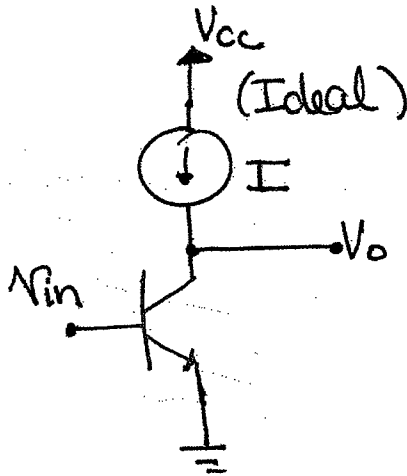
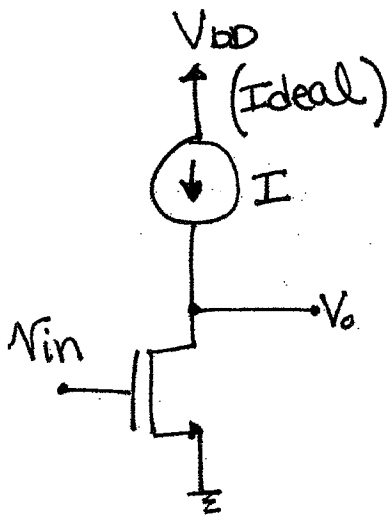
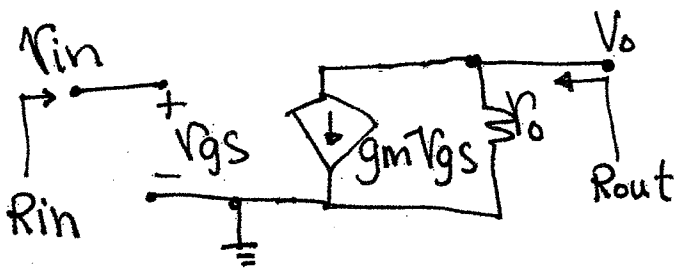


CS/CE Amplifiers



Ideal current source is open:

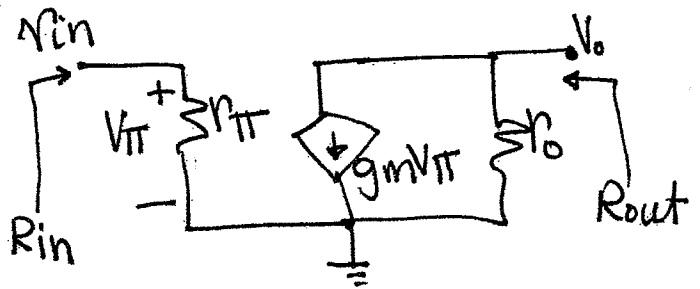


$$R_{in} = \infty$$

$$R_{out} = r_o = \frac{V_A}{I_D}$$

$$\frac{V_o}{V_{in}} = A_{vo} = -g_m r_o$$

$$A_{vo} = -\frac{2V_A}{V_{ov}}$$



$$R_{in} = r_{\pi}$$

$$R_{out} = r_o = \frac{V_A}{I_C}$$

$$\frac{V_o}{V_{in}} = A_{vo} = -g_m r_o$$

$$A_{vo} = -\frac{V_A}{V_T}$$

Definition:

"intrinsic gain", $A_o = g_m r_o$

Example: $I = 100\mu\text{A}$ (for both)

$$(\mu_n C_{ox}) = 267\mu\text{A}/\text{V}^2$$

$$\left(\frac{W}{L}\right) = \left(\frac{4\mu\text{m}}{.4\mu\text{m}}\right)$$

$$V_A = V_A' \cdot L = 10\frac{\text{V}}{\mu\text{m}} \cdot 0.4\mu\text{m}$$

$$\beta = 100$$

$$V_A = 10\text{V}$$

MOSFET:

$$100\mu = I_D = \frac{1}{2}(267\mu) \cdot \left(\frac{4}{.4}\right) (V_{ov})^2$$

$$\therefore V_{ov} = 0.27\text{V}$$

$$g_m = \frac{2I_D}{V_{ov}} = \frac{2(100\mu)}{0.27} = 0.74\text{m}$$

$$R_{in} = \underline{\underline{\infty}}$$

$$R_{out} = r_o = \frac{V_A' \cdot L}{I_D} = \frac{10 \times 0.4}{100\mu} = \underline{\underline{40\text{K}\Omega}}$$

$$A_o = g_m r_o = 0.74\text{m} \times 40\text{K} = \underline{\underline{29.6\frac{\text{V}}{\text{V}}}}$$

BJT:

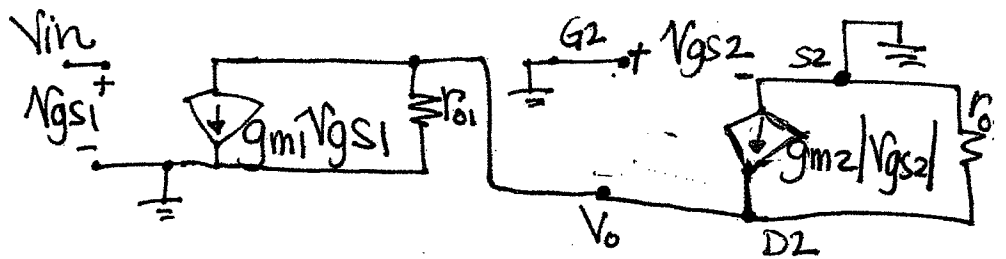
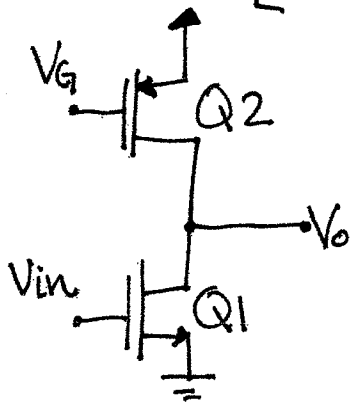
$$g_m = \frac{I_c}{V_T} = \frac{100\mu}{25\text{m}} = 4\text{m}\frac{\text{A}}{\text{V}}$$

$$R_{in} = r_{\pi} = \frac{\beta}{g_m} = \frac{100}{4\text{m}} = \underline{\underline{25\text{K}\Omega}}$$

$$r_o = \frac{V_A}{I_c} = \frac{10}{100\mu} = \underline{\underline{100\text{K}\Omega}} = R_{out}$$

$$A_o = 4\text{m}(100\text{K}) = \underline{\underline{400\frac{\text{V}}{\text{V}}}}$$

[Not ideal current source]:



$$V_{gs1} = V_{in}$$

Node - Voltage:

$$+g_{m1} V_{gs1} + \frac{+V_o}{r_{o1}} + g_{m2} V_{gs2} + \frac{V_o}{r_{o2}} = 0$$

$$V_o = \frac{-g_{m1} V_{gs1}}{\frac{1}{r_{o1}} + \frac{1}{r_{o2}}} \quad \begin{matrix} V_{gs2} = 0 \\ = -g_{m1} V_{gs1} (r_{o1} \parallel r_{o2}) \end{matrix}$$

