

Table A.4 Characteristics of aluminum cable, steel, reinforced (Aluminum Company of Ar

				Alum	เกมฑ		Steel										stan (Ohms pe		tor per N	1ile)		x _a Inductive Reactance (Ohms per Conductor per	x'a Shunt Capacitive Reactance (Megohms per
-	Code	Circular Mils			Strand Diameter		Strand Diameter	Outside Diameter	Copper Equivalent* Circular Mils or	Ultimate Strength	Weight (Pounds per	Geometric Mean Radius at 60 Hz	Approx. Current Carrying Capacity†	25°C	(77°F) \$	Small Cur	rents	50°C	(122°F) (75% Ca		pprox.	Mile at 1 Ft Spacing All Currents)	Conductor per Mile at 1 Ft Spacing)
	Word	Aluminum			(Inches)		(Inches)	(Inches)	A.W.G.	(Pounds)	Mile)	(Feet)	(Amps)	dc	25 Hz	50 Hz	60 Hz	dc	25 Hz	50 Hz	60 Hz	60 Hz	60 Hz
bigger	Joree Thrasher Kiwi Bluebird Chukar	2 515 000 2 312 000 2 167 000 2 156 000 1 781 000	76 76 72 84 84	 4 4 4	0.1819 0.1744 0.1735 0.1602 0.1456	19 19 7 19 19	0.0849 0.0814 0.1157 0.0961 0.0874	1.880 1.802 1.735 1.762 1.602		61 700 57 300 49 800 60 300 51 000		0.0621 0.0595 0.0570 0.0588 0.0534									0.0450 0.0482 0.0511 0.0505 0.0598	0.337 0.342 0.348 0.344 0.355	0.0755 0.0767 0.0778 0.0774 0.0802
Ŷ	Falcon Parrot Plover Martin Pheasant Grackle	1 590 000 1 510 500 1 431 000 1 351 000 1 272 000 1 192 500	54 54 54 54 54 54	3 3 3 3 3 3	0.1716 0.1673 0.1628 0.1582 0.1535 0.1486	19 19 19 19 19 19	0.1030 0.1004 0.0977 0.0949 0.0921 0.0892	1.545 1.506 1.465 1.424 1.382 1.338	1 000 000 950 000 900 000 850 000 800 000 750 000	56 000 53 200 50 400 47 600 44 800 43 100	10777 10237 9699 9160 8621 8082	0.0520 0.0507 0.0493 0.0479 0.0465 0.0450	1 380 1 340 1 300 1 250 1 200 1 160	0.0587 0.0618 0.0652 0.0691 0.0734 0.0783	0.0588 0.0619 0.0653 0.0692 0.0735 0.0784	0.0590 0.0621 0.0655 0.0694 0.0737 0.0786	0.0591 0.0622 0.0656 0.0695 0.0738 0.0788	0.0761 0.0808	0.0656 0.0690 0.0729 0.0771 0.0819 0.0872	0.0675 0.0710 0.0749 0.0792 0.0840 0.0894	0.0803 0.0851	0.359 0.362 0.365 0.369 0.372 0.376	0.0814 0.0821 0.0830 0.0838 0.0847 0.0857
	Finch Curlew Cardinal Canaty Crane Condor	1 113 000 1 033 500 954 000 900 000 874 500 795 000	54 54 54 54 54 54	3 3 3 3 3 3	0.1436 0.1384 0.1329 0.1291 0.1273 0.1214	19 7 7 7 7 7	0.0862 0.1384 0.1329 0.1291 0.1273 0.1214	1.293 1.246 1.196 1.162 1.146 1.093	700 000 650 000 600 000 566 000 550 000 500 000	40 200 37 100 34 200 32 300 31 400 28 500	7 544 7 019 6 479 6 112 5 940 5 399	0.0435 0.0420 0.0403 0.0391 0.0386 0.0368	1 110 1 060 1 010 970 950 900	0.0839 0.0903 0.0979 0.104 0.107 0.117	0.0840 0.0905 0.0980 0.104 0.107 0.118	0.0842 0.0907 0.0981 0.104 0.107 0.118	0.0909	0.0924 0.0994 0.1078 0.1145 0.1178 0.1288	0.0935 0.1005 0.1088 0.1155 0.1188 0.1308		0.1128 0.1185 0.1228	0.380 0.385 0.390 0.393 0.395 0.401	0.0867 0.0878 0.0890 0.0898 0.0903 0.0917
	Drake Mallard Crow Starling Redwing Flamingo	795 000 795 000 715 500 715 500 715 500 666 600	26 30 54 26 30 54	2 2 3 2 2 3	0.1749 0.1628 0.1151 0.1659 0.1544 0.1111	7 19 7 7 19 7	0.1360 0.0977 0.1151 0.1290 0.0926 0.1111	1.108 1.140 1.036 1.051 1.081 1.000	500 000 500 000 450 000 450 000 450 000 419 000	31 200 38 400 26 300 28 100 34 600 24 500	5770 6517 4859 5193 5865 4527	0.0375 0.0393 0.0349 0.0355 0.0372 0.0337	900 910 830 840 840 800	0.117 0.117 0.131 0.131 0.131 0.140	0.117 0.117 0.131 0.131 0.131 0.131 0.140	0.117 0.117 0.131 0.131 0.131 0.131 0.141	0.117 0.117 0.132 0.131 0.131 0.131 0.141	0.1288 0.1288 0.1442 0.1442 0.1442 0.1442 0.1541	0.1288 0.1288 0.1452 0.1442 0.1442 0.1442 0.1571	0.1472 0.1442 0.1442	0.1482 0.1442	0.399 0.393 0.407 0.405 0.399 0.412	0.0912 0.0904 0.0932 0.0928 0.0920 0.0943
	Rook Grosbeak Egret Peacock Squab Dove	636 000 636 000 636 000 605 000 605 000 556 500	54 26 30 54 26 26	3 2 3 2 2	0.1085 0.1564 0.1456 0.1059 0.1525 0.1463	7 7 19 7 7 7	0.1085 0.1216 0.0874 0.1059 0.1186 0.1138	0.977 0.990 1.019 0.953 0.966 0.927	400 000 400 000 380 500 380 500 350 000	23 600 25 000 31 500 22 500 24 100 22 400	4 319 4 616 5 213 4 109 4 391 4 039	0.0329 0.0335 0.0351 0.0321 0.0327 0.0313	770 780 780 750 760 730	0.147 0.147 0.147 0.154 0.154 0.154	0.147 0.147 0.147 0.155 0.154 0.168	0.148 0.147 0.147 0.155 0.154 0.168	0.148 0.147 0.147 0.155 0.154 0.168	0.1618 0.1618 0.1618 0.1695 0.1700 0.1849	0.1638 0.1618 0.1618 0.1715 0.1720 0.1859	0.1618	0.1618 0.1618 0.1775 0.1720	0.414 0.412 0.406 0.417 0.415 0.420	0.0950 0.0946 0.0937 0.0957 0.0953 0.0965
Smaller	Eagle Hawk Hen Ibis Lark	556 500 477 000 477 000 397 500 397 500	30 26 30 26 30	2 2 2 2 2	0.1362 0.1355 0.1261 0.1236 0.1151	7 7 7 7 7	0.1362 0.1054 0.1261 0.0961 0.1151	0.953 0.858 0.883 0.783 0.806	350 000 300 000 300 000 250 000 250 000	27 200 19 430 23 300 16 190 19 980	4 588 3 462 3 933 2 885 3 277	0.0328 0.0290 0.0304 0.0265 0.0278	730 670 670 590 600	0.168 0.196 0.196 0.235 0.235	0.168 0.196 0.196 S	0.168 0.196 0.196 ame as d	0.168 0.196 0.196 c	0.1849 0.216 0.216 0.259 0.259	0.1859 S	0.1859 ame as d		0.415 0.430 0.424 0.441 0.435	0.0957 0.0988 0.0980 0.1015 0.1006
Ļ	Linnet Oriole Ostrich Piper Partridge	336 400 336 400 300 000 300 000 266 800	26 30 26 30 26	2 2 2 2 2	0.1138 0.1059 0.1074 0.1000 0.1013	7 7 7 7 7	0.0855 0.1059 0.0835 0.1000 0.0788	0.721 0.741 0.680 0.700 0.642	4/0 4/0 188 700 188 700 3/0	14 050 17 040 12 650 15 430 11 250	2 442 2 774 2 178 2 473 1 936	0.0244 0.0255 0.0230 0.0241 0.0217	530 530 490 500 460	0.278 0.278 0.311 0.311 0.350				0.306 0.306 0.342 0.342 0.385				0.451 0.445 0.458 0.462 0.465	0.1039 0.1032 0.1057 0.1049 0.1074

