

Figure 5.1
Typical ACSR conductor

54/7 Cardinal

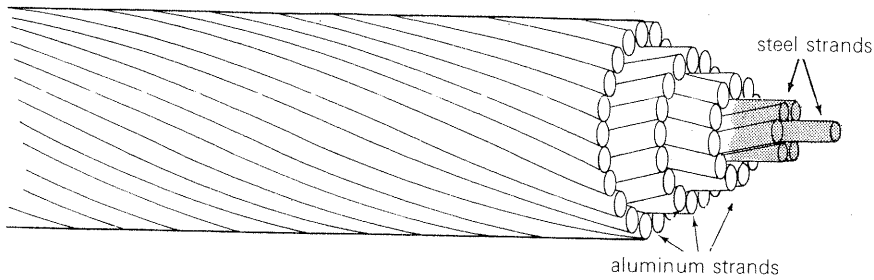


Table A.4 Characteristics of aluminum cable, steel, reinforced (Aluminum Company of America)

Code Word	Circular Mils Aluminum	Aluminum		Steel		Outside Diameter (Inches)	Copper Equivalent* Circular Mils or A.W.G.	Ultimate Strength (Pounds)	Weight (Pounds per Mile)	Geometric Mean Radius at 60 Hz (Feet)	Approx. Current Carrying Capacity† (Amps)	Resistance								X_L Inductive Reactance (Ohms per Conductor per Mile at 1 Ft Spacing All Currents)	X_C Shunt Capacitive Reactance (Megohms per Conductor per Mile at 1 Ft Spacing)	
		Strand Diameter (Inches)	Strand Diameter (Inches)	R_a Resistance (Ohms per Conductor per Mile)																		
				25°C (77°F) Small Currents								50°C (122°F) Current Approx. 75% Capacity‡										
				dc	25 Hz							50 Hz	60 Hz	dc	25 Hz	50 Hz	60 Hz					
Joree Thrasher Kiwi Bluebird Chukar	2515 000	76	...	0.1819	19	0.0849	1.880	61 700	10 777	0.0621	1 380	0.0587	0.0588	0.0590	0.0591	0.0646	0.0656	0.0675	0.0684	0.0450	0.337	0.0755

*Based on copper 97%, aluminum 61% conductivity.
 †For conductor at 75°C, air at 25°C, wind 1.4 miles per hour (2 ft/sec), frequency = 60 Hz.
 ‡"Current Approx. 75% Capacity" is 75% of the "Approx. Current Carrying Capacity in Amps" and is approximately the current which will produce 50°C conductor temp. (25°C rise) with 25°C air temp., wind 1.4 miles per hour.

$\rho = 100\% = 1.72 \times 10^{-8} \Omega \cdot m$, $10.37 \text{ cmil}/ft$ $Cu \ 1.77 \times 10^{-8} \Omega \cdot m$
 $Al \ 2.83 \times 10^{-8} \Omega \cdot m$

Other conductor types include the all-aluminum conductor (AAC), all-aluminum-alloy conductor (AAAC), aluminum conductor alloy-reinforced (ACAR), and aluminum-clad steel conductor (Alumoweld). There is also a conductor known as "expanded ACSR," which has a filler such as fiber or paper between the aluminum and steel strands. The filler increases the conductor diameter, which reduces the electric field at the conductor surface, to control corona.

EHV lines often have more than one conductor per phase; these conductors are called a *bundle*. The 765-kV line in Figure 5.2 has four conductors per phase, and the 345-kV double-circuit line in Figure 5.3 has two conductors per phase. Bundle conductors have a lower electric field strength at the conductor surfaces, thereby controlling corona. They also have a smaller series reactance.

NOMINAL VOLTAGE	PHASE CONDUCTORS			
	NUMBER OF CONDUCTORS PER BUNDLE	ALUMINUM CROSS-SECTION AREA PER CONDUCTOR (ACSR)	BUNDLE SPACING	MINIMUM CLEARANCES <i>0.3048 m = 1 ft</i>
kV		kcmil	cm	PHASE-TO-PHASE m PHASE-TO-GROUND m
<i>46 kV</i> 69	1	-	-	-
115 kV 138	1	300-700	-	4 to 5
230	1	400-1000	-	6 to 9
345	1	2000-2500	-	6 to 9 7.6 to 11
345	2	800-2200	45.7 (<i>18"</i>)	6 to 9 7.6 to 11
500	2	2000-2500	45.7	9 to 11 9 to 14
500	3	900-1500	45.7	9 to 11 9 to 14
765	4	900-1300	45.7	13.7 (<i>45'</i>) 12.2 (<i>40'</i>)

