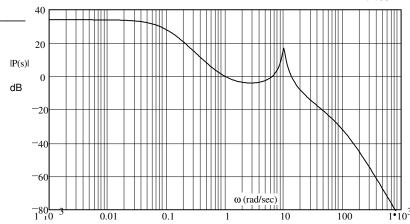
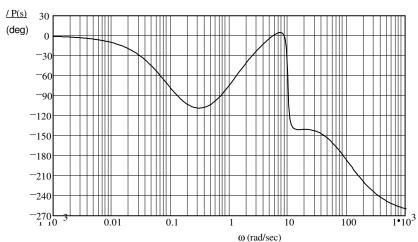
Name: _

Hand in this page showing how you used the drawings to find answers to 1a and 3b.

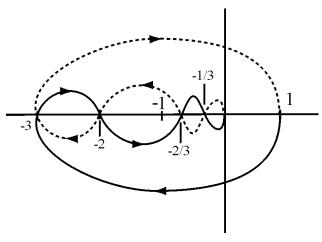
You must show the work needed to get the answers below

- 1. Problem 5.9 (p.142) in the text.
 - a) Give the gain margin and the phase margin of the system whose Bode plots are shown at right (the plots are for the open-loop transfer function and the closed-loop transfer function is assumed to be stable).





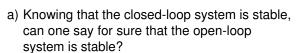
b) Indicate whether the system whose Nyquist curve is shown below is closed-loop stable, given that it is open-loop stable.

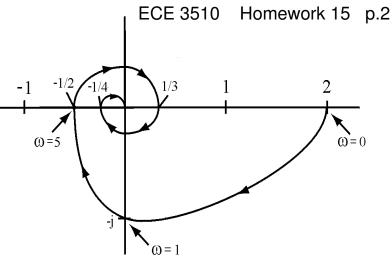


c) What are the values of the gain g > 0 by which the open-loop transfer function of part (b) may be multiplied, with the closed-loop system being stable?

d) Sketch an example of a Nyquist curve for a system which has three unstable open-loop poles, and which is closed-loop stable.

2. Problem 5.11 (p.144) in the text. All parts of this problem refer to the system whose Nyquist curve is shown at right (only the portion for $\omega > 0$ is plotted). Recall that the Nyquist curve represents the frequency response of the open-loop system, or $G(j\omega)$. If G(s) is the open-loop transfer function. The closed-loop transfer function is G(s)/(1+G(s)).

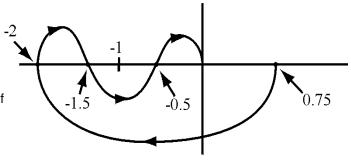




- b) Given the closed-loop system is stable, estimate the gain margin and the phase margin of the closed-loop system.
- c) How many unstable poles does the closed-loop system have if the open-loop gain is multiplied by 5?
- d) Give the steady-state response yss(t) of the open-loop system to an input x(t) = 2. Repeat for x(t)=3cos(t), and x(t)=4cos(5t).
- e) Repeat part (d) for the closed-loop system.

- 3. Problem 5.13 (p.144) in the text.
 - a) Consider the Nyquist diagram of a transfer function G(s) shown at right. Only the portion for $\omega > 0$ is plotted.

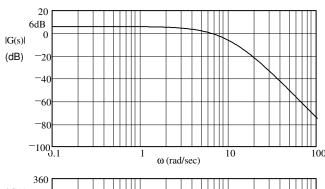
Assume that G(s) has no poles in the open right-half plane, and that a gain K is cascaded with G(s). Find the ranges of positive K for which the closed-loop system is stable.

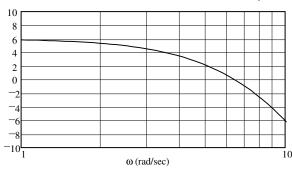


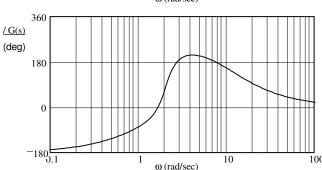
- b) Bode plots of the open-loop transfer function of a feedback system are shown below, with the detail from 1 to 10 rad/sec shown on the left. For this system:
 - How much can the open-loop gain be changed (increased and/or decreased) before the closed-loop system becomes unstable ?
 - What is a rough estimate of the phase margin of the feedback system? Show on the graph how the results are obtained. The numerical results do not have to be precise.

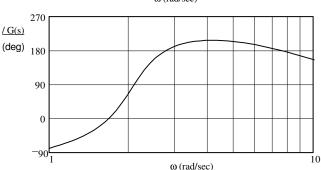
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c) For the system of part (b), give the steady-state response of the open-loop system and of the closed-loop system to an input x(t) = 2.

|G(s)|

(dB)

- 4. Problem 5.14 (p.146) in the text.
 - a) Consider the lead controller for the double integrator. For the design that makes the crossover frequency equal to ω_C , obtain the polynomial that specifies the closed-loop poles (as a function of a/b and ω_C). Show that one closed-loop pole is at $s = -\omega_C$ no matter what a/b is.

Hints: Find: $G(s) = P(s) \cdot C(s)$

Find the denominator of the closed-loop transfer function: ${
m D}_{G}+{
m N}_{G}$

Substitute in a, b, and k_c like eq. 5.62 in book, but use $\sqrt{\frac{a}{b}}$ instead of 3 (as mentioned in class).

Use polynomial division to show that $D_{G} + N_{G}$ can be divided by $(s + \omega_{c})$ with no remainder.

b) Compute the other closed-loop poles, as functions of ω_C , when a/b = 5.83, 9, and 13.9. Hint: The "other" roots are the roots of the quotient.

Answers

- 1. a) GM \simeq 30·dB
- PM $\sim 40 \cdot \deg$

- b) yes c) $0 < g < \frac{1}{3}$, $\frac{1}{2} < g < \frac{3}{2}$ or g > 3

- d) Need 3 CCW encirclements of -1

- 2. a) yes b) GM $\simeq 2 \ (30 \cdot dB)$ PM $\simeq 90 \cdot deg$ c) 4 e) $\frac{4}{3}$, $\frac{3 \cdot \sqrt{2}}{2} \cdot \cos(t 45 \cdot deg)$, $-4 \cdot \cos(5 \cdot t)$
 - d) 4, $3 \cdot \cos(t 90 \cdot \deg)$, $-2 \cdot \cos(5 \cdot t)$
- 3. a) $k < \frac{1}{2}$, $\frac{2}{3} < k < 2$ b) Gain may be increased by $\approx 2 dB$ and reduced by $\approx 5 dB$. PM = 10° to 15°

- c) Open loop: -4 Closed loop: 4
- 4. b) $(-0.7071 0.7071 \cdot j) \cdot \omega_c$ & $(-0.7071 + 0.7071 \cdot j) \cdot \omega_c$, $-\omega_c$ & $-\omega_c$, $-0.436 \cdot \omega_c$ & $-2.292 \cdot \omega_c$ (double) ECE 3510 Homework 15 p.3