*Based on copper 97%, aluminum 61% conductivity

For conductor at 75°C, air at 25°C, wind 1.4 miles per hour (2 ft/sec), frequency = 60 Hz, ‡"Current Approx. 75% Capacity" is 75% of the "Approx. Current Carrying Capacity in Amps" and is appro ately the current which will produce 50°C conductor temp. (25°C rise) with 25°C air ter wind 1.4 miles per hour

0:	100%	÷	1.72 ×10-8	n.m)	10.37	cmil/f+	

Cu 1.77 ×10-8 R.m 2.83 ×10-8 A.m

AL

Other conductor types include the all-aluminum conductor (AAC), allaluminum-alloy conductor (AAAC), aluminum conductor alloy-reinforced (ACAR), and aluminum-clad steel conductor (Alumoweld). There is also a conductor known as "expanded ACSR," which has a filler such as fiber or paper between the aluminum and steel strands. The filler increases the conductor diameter, which reduces the electric field at the conductor surface, to control corona.

EHV lines often have more than one conductor per phase; these conductors are called a bundle. The 765-kV line in Figure 5.2 has four conductors per phase, and the 345-kV double-circuit line in Figure 5.3 has two conductors per phase. Bundle conductors have a lower electric field strength at the conductor surfaces, thereby controlling corona. They also have a smaller series reactance.