3.281 ft = 1 m

NOMINAL VOLTAGE	SUSPENSION INSULATOR STRING		SHIELD WIRES <i>(lightning protection)</i>		
	NUMBER OF STRINGS PER PHASE	NUMBER OF STANDARD INSULATOR DISCS PER SUSPENSION STRING	TYPE	NUMBER	DIAMETER
kV					cm
69	1	4 to 6	Steel	0,1 or 2	-
138	1	8 to 11	Steel	0,1 or 2	-
230	1	12 to 21	Steel or ACSR	1 or 2	1.1 to 1.5
345	1	18 to 21	Alumoweld	2	0.87 to 1.5
345	1 and 2	18 to 21	Alumoweld	2	0.87 to 1.5
500	2 and 4	24 to 27	Alumoweld	2	0.98 to 1.5
500	2 and 4	24 to 27	Alumoweld	2	0.98 to 1.5
765	2 and 4	30 to 35	Alumoweld	2	0.98

Table 5.1 Typical transmission-line characteristics [1,2]

Figure 5.5

Cut-away view of a standard insulator disc for suspension insulator strings

(Courtesy of Ohio Brass)

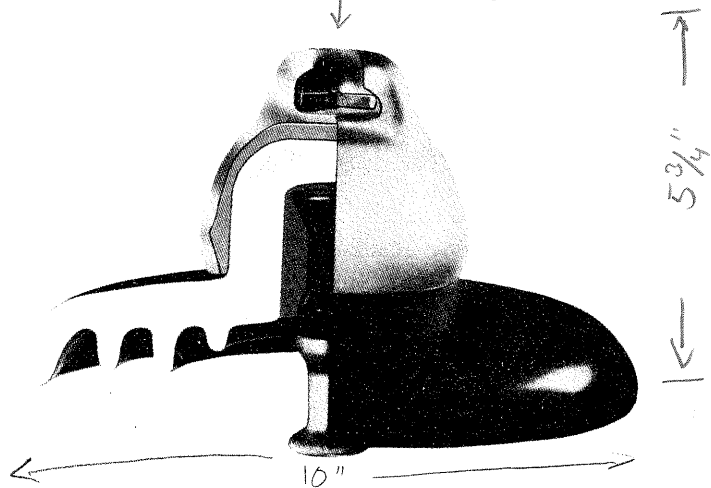


Table 5.2

Comparison of SI and English units for calculating conductor resistance

QUANTITY	SYMBOL	SI UNITS	ENGLISH UNITS
Resistivity	ρ	Ωm	$\Omega\text{-cmil/ft}$
Length	ℓ	m	ft
Cross-sectional area	A	m^2	cmil
dc resistance	$R_{dc} = \frac{\rho\ell}{A}$	Ω	Ω

Resistivity depends on the conductor metal. Annealed copper is the international standard for measuring resistivity ρ (or conductivity σ , where $\sigma = 1/\rho$). Resistivity of conductor metals is listed in Table 5.3. As shown, hard-drawn aluminum, which has 61% of the conductivity of the international standard, has a resistivity at 20°C of 17.00 $\Omega\text{-cmil/ft}$ or $2.83 \times 10^{-8} \Omega\text{m}$.

Table 5.3

% Conductivity, resistivity, and temperature constant of conductor metals

MATERIAL	% CONDUCTIVITY	$\rho_{20^\circ\text{C}}$		T
		RESISTIVITY AT 20°C		TEMPERATURE CONSTANT
		$\Omega\text{m} \times 10^{-8}$	$\Omega\text{-cmil/ft}$	°C
Copper:				
Annealed	100%	1.72	10.37	234.5
Hard-drawn	97.3%	1.77	10.66	241.5
Aluminum				
Hard-drawn	61%	2.83	17.00	228.1
Brass	20-27%	6.4-8.4	38-51	480
Bronze	9-13%	13-18	78-108	1980
Iron	17.2%	10	60	180
Silver	108%	1.59	9.6	243
Sodium	40%	4.3	26	207
Steel	2 to 14%	12 to 88	72-530	180-980

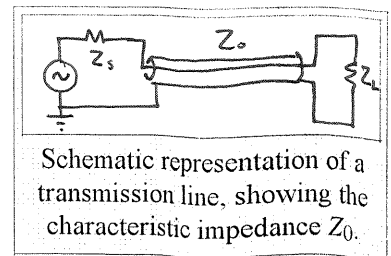
Conductor resistance depends on the following factors:

1. Spiraling + 1-2% resistance
2. Temperature $\rightarrow \rho_{T_2} = \rho_{20} \left(\frac{T_2 + T}{20^\circ\text{C} + T} \right)$
3. Frequency ("skin effect") $\sim +3\%$
4. Current magnitude—magnetic conductors

Characteristic impedance

From Wikipedia, the free encyclopedia

The **characteristic impedance** or **surge impedance** of a uniform transmission line, usually written Z_0 , is the ratio of the amplitudes of a *single* pair of voltage and current waves propagating along the line in the absence of reflections. The SI unit of characteristic impedance is the ohm. The characteristic impedance of a lossless transmission line is purely real, that is, there is no imaginary component ($Z_0 = |Z_0| + j0$). Characteristic impedance appears like a resistance in this case, such that power generated by a source on one end of an infinitely long lossless transmission line is dissipated *through* the line but is not dissipated *in* the line itself. A transmission line of finite length (lossless or lossy) that is terminated at one end with a resistor equal to the characteristic impedance ($Z_L = Z_0$) appears like an infinitely long transmission line to the source.



