

Name: _____

ECE 3510 homework 3B

d

1. Find the inverse Laplace transform of each of the following functions: Use the mixed method and the tables.

a) $F(s) = \frac{3s+6}{(s^2+1)\cdot(s^2+4)}$

b) $F(s) = \frac{1}{(s+2)\cdot(s+1)^2}$

$$c) \quad F(s) = \frac{2 \cdot s}{s^2 + 2 \cdot s + \frac{5}{4}}$$

$$d) \quad F(s) = \frac{8s + 4}{s^2 \cdot (s + 1)^2}$$

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$$e) \quad F(s) = \frac{\frac{1}{2} \cdot s^3 + s^2 + s + \frac{5}{2}}{s^2 \cdot (s^2 + 2 \cdot s + 5)}$$

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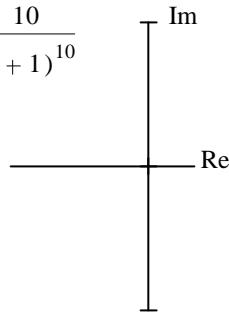
$$2. F(s) = \frac{s-1}{s^3 \cdot (s^2 + 2s + 5)^2}$$

Show the form of $f(t)$ without actually finding it. Indicate which of the coefficients may not be 0

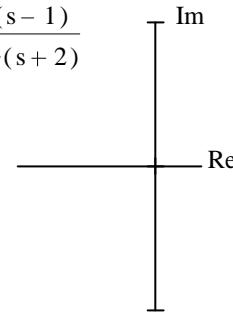
3. Problem 2.3 a) - g) in textbook (p.21)

As part of your work to reach a solution, draw the pole diagram for each.

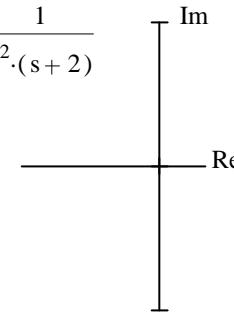
$$a) \frac{10}{(s+1)^{10}}$$



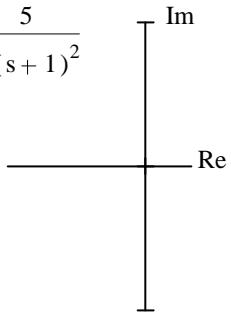
$$b) \frac{(s-1)}{s \cdot (s+2)}$$



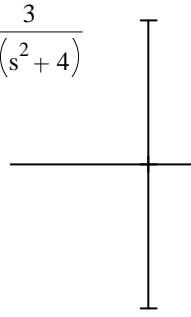
$$c) \frac{1}{s^2 \cdot (s+2)}$$



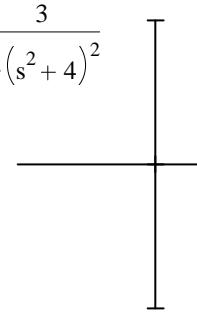
$$d) \frac{5}{s \cdot (s+1)^2}$$



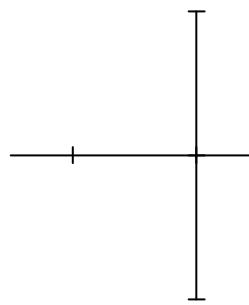
$$e) \frac{3}{s \cdot (s^2 + 4)}$$



$$f) \frac{3}{s \cdot (s^2 + 4)^2}$$



$$g) \frac{2 \cdot (s-1)}{(s^2 + 2s + 1) \cdot (s+3)}$$



Bounded

Converges

$f(\infty)$

a)

b)

c)

d)

e)

f)

Answers (time functions below valid for $t \geq 0$ only)

$$1. a) (\cos(t) + 2\sin(t) - \cos(2t) - \sin(2t)) \cdot u(t)$$

$$b) (e^{-2t} + t \cdot e^{-t} - e^{-t}) \cdot u(t)$$

$$c) \left(2e^{-t} \cdot \cos\left(\frac{1}{2}t\right) - 4e^{-t} \cdot \sin\left(\frac{1}{2}t\right)\right) \cdot u(t)$$

$$d) (4t - 4e^{-t}) \cdot u(t)$$

$$e) \left(\frac{1}{2}t + \frac{1}{2}e^{-t} \cdot \cos(2t)\right) \cdot u(t)$$

$$2. (A + Bt + Ct^2 + D \cdot e^{at} \cdot \cos(bt) + E \cdot e^{at} \cdot \sin(bt) + F \cdot t \cdot e^{at} \cdot \cos(bt) + G \cdot t \cdot e^{at} \cdot \sin(bt)) \cdot u(t)$$

C may not be 0 & Either F or G may be 0, but **NOT BOTH**

$$\text{Alternate solution: } \left(A + Bt + Ct^2 + \sqrt{D^2 + E^2} \cdot e^{at} \cdot \cos(bt + \theta) + \sqrt{F^2 + G^2} \cdot t \cdot e^{at} \cdot \cos(bt + \phi)\right) \cdot u(t)$$

3. Bounded Converges $f(\infty)$

a) yes yes 0

Bounded Converges $f(\infty)$

yes yes 5

Can't be 0: C & $\sqrt{F^2 + G^2}$

b) yes yes $-\frac{1}{2}$

d) yes yes no

c) no

f) no

g) yes yes 0