ECE 3600

Transmission Line notes p1

NOMINAL VOLTAGE		PHA	SE CONDUCTORS	3	
	NUMBER OF CONDUCTORS PER BUNDLE	ALUMINUM CROSS- SECTION	BUNDLE SPACING	MINIMUM CL 0.3048.	-
		AREA PER CONDUCTOR (ACSR)		PHASE-TO- PHASE	PHASE-TO- GROUND
kV		kcmil	cm	m	m
96 hV 69	1				
138	1	300-700	-	4 to 5	
230	1	400-1000	~~	6 to 9	
345	1	2000-2500	-	6 to 9	7.6 to 11
345	2	800-2200	45.7 (18")	6 to 9	7.6 to 11
500	2	2000-2500	45.7	9 to 11	9 to 14
500	3	900-1500	45.7	9 to 11	9 to 14,
765	4	900-1300	45.7	13.7 (45')	12.2 (40')
				3.28	1 ft= lm

	MINAL TAGE	SUSPENSION IN	SULATOR STRING	(light	SHIELD WIRE ning protect	
		NUMBER OF STRINGS PER PHASE	NUMBER OF STANDARD INSULATOR DISCS PER SUSPENSION STRING	TYPE	NUMBER	DIAMETER
	kV					cm
	69	1	-4 to 6	Steel	0,1 or 2	_
1	38	1	8 to 11	Steel	0,1 or 2	-
. 2	:30	1	12 to 21	Steel or ACSR	1 or 2	1.1 to 1.5
3	345	1	18 to 21	Alumoweld	2	0.87 to 1.5
. 3	45	1 and 2	18 to 21	Alumoweld	2	0.87 to 1.5
5	00	2 and 4	24 to 27	Alumoweld	2	0.98 to 1.5
5	00	2 and 4	24 to 27	Alumoweld	2	0.98 to 1.5
7	65	2 and 4	30 to 35 🦷	Alumoweld	2	O.98

 Table 5.1
 Typical transmission-line characteristics [1, 2]

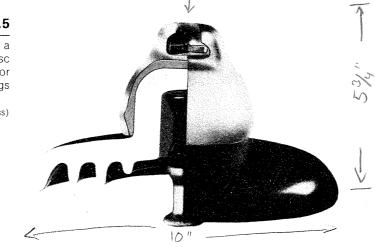


Figure 5.5

Cut-away view of a standard insulator disc for suspension insulator strings

(Courtesy of Ohio Brass)

Table 5.2

Comparison of SI and English units for calculating conductor resistance

QUANTITY	SYMBOL	SI UNITS	ENGLISH UNITS
Resistivity	ρ	Ωm	Ω-cmil/ft ft
Length Cross-sectional	ć	m	
area	A	m²	cmil
dc resistance	$R_{dc} = \frac{\mu t}{A}$	Ω	Ω

Resistivity depends on the conductor metal. Annealed copper is the international standard for measuring resistivity ρ (or conductivity σ , where $\sigma = 1/\rho$). Resistivity of conductor metals is listed in Table 5.3. As shown, hard-drawn aluminum, which has 61% of the conductivity of the international standard, has a resistivity at 20°C of 17.00 Ω -cmil/ft or 2.83 × 10⁻⁸ Ω m.

Table 5.3

% Conductivity, resistivity, and temperature constant of conductor metals

j.	%	ρ_{20}	ЪС	Т
MATERIAL	CONDUCTIVITY	RESISTIVITY AT 20°C		TEMPERATURE CONSTANT
		Ω m × 10 ⁻⁸	Ω -cmil/ft	°C
Copper:				
Annealed	100%	1.72	10.37	234.5
Hard-drawn	97.3%	1.77	10.66	241.5
Aluminum				
Hard-drawn	61%	2.83	17.00	228.1
Brass	20-27%	6.4-8.4	38–51	480
Bronze	9–13%	13-18	78–108	1980
Iron	17.2%	10	60	180
Silver	108%	1.59	9.6	243
Sodium	40%	4.3	26	207
Steel	2 to 14%	12 to 88	72–530	180–980

Conductor resistance depends on the following factors:

- **1.** Spiraling $+ 1 2^{\circ}/_{\circ}$ resistance **2.** Temperature
- **2.** Temperature

 $\rho_{T_2} = \rho_{2b} \left(\frac{T_2 + T_1}{20^{\circ}C + T} \right)$

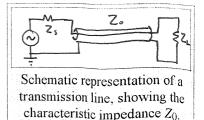
3. Frequency ("skin effect") $\sim + 3^{\circ}/_{b}$

4. Current magnitude-magnetic conductors

Characteristic impedance

From Wikipedia, the free encyclopedia

The **characteristic impedance** or **surge impedance** of a uniform transmission line, usually written Z_0 , is the ratio of the amplitudes of a *single* pair of voltage and current waves propagating along the line in the absence of reflections. The SI unit of characteristic impedance is the ohm. The characteristic impedance of a lossless transmission line is purely real, that is, there is no imaginary component $(Z_0 = |Z_0| + j0)$. Characteristic impedance appears like a resistance in this case, such that power generated by a source on one end of an infinitely long lossless



transmission line is dissipated *through* the line but is not dissipated *in* the line itself. A transmission line of finite length (lossless or lossy) that is terminated at one end with a resistor equal to the characteristic impedance ($Z_L = Z_0$) appears like an infinitely long transmission line to the source.

ECE 3600 Transmission Line notes p3

ECE 3600 Transmission Line notes p4 Transmission line model

Applying the transmission line model based on the telegrapher's equations, the general expression for the characteristic impedance of a transmission line is:

$$Z_0 = \sqrt{\frac{R + j\omega L}{G + j\omega C}}$$

where

R is the resistance per unit length,

L is the inductance per unit length,

G is the conductance of the dielectric per unit length,

C is the capacitance per unit length,

j is the imaginary unit, and

 ω is the angular frequency.