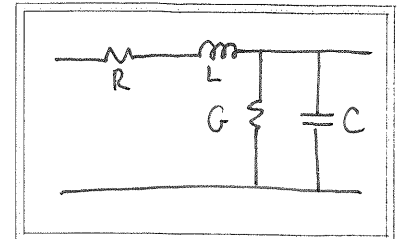
Transmission line model

Applying the transmission line model based on the telegrapher's equations, the general expression for the characteristic impedance of a transmission line is:

$$Z_0 = \sqrt{\frac{R + j\omega L}{G + j\omega C}}$$

where

R is the resistance per unit length,
 L is the inductance per unit length,
 G is the conductance of the dielectric per unit length,
 C is the capacitance per unit length,
 j is the imaginary unit, and
 ω is the angular frequency.



Schematic representation of the elementary components of a transmission line.

The voltage and current phasors on the line are related by the characteristic impedance as:

$$\frac{V^+}{I^+} = Z_0 = -\frac{V^-}{I^-}$$

where the superscripts + and - represent forward- and backward-traveling waves, respectively.

Lossless line

For a lossless line, R and G are Zero so the equation for characteristic impedance reduces to

$$Z_0 = \sqrt{\frac{L}{C}}$$

Surge Impedance Loading

In electric power transmission, the characteristic impedance of a transmission line is expressed in terms of the **surge impedance loading (SIL)**, or natural loading, being the MW loading at which reactive power is neither produced nor absorbed:

$$SIL = \frac{(V_{L-L})^2}{Z_0} = 3 \frac{V_{LN}^2}{Z_0} = 3 \frac{V_R^2}{Z_0}$$

in which V_{L-L} is the line-to-line voltage in volts.

Loaded below its SIL, a line supplies lagging reactive power to the system, tending to raise system voltages. Above it, the line absorbs reactive power, tending to depress the voltage. The Ferranti effect describes the voltage gain towards the remote end of a very lightly loaded (or open ended) transmission line. Underground cables normally have a very low characteristic impedance, resulting in an SIL that is typically in excess of the thermal limit of the cable. Hence a cable is almost always a source of lagging reactive power.

ECE 3600 Transmission Line Typical Values

Table 4-1
Transmission Line Parameters with Bundled Conductors (except at 230 kV)
at 60 Hz [2, 6]

Nominal Voltage	$R(\Omega/km)$	$\omega L(\Omega/km)$	$\omega C(\mu S/km)$
230 kV	0.055	0.489	3.373
345 kV	0.037	0.376	4.518
500 kV	0.029	0.326	5.220
765 kV	0.013	0.339	4.988

10^{-6} Siemens

Table 4-2
Surge Impedance and Three-Phase Surge Impedance Loading [2, 6]

Nominal Voltage	$Z_c(\Omega)$	$SIL(MW)$ (MVA)	Cor SIL $I_L(A)$
230 kV	375	140 MW	350A
345 kV	280	425 MW	710A
500 kV	250	1000 MW	1160A
765 kV	255	2300 MW	1740A

Table 4-3
Loadability of Transmission Lines [6]

Line Length (km)	Limiting Factor	Multiple of SIL
0 - 80 km 50 mi	Thermal	> 3
80 - 240 km 50 - 150 mi	5% Voltage Drop	1.5 - 3
240 - 480 km 150 - 300 mi	Stability	1.0 - 1.5

short

medium

Long
240 km +

Typical values for transmission lines taken from:
First Course on Power Systems by Ned Mohan

Long-length Lines: over 240 km (150 miles)

(over 200 mi in some texts)

Need:

		<u>Units</u>			
line length:	len , d	m or km		stick to the same unit length for all parameters miles may also be used	
Resistance per unit length:	r	$\frac{\Omega}{m}$ or $\frac{\Omega}{km}$			
Inductance per unit length:	l	$\frac{H}{m}$ or $\frac{H}{km}$	OR	Inductive reactance per unit length:	x $\frac{\Omega}{m}$ or $\frac{\Omega}{km}$
Capacitance per unit length:	c	$\frac{F}{m}$ or $\frac{F}{km}$	OR	Capacitance admittance per unit length:	y $\frac{S}{m}$ or $\frac{S}{km}$
Conductance to ground:	g	$\frac{S}{m}$ or $\frac{S}{km}$		Common assumption: g := 0 · $\frac{S}{km}$	S := siemens

Find:

		<u>Units</u>
Surge impedance:	$Z_c = \frac{\sqrt{j \cdot x + r}}{\sqrt{j \cdot y + g}}$	Ω
Propagation constant:	$\gamma = \sqrt{(j \cdot x + r) \cdot (j \cdot y + g)}$	$\frac{1}{m}$ or $\frac{1}{km}$

