

1. Draw a control system loop like the bottom one shown on p.2 of my Control System Characteristics & Performance notes. This is a more complex version of Fig 4.7 (Bodson, p.67), including gain, a feedback sensor (  $F(s)$  ) and a disturbance input (  $D(s)$  ).

2. With  $F(s)$  (or  $N_F(s)$  and  $D_F(s)$  ) added into the following equations, find:

a) The full  $Y(s) =$

Note: you may consider  $k$  as part of  $C(s)$ .

- b)  $\mathbf{E}(s)$  with disturbance ( $\mathbf{D}(s)$ ) as zero: Eq. 4.14  
Also find the "DC gain" from  $\mathbf{R}(s)$  to  $\mathbf{E}(s)$ . Eq. 4.19

- c)  $\mathbf{E}(s)$  with input ( $\mathbf{R}(s)$ ) as zero: Eq. 4.22  
Also find the "DC gain" from  $\mathbf{D}(s)$  to  $\mathbf{E}(s)$ . Eq. 4.23

3. List 5 measures of a control system's quality (see p. 64) and list one or two things that can be done to achieve each.

- 1.
- 2.
- 3.
- 4.
- 5.

4. The transfer functions of  $\mathbf{C}(s)$  and  $\mathbf{P}(s)$  are given below. In each case determine if the steady-state error will go to zero and whether disturbances will be completely rejected. Be sure to check for closed-loop stability when needed.

a)  $\mathbf{C}(s) = \frac{s + 4}{s^2 + 3 \cdot s + 2}$        $\mathbf{P}(s) = \frac{s + 1}{s^2 + 3 \cdot s}$

$$\text{b) } \mathbf{C}(s) = \frac{s+1}{s^2+3\cdot s} \quad \mathbf{P}(s) = \frac{s+4}{s^2+3\cdot s+2}$$

$$\text{c) } \mathbf{C}(s) = \frac{s\cdot(s+6)}{s^2+3\cdot s+2} \quad \mathbf{P}(s) = \frac{s+8}{s^2+12\cdot s}$$

$$\text{d) } \mathbf{C}(s) = \frac{s+9}{s^2+3\cdot s+2} \quad \mathbf{P}(s) = \frac{s}{s+16}$$

$$e) \quad C(s) = \frac{s+1}{s^2+5s+6} \quad \mathbf{P}(s) = \frac{s+1}{s^2+8s+15}$$

$$f) \quad C(s) = \frac{s+1}{s^3+7s^2+12s} \quad \mathbf{P}(s) = \frac{s+1}{s+3}$$

5. Problem 4.2 (p.108) in the text. Determine whether all the roots of the following polynomials are in the open left half-plane. Use your calculator or Matlab to find the actual roots, or use the Routh-Hurwitz method.

$$a) \quad \mathbf{D}(s) = s^4 + 4s^3 + 3s^2 + 4s + 1$$

b)  $D(s) = s^5 + 5 \cdot s^4 + 8 \cdot s^3 + 4 \cdot s^2 - s - 1$

c)  $D(s) = s^4 + 2 \cdot s^3 + 2 \cdot s^2 + 2 \cdot s + 1$

**Answers**

1. & 2. See notes and read sections 4.1 - 4.2 in text (Bodson).

3. b) Eq. 4.14  $\frac{1}{1 + F \cdot P \cdot k \cdot C} \cdot R$

Eq. 4.19  $\frac{1}{1 + F(0) \cdot P(0) \cdot C(0)}$

c) Eq. 4.22  $\frac{-F \cdot P}{1 + P \cdot k \cdot C \cdot F} \cdot D$

Eq. 4.23  $\frac{-F(0) \cdot P(0)}{1 + F(0) \cdot P(0) \cdot C(0)}$

- 4. a) Yes No
- c) No No
- e) No No

- b) Yes Yes
- d) No Yes
- f) Yes Yes

3. a)  $Y(s) = \frac{P \cdot C \cdot R + P \cdot D}{1 + P \cdot C \cdot F} = \frac{P \cdot k \cdot C \cdot R + P \cdot D}{1 + P \cdot k \cdot C \cdot F}$   
 k as part of C(s)      k separate from C(s)

OR  $\frac{D_F(0) \cdot D_P(0) \cdot D_C(0)}{D_F(0) \cdot D_P(0) \cdot D_C(0) + N_F(0) \cdot N_P(0) \cdot N_C(0)}$

OR  $\frac{-N_F(0) \cdot N_P(0) \cdot D_C(0)}{D_F(0) \cdot D_P(0) \cdot D_C(0) + N_F(0) \cdot N_P(0) \cdot N_C(0)}$

5. a) Yes      b) No      c) No

6. EXTRA CREDIT    a)  $0 < K < 0.4975$   
 b)  $0 < K < 2.25$

## 6. EXTRA CREDIT

Characteristic equations of feedback systems are shown below. In each case, use the Routh-Hurwitz method to determine the value range of  $K$  that will produce a stable system. You must show your work.

a)  $0 = s^4 + 20 \cdot s^3 + 10 \cdot s^2 + s + K$

b)  $0 = s^4 + 2 \cdot K \cdot s^3 + 5 \cdot s^2 + K \cdot s + K$