The voltage and current phasors on the line are related by the characteristic impedance as:

V^+						V^{-}	-
	 	2			niniwedi A		-
I^+						I^{-}	

where the superscripts + and - represent forward- and backward-traveling waves, respectively.

Lossless line

For a lossless line, R and G are Zero so the equation for characteristic impedance reduces to

$$Z_0 = \sqrt{\frac{L}{C}}$$

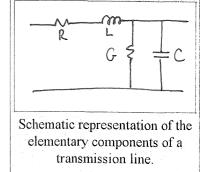
Surge Impedance Loading

In electric power transmission, the characteristic impedance of a transmission line is expressed in terms of the **surge impedance loading (SIL**), or natural loading, being the MW loading at which reactive power is neither produced nor absorbed:

$$SIL = \frac{(V_{L-L})^{2}}{Z_{0}} = 3 \frac{V_{LN}}{Z_{0}} = 3 \frac{V_{R}^{2}}{Z_{0}}$$

in which $V_{\rm L} - L$ is the line-to-line voltage in volts.

Loaded below its SIL, a line supplies lagging reactive power to the system, tending to raise system voltages. Above it, the line absorbs reactive power, tending to depress the voltage. The Ferranti effect describes the voltage gain towards the remote end of a very lightly loaded (or open ended) transmission line. Underground cables normally have a very low characteristic impedance, resulting in an SIL that is typically in excess of the thermal limit of the cable. Hence a cable is almost always a source of lagging reactive power.



ECE 3600 Transmission Line Typical Values

	at 60 H:	z [2, 6]	10-6 Siemens		
Nominal Voltage	$R(\Omega/km)$	$\omega L(\Omega/km)$	$\omega C(\mu \overline{\mho}/km)$		
230 kV	0.055	0.489	3.373		
345 kV	0.037	0.376	4.518		
500 kV	0.029	0.326	5.220		
765 kV	0.013	0.339	4.988		

	Table 4-1	
Trans	smission Line Parameters with Bundled Conductors (except at 23	0 kV)
	at 60 Hz [2 6]	

Table 4-2	
Surge Impedance and Three-Phase Surge Impedance Loading [2, 6	1

Nominal Voltage	$Z_c(\Omega)$	SIL (MW)	Lov ISIL IL(A)
230 kV	375	140 MW	350p
345 kV	280	425 MW	710A
500 kV	250	1000 MW	1160A
765 kV	255	2300 MW	1740A

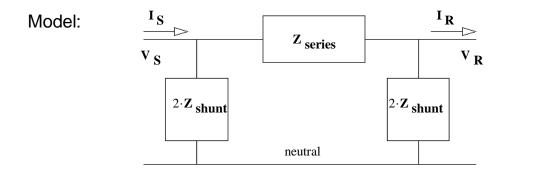
	Table 4-3Loadability of Transmission Lines [6]						
	Line Length (km)	Limiting Factor	Multiple of SIL				
short	0 - 80 km 50 mi	Thermal	> 3				
medium	80 - 240 km	5% Voltage Drop	1.5 - 3				
Long	240 - 480 Km	Stability	1.0 – 1.5				

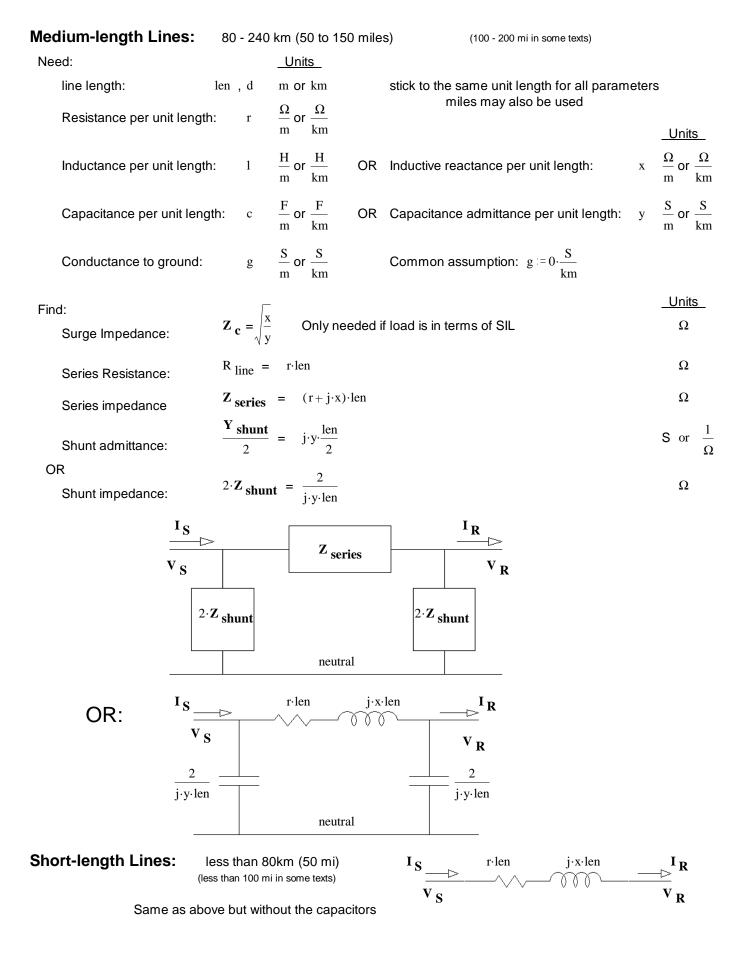
Typical values for transmission lines taken from: *First Course on Power Systems* by Ned Mohan