If your calculator doesn't have hyperbolic trig functions

Series impedance $Z_{series} = Z_c \cdot \sinh(\gamma \cdot len) = Z_c \cdot \frac{e^{\gamma \cdot len} - e^{-\gamma \cdot len}}{2}$ Ω

Shunt admittance: $\frac{Y_{shunt}}{2} = \frac{1}{Z_c} \cdot \tanh\left(\gamma \frac{len}{2}\right) = \frac{1}{Z_c} \cdot \frac{e^{\frac{\gamma \cdot len}{2}} - e^{-\frac{\gamma \cdot len}{2}}}{e^{\frac{\gamma \cdot len}{2}} + e^{-\frac{\gamma \cdot len}{2}}} = \frac{1}{Z_c} \cdot \frac{\sqrt{e^{\gamma \cdot len}} - \sqrt{e^{-(\gamma \cdot len)}}}{\sqrt{e^{\gamma \cdot len}} + \sqrt{e^{-(\gamma \cdot len)}}}$ Ω

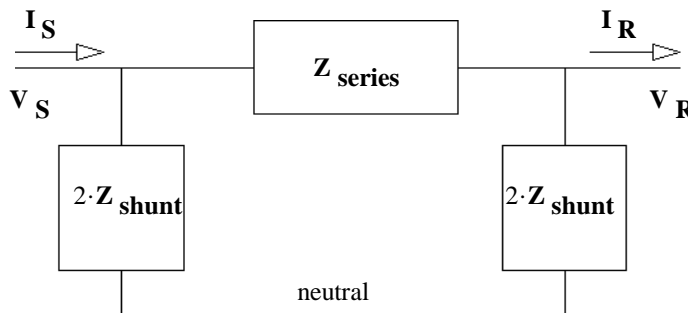
OR

Shunt impedance: $2 \cdot Z_{shunt} = \frac{Z_c}{\tanh\left(\gamma \frac{len}{2}\right)}$ S or $\frac{1}{\Omega}$

If your calculator can't handle complex exponents

$e^{(a+b \cdot j)} = e^a \cdot e^{b \cdot j} = e^a / b$ (in radians)

Model:



Medium-length Lines: 80 - 240 km (50 to 150 miles)

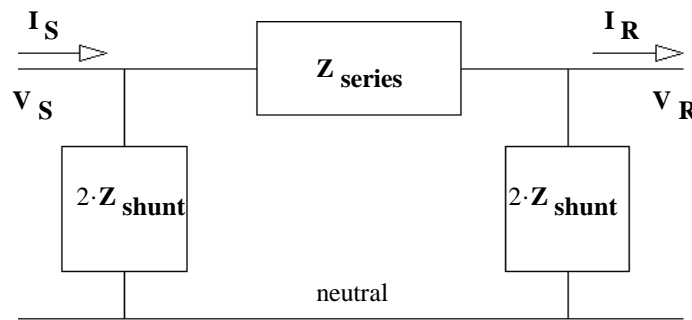
(100 - 200 mi in some texts)

Need:

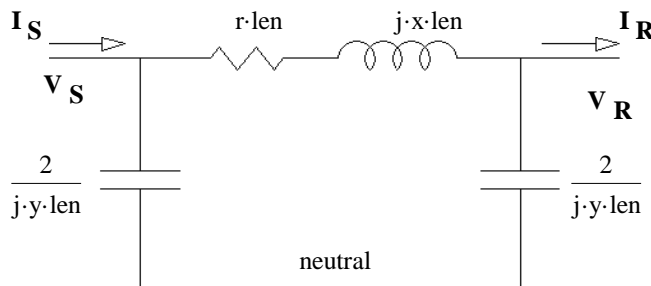
		<u>Units</u>		
line length:	len , d	m or km		stick to the same unit length for all parameters miles may also be used
Resistance per unit length:	r	$\frac{\Omega}{m}$ or $\frac{\Omega}{km}$		
Inductance per unit length:	l	$\frac{H}{m}$ or $\frac{H}{km}$	OR	Inductive reactance per unit length: x $\frac{\Omega}{m}$ or $\frac{\Omega}{km}$
Capacitance per unit length:	c	$\frac{F}{m}$ or $\frac{F}{km}$	OR	Capacitance admittance per unit length: y $\frac{S}{m}$ or $\frac{S}{km}$
Conductance to ground:	g	$\frac{S}{m}$ or $\frac{S}{km}$		Common assumption: g := 0. $\frac{S}{km}$

Find:

