Load2} = 377.8 \cdot V$$

j) Find the line voltage at the generator (magnitude).

$$V_{pu,G} := V_{pu,bus1} + I_{pu,G} \cdot (Z_{pu,G} + Z_{pu,T1}) \quad V_{pu,G} = 106.686 + 21.055j \cdot \% \quad |V_{pu,G}| \cdot V_{base1} = 5.437 \cdot kV$$

k) The line voltage at bus1 drops by 8% to: $146 \cdot kV \cdot 0.92 = 134.32 \cdot kV$

Find the magnitude of Load-3 line current and repeat parts h) and i) for this new generator voltage.

Note: It may be helpful to realize that if one voltage in the system drops by 8%, so do all the rest, and so do all the currents. Drop by 8% means multiply by 0.92. All powers drop too, but use $(0.92)^2$ as the factor.

$$\text{new } I_{Load3} = |I_{pu,L3}| \cdot I_{base4} \cdot 0.92 = 4.5 \cdot A$$

$$\text{new } P_{L2} = P_{L2} \cdot 0.92^2 = 2.323 \cdot kW$$

$$\text{new } V_{Load2} = V_{Load2} \cdot 0.92 = 347.5 \cdot V$$