ECE 3600 Lumped-Parameter Transmission Line Models

ECE 360	0 Lur	mped-Paramet	ter Transmission Line Models	С
Long-length Lines:	over 240 kn	n (150 miles)	(over 200 mi in some texts)	
Need:		Units		
line length:	line length: len , d		stick to the same unit length for all parame	eters
Resistance per unit length: r		$rac{\Omega}{m}$ or $rac{\Omega}{km}$	miles may also be used	Units
Inductance per unit length	n: 1	$rac{H}{m}$ or $rac{H}{km}$ OR	Inductive reactance per unit length:	x $\frac{\Omega}{m}$ or $\frac{\Omega}{km}$
Capacitance per unit leng	ıth: c	$rac{F}{m}$ or $rac{F}{km}$ OR	Capacitance admittance per unit length:	y $\frac{S}{m}$ or $\frac{S}{km}$
Conductance to ground:	g	$\frac{S}{m}$ or $\frac{S}{km}$	Common assumption: $g := 0 \cdot \frac{S}{km}$	S := siemens
Find:				Units
Surge impedance:	Z _c	$f = \sqrt{\frac{\mathbf{j} \cdot \mathbf{x} + \mathbf{r}}{\mathbf{j} \cdot \mathbf{y} + \mathbf{g}}}$		<u>- 01iits</u> Ω
Propagation constant:	γ	$= \sqrt{(j \cdot x + r) \cdot (j \cdot y + r)}$	g)	$\frac{1}{m}$ or $\frac{1}{km}$
			If your calculator doesn't have hyperbol	ic trig functions
Series impedance	Z _{series}	$= \mathbf{Z}_{\mathbf{c}} \cdot \sinh(\gamma \cdot \operatorname{len})$	$= \mathbf{Z} \cdot \frac{\mathrm{e}^{\gamma \mathrm{len}} - \mathrm{e}^{-\gamma \mathrm{len}}}{2}$	Ω
Shunt admittance: OR	$\frac{\mathbf{Y}_{\mathbf{shunt}}}{2}$	$= \frac{1}{\mathbf{Z}_{\mathbf{c}}} \cdot \tanh\left(\gamma \frac{\mathrm{len}}{2}\right)$	$= \frac{1}{\mathbf{Z}_{\mathbf{c}}} \cdot \frac{\mathbf{e}^{\frac{\gamma \cdot \ln}{2}} - \mathbf{e}^{-\gamma \cdot \frac{\ln}{2}}}{\mathbf{e}^{\frac{\gamma \cdot \ln}{2}} + \mathbf{e}^{-\gamma \cdot \frac{\ln}{2}}} = \frac{1}{\mathbf{Z}_{\mathbf{c}}} \cdot \frac{\sqrt{\mathbf{e}^{\gamma \cdot \ln}} - \gamma}{\sqrt{\mathbf{e}^{\gamma \cdot \ln}} + \gamma}$	$rac{\sqrt{e^{-(\gamma \cdot len)}}}{\sqrt{e^{-(\gamma \cdot len)}}}$ Ω
Shunt impedance:	$2 \cdot \mathbf{Z}_{shunt}$	$= \frac{\mathbf{Z}_{\mathbf{c}}}{\tanh\left(\gamma \frac{\mathrm{len}}{2}\right)}$		S or $\frac{1}{\Omega}$
		\ <i>I</i>	If your calculator can't handle complex	evnonents

If your calculator can't handle complex exponents $e^{(a+b\cdot j)} = e^{a} \cdot e^{b\cdot j} = e^{a} / b \text{ (in radians)}$





neutral

ECE 3600 Transmission Line Examples

Ex1. A 500 kV transmission line is 500 km long and has the line parameters shown below. Use the long-length model to find V_S and I_S if the line is loaded to 900 MVA and $|V_{RLL}|$ is 490 kV. Assume the phase angle of V_R is 0° and assume load pf = 1.