		<u>Units</u>
Surge Impedance:	$Z_c = \sqrt{\frac{x}{y}}$	Ω
Series Resistance:	$R_{line} = r \cdot len$	Ω
Series impedance	$Z_{series} = (r + j \cdot x) \cdot len$	Ω
Shunt admittance:	$\frac{Y_{shunt}}{2} = j \cdot y \cdot \frac{len}{2}$	S or $\frac{1}{\Omega}$
OR		
Shunt impedance:	$2 \cdot Z_{shunt} = \frac{2}{j \cdot y \cdot len}$	Ω

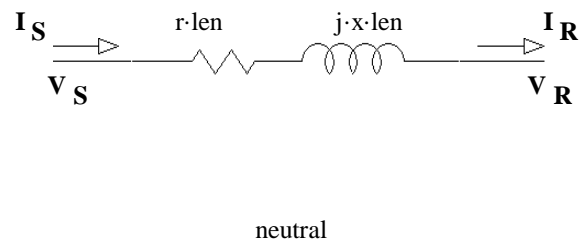


OR:



Short-length Lines: less than 80km (50 mi)
(less than 100 mi in some texts)

Same as above but without the capacitors



ECE 3600 Transmission Line Examples

b

Ex1. A 500 kV transmission line is 500 km long and has the line parameters shown below. Use the long-length model to find V_S and I_S if the line is loaded to 900 MVA and $|V_{RLL}|$ is 490 kV. Assume the phase angle of V_R is 0° and assume load $pf = 1$.

$$\begin{aligned} \text{len} &:= 500 \cdot \text{km} & V_{RLL} &:= 490 \cdot \text{kV} & V_R &:= \frac{V_{RLL}}{\sqrt{3}} & S_{1\phi} &:= \frac{900 \cdot \text{MVA}}{3} \\ r &:= 0.029 \cdot \frac{\Omega}{\text{km}} & \text{Assume: } g &:= 0 \cdot \frac{\text{S}}{\text{km}} \\ x &:= 0.326 \cdot \frac{\Omega}{\text{km}} & y &:= 5.220 \cdot 10^{-6} \cdot \frac{\text{S}}{\text{km}} \end{aligned}$$

Note: These are typical values for a 500 kV transmission line

Long-length line model:

Surge Impedance: $Z_c := \frac{j \cdot x + r}{j \cdot y + g}$ $Z_c = 250.151 - 11.104j \cdot \Omega$

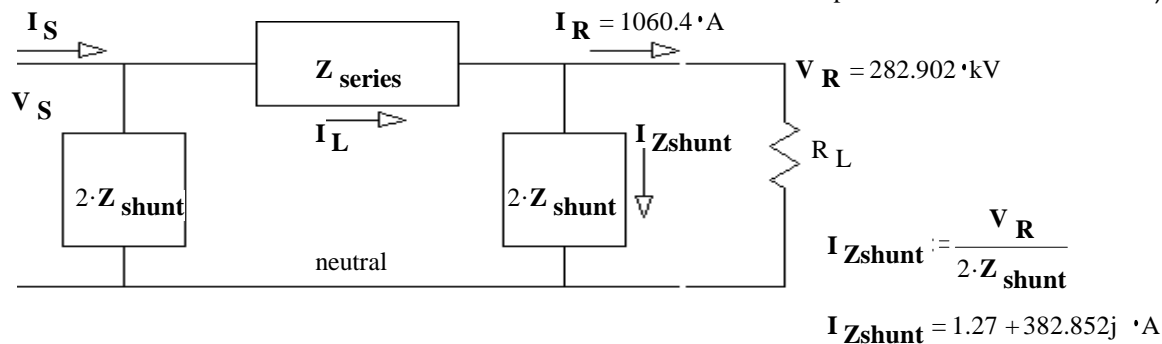
Propagation constant: $\gamma := \sqrt{(j \cdot x + r) \cdot (j \cdot y + g)}$ $\gamma = 5.797 \cdot 10^{-5} + 1.306 \cdot 10^{-3}j \cdot \frac{1}{\text{km}}$

Series impedance: $Z_{\text{series}} := Z_c \cdot \sinh(\gamma \cdot \text{len})$ $Z_{\text{series}} = 12.508 + 151.772j \cdot \Omega$

Shunt admittance: $Y_{\text{shunt}} := \frac{2}{Z_c} \cdot \tanh\left(\gamma \cdot \frac{\text{len}}{2}\right)$ $\frac{Y_{\text{shunt}}}{2} = 4.49 \cdot 10^{-6} + 1.353 \cdot 10^{-3}j \cdot \text{S}$
 (Not used in my solution)

Shunt impedance: $Z_{\text{shunt}} := \frac{Z_c}{2 \cdot \tanh\left(\gamma \cdot \frac{\text{len}}{2}\right)}$ $2 \cdot Z_{\text{shunt}} = 2.451 - 738.924j \cdot \Omega$

Solve circuit: $I_R := \frac{S_{1\phi}}{|V_R|}$ (Not complex in this case because $pf = 1$ otherwise include a phase angle calculated from the pf or load other information)