$\mathbf{v}_{\mathbf{R}}$ is 0° and assume load \mathbf{r}		37
len := 500·km	$\mathbf{V}_{\mathbf{RLL}} = 490 \cdot \mathbf{kV} \qquad \mathbf{V}_{\mathbf{R}} =$	$\frac{\mathbf{V}_{\text{RLL}}}{\sqrt{3}} \qquad \mathbf{S}_{1\phi} = \frac{900 \cdot \text{MVA}}{3}$
$r := 0.029 \cdot \frac{\Omega}{km}$ $x := 0.326 \cdot \frac{\Omega}{km}$	Assume: $g := 0 \cdot \frac{S}{km}$	Note: These are typical values
$x = 0.326 \cdot \frac{m}{km}$	y := 5.220·10	km
Long-length line model:	li v L v	
Surge Impedance:	$\mathbf{Z}_{\mathbf{c}} := \sqrt{\frac{\mathbf{j} \cdot \mathbf{x} + \mathbf{r}}{\mathbf{j} \cdot \mathbf{y} + \mathbf{g}}}$	$\mathbf{Z}_{\mathbf{c}} = 250.151 - 11.104 \mathbf{j} \cdot \mathbf{\Omega}$
Propagation constant:	$\gamma := \sqrt{(j \cdot x + r) \cdot (j \cdot y + g)}$	$\gamma = 5.797 \cdot 10^{-5} + 1.306 \cdot 10^{-3} j \cdot \frac{1}{km}$
Series impedance:	$\mathbf{Z}_{series} := \mathbf{Z}_{c} \cdot \sinh(\gamma \operatorname{len})$	$Z_{series} = 12.508 + 151.772 j$ ·Ω
Shunt admittance: (Not used in my solution)	$\mathbf{Y}_{\mathbf{shunt}} := \frac{2}{\mathbf{Z}_{\mathbf{c}}} \cdot \tanh\left(\gamma \cdot \frac{\mathrm{len}}{2}\right)$	$\frac{\mathbf{Y}_{shunt}}{2} = 4.49 \cdot 10^{-6} + 1.353 \cdot 10^{-3} \mathbf{j} \qquad \mathbf{\cdot}\mathbf{S}$
Shunt impedance:	$\mathbf{Z}_{shunt} := \frac{\mathbf{Z}_{c}}{2 \cdot \tanh\left(\gamma \cdot \frac{\operatorname{len}}{2}\right)}$	$2 \cdot \mathbf{Z}_{shunt} = 2.451 - 738.924 j \cdot \Omega$
Solve circuit:	$\mathbf{I}_{\mathbf{R}} := \frac{\mathbf{S}_{1\phi}}{ \mathbf{V}_{\mathbf{R}} }$	from the profiload other information)
	$\mathbf{Z}_{\text{series}}$ $\mathbf{I}_{\mathbf{R}} = 1060.4$	$\mathbf{V}_{\mathbf{R}} = 282.902 \cdot kV$
$2 \cdot \mathbf{Z}_{shunt}$	$2 \cdot \mathbf{Z}_{shunt} \Big _{\mathbb{V}}$	
	neutral	$\mathbf{I}_{\mathbf{Zshunt}} := \frac{\mathbf{V}_{\mathbf{R}}}{2 \cdot \mathbf{Z}_{\mathbf{shunt}}}$
		$I_{Zshunt} = 1.27 + 382.852j$ ·A
$\mathbf{I}_{\mathbf{L}} := \mathbf{I}_{\mathbf{Zshunt}} + \mathbf{I}_{\mathbf{R}}$	$I_L = 1.062 \cdot 10^3 + 382.852j$ ·A	
$\mathbf{V}_{\mathbf{S}} := \mathbf{V}_{\mathbf{R}} + \mathbf{I}_{\mathbf{L}} \cdot \mathbf{Z}_{\mathbf{series}}$	$\mathbf{V}_{\mathbf{S}} = 2.381 \cdot 10^5 + 1.659 \cdot 10^5 \mathbf{j} $ $\cdot \mathbf{V}$	$ \mathbf{V}_{\mathbf{S}} = 290.192 \cdot k\mathbf{V} \arg(\mathbf{V}_{\mathbf{S}}) = 34.874 \cdot \deg$
$\mathbf{I}_{\mathbf{ZshuntS}} := \frac{\mathbf{V}_{\mathbf{S}}}{2 \cdot \mathbf{Z}_{\mathbf{shunt}}}$	$I_{ZshuntS} = -223.48 + 322.934j$ ·A	$\left \sqrt{3} \cdot \mathbf{V}_{\mathbf{S}}\right = 502.628 \cdot \mathbf{kV}$
IS := IZshuntS + IL	I _S = 838.23 + 705.786j •A	$ \mathbf{I}_{\mathbf{S}} = 1096 \cdot \mathbf{A}$ $\arg(\mathbf{I}_{\mathbf{S}}) = 40.097 \cdot \deg$
5 ZSHUIIUS L	1S = 0.0000000000000000000000000000000000	$ \mathbf{IS} = 1000 \text{ fr} \qquad \text{arg}(\mathbf{IS}) = 1000 \text{ fr} \text{ arg}$

ECE 3600 Transmission Line notes p8

b

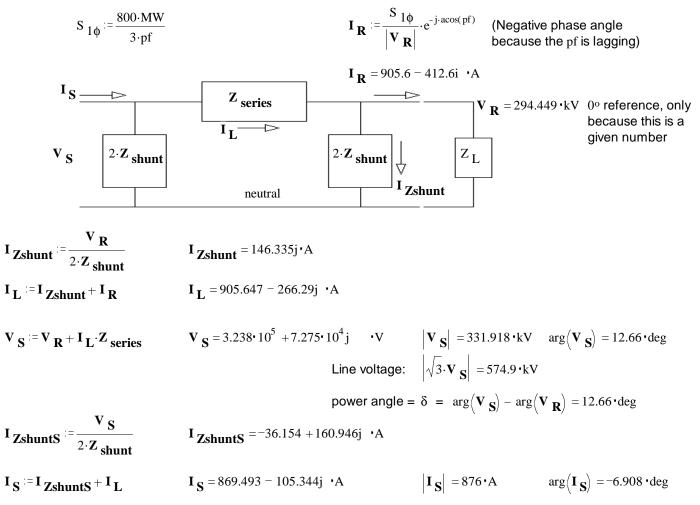
Ex 2. A 345 kV transmission line is 220 km long and has the line parameters shown below. Find V_s and I_s if the line is loaded to 800MVA with pf = 91% lagging. $|V_{RLL}|$ is 510 kV. pf := 0.91

len := 220 kmV
RLL := 510 kVV
R:=
$$\frac{V}{\sqrt{3}}$$
Assume the phase angle
of V
R is 0° if V
R is givenr := 0.037 $\cdot \frac{\Omega}{km}$ Assume:g := $0 \cdot \frac{S}{km}$ Note: These are typical values
for a 345 kV transmission linex := 0.376 $\cdot \frac{\Omega}{km}$ y := $4.518 \cdot 10^{-6} \cdot \frac{S}{km}$ Note: These are typical values
for a 345 kV transmission line

Medium-length line model:

Series impedance: $\mathbf{Z}_{series} := (\mathbf{r} + \mathbf{j} \cdot \mathbf{x}) \cdot \text{len}$ $\mathbf{Z}_{series} = 8.14 + 82.72\mathbf{j} \cdot \Omega$ Shunt admittance: $\mathbf{Y}_{shunt} := \mathbf{j} \cdot \mathbf{y} \cdot \text{len}$ $\frac{\mathbf{Y}_{shunt}}{2} = 496.98\mathbf{j} \cdot \mu S$ Not used in my solution $\mathbf{Z}_{shunt} := \frac{1}{\mathbf{j} \cdot \mathbf{y} \cdot \text{len}}$ $2 \cdot \mathbf{Z}_{shunt} = -2.012 \cdot 10^3 \mathbf{j} \cdot \Omega$

Solve circuit:

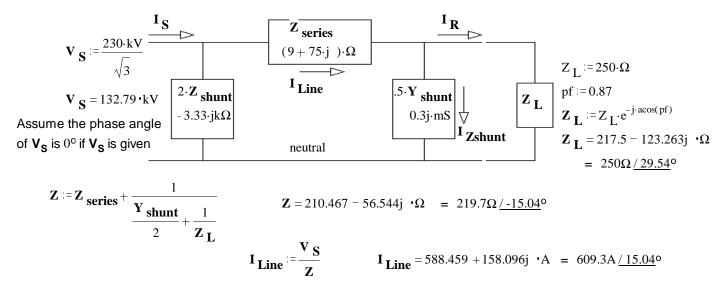


ECE 3600 Transmission Line notes p9

Ex3. A 230 kV transmission line has the following length and line parameters.

•			
m $r := 0.06 \cdot \frac{\Omega}{km}$	$\mathbf{x} := 0.5 \cdot \frac{\Omega}{\mathbf{km}}$	$g := 0 \cdot \frac{S}{km} \qquad \qquad y := 4 \cdot 10^{-6} \cdot \frac{1}{km}$	S cm
Series impedance:	$\mathbf{Z}_{series} := (r + j \cdot x) \cdot len$	$\mathbf{Z}_{series} = 9 + 75j \cdot \Omega$	
Shunt admittance:	$\mathbf{Y}_{\mathbf{shunt}} := \mathbf{j} \cdot \mathbf{y} \cdot \mathbf{len}$	$\frac{\mathbf{Y}_{\mathbf{shunt}}}{2} = 0.3 \mathbf{j} \cdot \mathbf{mS}$	
Shunt impedance:	$\mathbf{Z}_{\mathbf{shunt}} := \frac{1}{j \cdot y \cdot len}$	$2 \cdot \mathbf{Z}_{\text{shunt}} = -3.333 \mathbf{j} \cdot \mathbf{k} \mathbf{\Omega}$	2
	km Series impedance: Shunt admittance:	kmkmSeries impedance: $\mathbf{Z}_{series} := (r + j \cdot x) \cdot len$ Shunt admittance: $\mathbf{Y}_{shunt} := j \cdot y \cdot len$	Series impedance: $Z_{series} := (r + j \cdot x) \cdot len$ $Z_{series} = 9 + 75j \cdot \Omega$ Shunt admittance: $Y_{shunt} := j \cdot y \cdot len$ $\frac{Y_{shunt}}{2} = 0.3j \cdot mS$

a) The load is 250Ω with a power factor of 0.87, leading. Find the line current, \mathbf{I}_{Line} .



b) Find the load line voltage.

I Line \mathbb{Z} series = -6.561 + 45.557 j·kV

$$\mathbf{V}_{\mathbf{R}} := \mathbf{V}_{\mathbf{S}} - \mathbf{I}_{\mathbf{Line}} \cdot \mathbf{Z}_{\mathbf{series}} \qquad \mathbf{V}_{\mathbf{R}} = 139.352 - 45.557 \mathbf{j} \cdot \mathbf{kV} = 146.6 \mathbf{kV} \underline{/-18.1}^{\circ} \mathbf{kV}$$

Receiving line voltage = $\left| \sqrt{3} \cdot \mathbf{V}_{\mathbf{R}} \right| = 253.9 \cdot \mathbf{kV}$

Notice that $|V_R|$ is bigger than $|V_S|$, this can happen when the receiving-end power factor is leading.