$I_L := I_{Zshunt} + I_R$ $I_L = 1.062 \cdot 10^3 + 382.852j \cdot \text{A}$

$V_S := V_R + I_L \cdot Z_{\text{series}}$ $V_S = 2.381 \cdot 10^5 + 1.659 \cdot 10^5 j \cdot \text{V}$ $|V_S| = 290.192 \cdot \text{kV}$ $\arg(V_S) = 34.874 \cdot \text{deg}$

$I_{ZshuntS} := \frac{V_S}{2 \cdot Z_{shunt}}$ $I_{ZshuntS} = -223.48 + 322.934j \cdot \text{A}$ $|\sqrt{3} \cdot V_S| = 502.628 \cdot \text{kV}$

$I_S := I_{ZshuntS} + I_L$ $I_S = 838.23 + 705.786j \cdot \text{A}$ $|I_S| = 1096 \cdot \text{A}$ $\arg(I_S) = 40.097 \cdot \text{deg}$

ECE 3600 Transmission Line notes p9

Ex 2. A 345 kV transmission line is 220 km long and has the line parameters shown below.

Find V_S and I_S if the line is loaded to 800MVA with $pf = 91\%$ lagging. $|V_{RLL}|$ is 510 kV. $pf := 0.91$

$$\text{len} := 220 \cdot \text{km} \quad V_{RLL} := 510 \cdot \text{kV} \quad V_R := \frac{V_{RLL}}{\sqrt{3}} \quad \text{Assume the phase angle of } V_R \text{ is } 0^\circ \text{ if } V_R \text{ is given}$$

$$r := 0.037 \cdot \frac{\Omega}{\text{km}} \quad \text{Assume: } g := 0 \cdot \frac{\text{S}}{\text{km}} \quad \text{Note: These are typical values for a 345 kV transmission line}$$

$$x := 0.376 \cdot \frac{\Omega}{\text{km}} \quad y := 4.518 \cdot 10^{-6} \cdot \frac{\text{S}}{\text{km}}$$

Medium-length line model:

$$\text{Series impedance: } Z_{\text{series}} := (r + j \cdot x) \cdot \text{len} \quad Z_{\text{series}} = 8.14 + 82.72j \cdot \Omega$$

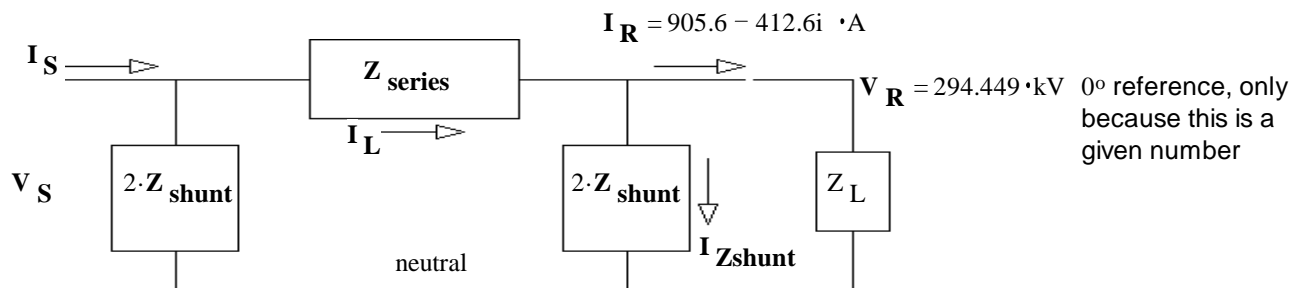
$$\text{Shunt admittance: } Y_{\text{shunt}} := j \cdot y \cdot \text{len} \quad \frac{Y_{\text{shunt}}}{2} = 496.98j \cdot \mu\text{S}$$

Not used in my solution

$$\text{Shunt impedance: } Z_{\text{shunt}} := \frac{1}{j \cdot y \cdot \text{len}} \quad 2 \cdot Z_{\text{shunt}} = -2.012 \cdot 10^3 j \cdot \Omega$$

Solve circuit:

$$S_{1\phi} := \frac{800 \cdot \text{MW}}{3 \cdot \text{pf}} \quad I_R := \frac{S_{1\phi}}{|V_R|} \cdot e^{-j \cdot \arccos(\text{pf})} \quad \text{(Negative phase angle because the pf is lagging)}$$



$$I_{Z\text{shunt}} := \frac{V_R}{2 \cdot Z_{\text{shunt}}} \quad I_{Z\text{shunt}} = 146.335j \cdot \text{A}$$

$$I_L := I_{Z\text{shunt}} + I_R \quad I_L = 905.647 - 266.29j \cdot \text{A}$$

$$V_S := V_R + I_L \cdot Z_{\text{series}} \quad V_S = 3.238 \cdot 10^5 + 7.275 \cdot 10^4 j \cdot \text{V} \quad |V_S| = 331.918 \cdot \text{kV} \quad \arg(V_S) = 12.66 \cdot \text{deg}$$