- c) What is the "power angle" (δ)? $\delta = -\arg(\mathbf{V}_{\mathbf{R}}) = 18.104 \cdot \text{deg}$
- d) How much power is delivered to the load?

$$\mathbf{I}_{\mathbf{R}} := \frac{|\mathbf{V}_{\mathbf{R}}|}{|\mathbf{Z}_{\mathbf{L}}|} \qquad \mathbf{P}_{\mathbf{L}} = 3 \cdot |\mathbf{V}_{\mathbf{R}}| \cdot \mathbf{I}_{\mathbf{R}} \cdot \mathbf{pf} = 224.4 \cdot \mathbf{MW}$$

Power estimate for the same
$$|\mathbf{V}_{\mathbf{R}}|$$
 and
 $|\mathbf{V}_{\mathbf{S}}|$, but neglecting the line resistance:
 $\simeq 3 \cdot \frac{|\mathbf{V}_{\mathbf{S}}| \cdot |\mathbf{V}_{\mathbf{R}}| \cdot \sin(18.1 \cdot \deg)}{|\mathbf{Z}_{\text{series}}|} = 240 \cdot \text{MW}$
e) Express this loading in terms of SIL
Surge Impedance:
 $\mathbf{Z}_{\mathbf{c}} := \sqrt{\frac{x}{y}}$
 $\mathbf{Z}_{\mathbf{c}} = 353.6 \cdot \Omega$
 $\frac{\mathbf{Z}_{\mathbf{c}}}{\mathbf{Z}_{\mathbf{L}}} = 1.41$

 $\frac{-c}{Z_L} = 1.414$ SIL load Not asked for in this class

ECE 3600 Transmission Line notes p10

Answer the following questions in your textbook, starting on p.488.

- 9-3 What factors influence the inductance of a transmission line?
- 9-4 Suppose that there are two transmission lines using a single conductor per phase, and that the conductors in the two transniission lines are identical (same material and same diameter). If one transmission line is rated at 345 kV and the other one is rated at 238 kV. which transmission line is likely to have the highest inductance? Why?
- 9-5 Suppose someone asked you to evaluate a proposal for an underwater power cable between North Carolina and the Bahamas. What would you say about the probability of success of this proposal? Why?
- 9-6 What line lengths are generally considered to be short transmission lines? Medium-length transmission lines? Long transmission lines?
- 9-9 What happens to the receiving end voltage as the load on a transmission line is increased if the load has a lagging power factor? Sketch a phasor diagram showing the resulting behavior.
- 9-11 What happens to the receiving end voltage as the load on a transmission line is increased if the load has a leading power factor? Sketch a phasor diagram showing the resulting behavior.
- 9-12 What is the significance of the angle δ between V_S and V_R in a transmission line?

Problems

1. A 230 kV transmission line is 70 km long and has line parameters shown in Table 4.1 (handout). $|V_{SLL}|$ is 230 kV. Assume the phase angle of V_S is 0° and that the source sees a pf = 0.8, lagging.

From Table 4.1: $r := 0.055 \ \Omega/km$ $x := 0.489 \ \Omega/km$ $y := 3.373 \cdot 10^{-6} \ S/km$ Assume: $g := 0 \ S/km$

- a) Use the short-length model to find I_{R} and V_{R} if the source is loaded to 170 MVA (as calculated for the line).
- b) What is the angle δ ?
- c) What is the power factor of the load?

Solve the following problems in your textbook, starting on p.489.

2. 9-11 A 138 kV, 200 MVA, 60 Hz, three-phase, power transmission line is 100 km long, and has the following

characteristics:

 $r = 0.103 \ \Omega/km$ $x = 0.525 \ \Omega/km$ $y = 3.3 \cdot 10^{-6} \ S/km$

- a) What is per phase series impedance and shunt admittance of this transmission line?
- b) Should it be modeled as a short, medium, or long transmission line?
- d) Sketch the phasor diagram of this transmission line when the line is supplying rated voltage and apparent power at a 0.90 power factor lagging.
- e) Calculate the sending-end voltage if the line is supplying rated voltage and apparent power at 0.90 PF lagging.
- f) What is the voltage regulation of the transmission line for the conditions in (e)?
- g) What is the efficiency of the transmission line for the conditions in (e)?
- h) 9-13 What is the "power angle", δ ?
 Original problem statment: If the series resistance and shunt admittance of the transmission line in Problem 9-11 are not ignored, what would the value of the angle δ be at rated conditions and 0.90 PF lagging?
- 3. 9-12 If the series resistance and shunt admittance of the transmission line in Problem 9-11 are ignored, what would the value of the angle δ be at rated conditions and 0.90 PF lagging?
- 4. A 765 kV transmission line is 200 km long and has line parameters shown in Table 4.1, p.4-10. Use the medium-length model to find V_S and I_S if the line is loaded to 1800 MVA and $|V_{RLL}|$ is 770 kV. Assume the phase angle of V_R is 0° and assume load pf = 1.

Table 4.1: $r = 0.013 \ \Omega/km$ $x = 0.339 \ \Omega/km$ $y = 4.988 \cdot 10^{-6} \ S/km$

Answers