Line voltage: $|\sqrt{3} \cdot V_S| = 574.9 \cdot \text{kV}$

power angle = $\delta = \arg(V_S) - \arg(V_R) = 12.66 \cdot \text{deg}$

$$I_{Z\text{shunt}S} := \frac{V_S}{2 \cdot Z_{\text{shunt}}} \quad I_{Z\text{shunt}S} = -36.154 + 160.946j \cdot \text{A}$$

$$I_S := I_{Z\text{shunt}S} + I_L \quad I_S = 869.493 - 105.344j \cdot \text{A} \quad |I_S| = 876 \cdot \text{A} \quad \arg(I_S) = -6.908 \cdot \text{deg}$$

Ex3. A 230 kV transmission line has the following length and line parameters.

$$\text{len} := 150 \cdot \text{km} \quad r := 0.06 \cdot \frac{\Omega}{\text{km}} \quad x := 0.5 \cdot \frac{\Omega}{\text{km}} \quad g := 0 \cdot \frac{\text{S}}{\text{km}} \quad y := 4 \cdot 10^{-6} \cdot \frac{\text{S}}{\text{km}}$$

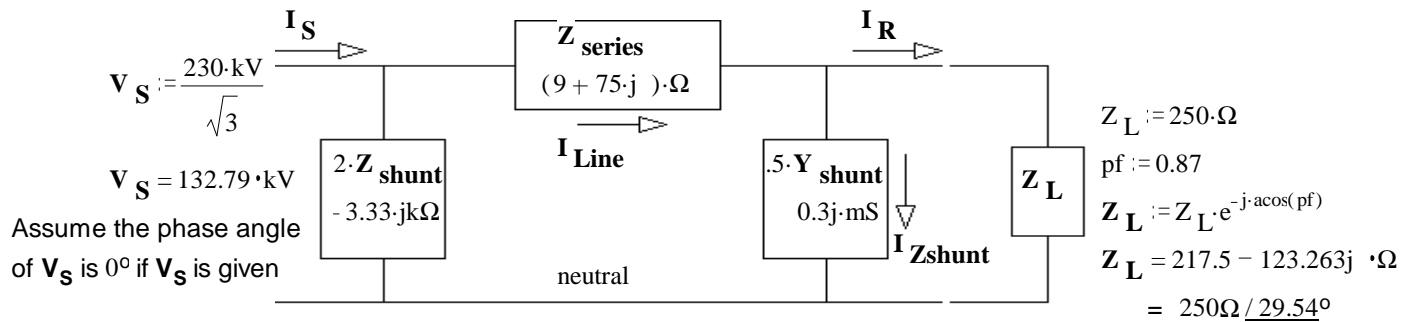
Medium-length line model:

Series impedance: $Z_{\text{series}} := (r + j \cdot x) \cdot \text{len} \quad Z_{\text{series}} = 9 + 75j \cdot \Omega$

Shunt admittance: $Y_{\text{shunt}} := j \cdot y \cdot \text{len} \quad \frac{Y_{\text{shunt}}}{2} = 0.3j \cdot \text{mS}$

Shunt impedance: $Z_{\text{shunt}} := \frac{1}{j \cdot y \cdot \text{len}} \quad 2 \cdot Z_{\text{shunt}} = -3.333j \cdot \text{k}\Omega$

a) The load is 250Ω with a power factor of 0.87, leading. Find the line current, I_{Line} .



$$Z := Z_{\text{series}} + \frac{1}{\frac{Y_{\text{shunt}}}{2} + \frac{1}{Z_L}} \quad Z = 210.467 - 56.544j \cdot \Omega = 219.7\Omega / -15.04^\circ$$

$$I_{\text{Line}} := \frac{V_S}{Z} \quad I_{\text{Line}} = 588.459 + 158.096j \cdot \text{A} = 609.3\text{A} / 15.04^\circ$$

b) Find the load line voltage.

$$I_{\text{Line}} \cdot Z_{\text{series}} = -6.561 + 45.557j \cdot \text{kV}$$

$$V_R := V_S - I_{\text{Line}} \cdot Z_{\text{series}} \quad V_R = 139.352 - 45.557j \cdot \text{kV} = 146.6\text{kV} / -18.1^\circ$$

$$\text{Receiving line voltage} = \sqrt{3} \cdot V_R = 253.9 \cdot \text{kV}$$

Notice that $|V_R|$ is bigger than $|V_S|$, this can happen when the receiving-end power factor is leading.

c) What is the "power angle" (δ)?

$$\delta = -\arg(V_R) = 18.104 \cdot \text{deg}$$

d) How much power is delivered to the load?

$$I_R := \frac{V_R}{Z_L} \quad P_L = 3 \cdot |V_R| \cdot |I_R| \cdot \text{pf} = 224.4 \cdot \text{MW}$$

Power estimate for the same $|V_R|$ and $|V_S|$, but neglecting the line resistance:

$$\approx 3 \cdot \frac{|V_S| \cdot |V_R| \cdot \sin(18.1 \cdot \text{deg})}{|Z_{\text{series}}|} = 240 \cdot \text{MW}$$

e) Express this loading in terms of SIL

Surge Impedance: $Z_c := \sqrt{\frac{x}{y}} \quad Z_c = 353.6 \cdot \Omega$

$$\frac{Z_c}{Z_L} = 1.414 \quad \text{SIL load}$$

Not asked for in this class

Answer the following questions in your textbook, starting on p.488.

- 9-3 What factors influence the inductance of a transmission line?
- 9-4 Suppose that there are two transmission lines using a single conductor per phase, and that the conductors in the two transmission lines are identical (same material and same diameter). If one transmission line is rated at 345 kV and the other one is rated at 238 kV. which transmission line is likely to have the highest inductance? Why?
- 9-5 Suppose someone asked you to evaluate a proposal for an underwater power cable between North Carolina and the Bahamas. What would you say about the probability of success of this proposal? Why?
- 9-6 What line lengths are generally considered to be short transmission lines? Medium-length transmission lines? Long transmission lines?
- 9-9 What happens to the receiving end voltage as the load on a transmission line is increased if the load has a lagging power factor? Sketch a phasor diagram showing the resulting behavior.
- 9-11 What happens to the receiving end voltage as the load on a transmission line is increased if the load has a leading power factor? Sketch a phasor diagram showing the resulting behavior.
- 9-12 What is the significance of the angle δ between \mathbf{V}_S and \mathbf{V}_R in a transmission line?

Problems

1. A 230 kV transmission line is 70 km long and has line parameters shown in Table 4.1 (handout). $|\mathbf{V}_{SLL}|$ is 230 kV.

Assume the phase angle of \mathbf{V}_S is 0° and that the source sees a pf = 0.8, lagging.

From Table 4.1: $r := 0.055 \Omega/\text{km}$ $x := 0.489 \Omega/\text{km}$ $y := 3.373 \cdot 10^{-6} \text{ S}/\text{km}$ Assume: $g := 0 \text{ S}/\text{km}$

- a) Use the short-length model to find \mathbf{I}_R and \mathbf{V}_R if the source is loaded to 170 MVA (as calculated for the line).
 b) What is the angle δ ?
 c) What is the power factor of the load?

Solve the following problems in your textbook, starting on p.489.

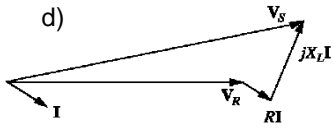
2. 9-11 A 138 kV, 200 MVA, 60 Hz, three-phase, power transmission line is 100 km long, and has the following characteristics:

$r := 0.103 \Omega/\text{km}$ $x := 0.525 \Omega/\text{km}$ $y := 3.3 \cdot 10^{-6} \text{ S}/\text{km}$

- a) What is per phase series impedance and shunt admittance of this transmission line?
 b) Should it be modeled as a short, medium, or long transmission line?
 d) Sketch the phasor diagram of this transmission line when the line is supplying rated voltage and apparent power at a 0.90 power factor lagging.
 e) Calculate the sending-end voltage if the line is supplying rated voltage and apparent power at 0.90 PF lagging.
 f) What is the voltage regulation of the transmission line for the conditions in (e)?
 g) What is the efficiency of the transmission line for the conditions in (e)?
 h) 9-13 What is the "power angle", δ ?
 Original problem statement: If the series resistance and shunt admittance of the transmission line in Problem 9-11 are not ignored, what would the value of the angle δ be at rated conditions and 0.90 PF lagging?
3. 9-12 If the series resistance and shunt admittance of the transmission line in Problem 9-11 are ignored, what would the value of the angle δ be at rated conditions and 0.90 PF lagging?
4. A 765 kV transmission line is 200 km long and has line parameters shown in Table 4.1, p.4-10. Use the medium-length model to find \mathbf{V}_S and \mathbf{I}_S if the line is loaded to 1800 MVA and $|\mathbf{V}_{RLL}|$ is 770 kV. Assume the phase angle of \mathbf{V}_R is 0° and assume load pf = 1.

Table 4.1: $r := 0.013 \Omega/\text{km}$ $x := 0.339 \Omega/\text{km}$ $y := 4.988 \cdot 10^{-6} \text{ S}/\text{km}$

Answers

1. a) $426.7 \text{ A} \angle -36.87\text{-deg}$ $123.2 \text{ kV} \angle -4.98\text{-deg}$ 2. a) $(10.3 + j52.5) \cdot \Omega$ d)  e) 111.8 kV
 b) 4.98 deg c) 0.849 $j \cdot 0.00033 \cdot \text{S}$ f) 40.3%
 b) medium g) 89.3%
 3. 21.8 deg h) 18.74 deg
 4. 443 kV $\angle 12.0^\circ$ 1375 A $\angle 18.56^\circ$