$$\frac{V_o}{V_{in}} = A_v = -g_{m1} (r_{o1} \parallel r_{o2})$$

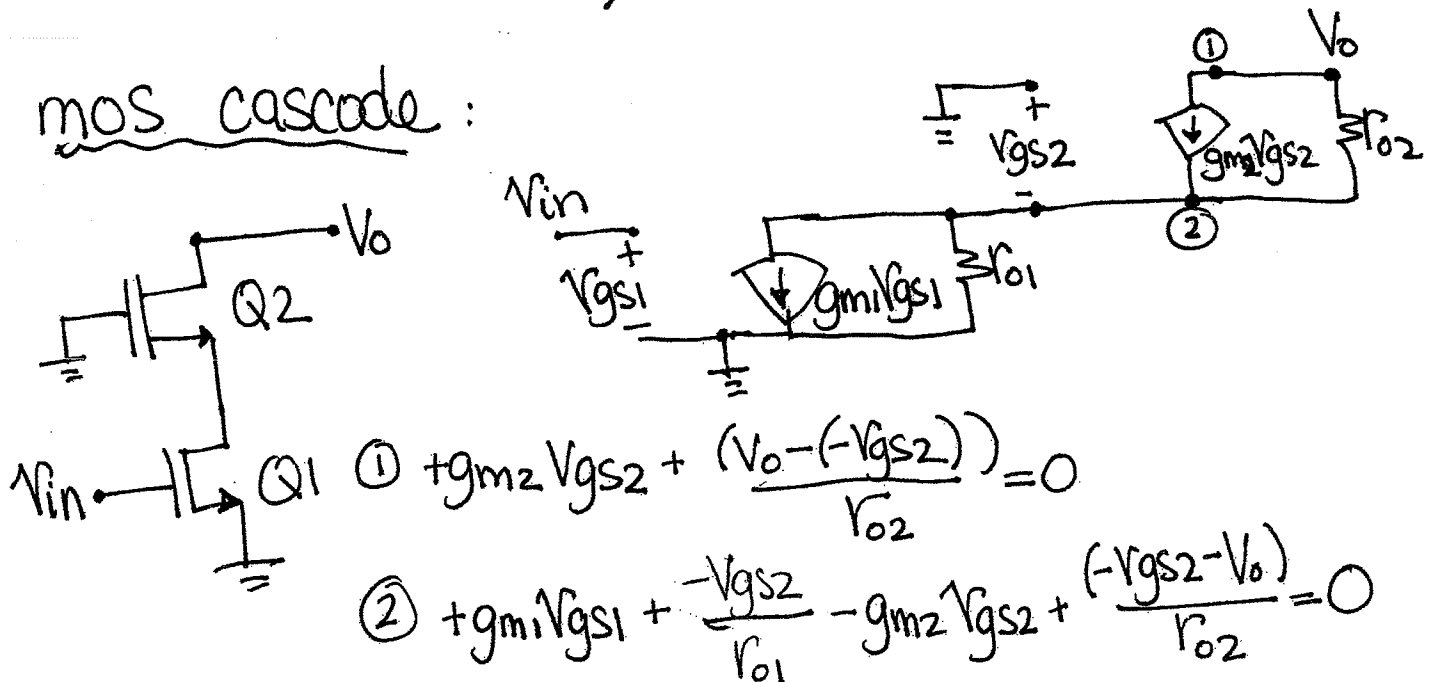
Cascode Amplifier

- current buffer: unity current, $\uparrow R_{out}$
- voltage buffer: unity voltage, $\downarrow R_{out}$
- Cascoding:

$$V_o = -g_m V_{in} (r_{o1} \parallel r_{o2})$$

method: connect C_G (or CB) at output of CS (or CE)

mos cascode:



From ①: $V_{gs2} (g_{m2} + \frac{1}{r_{o2}}) = -\frac{V_o}{r_{o2}}$

$$V_{gs2} = -\frac{V_o}{r_{o2}} \left[\frac{1}{\frac{r_{o2}g_{m2} + 1}{r_{o2}}} \right] = \frac{-V_o}{r_{o2}g_{m2} + 1}$$

plug into (2)

$$g_{m1}(V_{in}) = v_{gs2} \left[\frac{1}{r_{o1}} + g_{m2} + \frac{1}{r_{o2}} \right] + \frac{V_o}{r_{o2}}$$

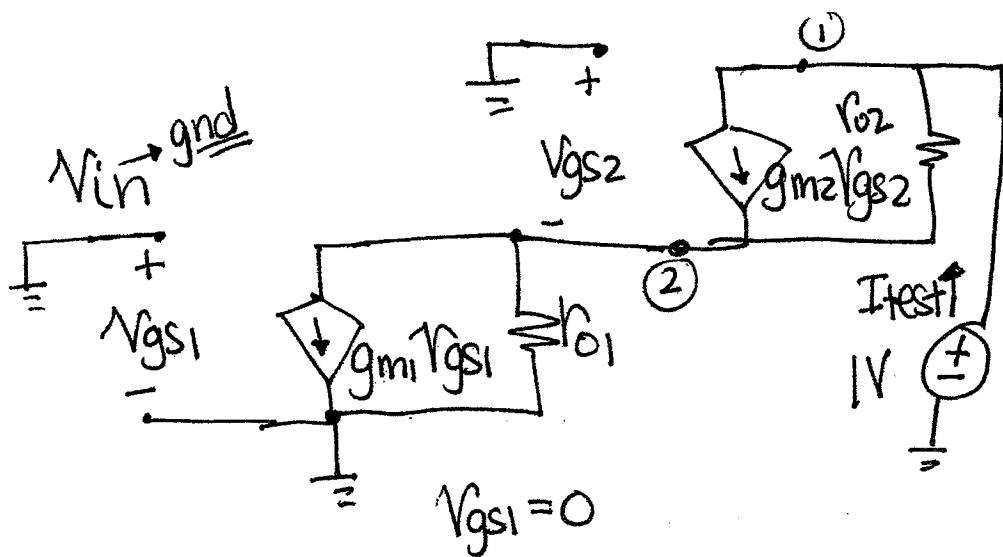
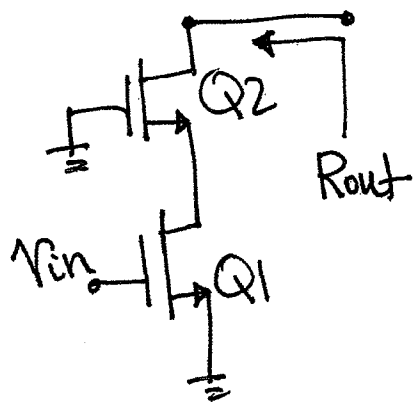
$$g_{m1}(V_{in}) = \frac{-V_o}{(1+g_{m2}r_{o2})} \left[\frac{r_{o2} + g_{m2}r_{o1}r_{o2} + r_{o1}}{r_{o1}r_{o2}} \right] + \frac{V_o(1+g_{m2}r_{o2})r_{o1}}{(1+g_{m2}r_{o2})r_{o1}r_{o2}}$$

$$\left[\frac{-r_{o2} - g_{m2}r_{o1}r_{o2} - r_{o1} + r_{o1} + g_{m2}r_{o1}r_{o2}}{(1+g_{m2}r_{o2})r_{o1}r_{o2}} \right] V_o = g_{m1}(V_{in})$$

$$\left[\frac{-r_{o2}}{(1+g_{m2}r_{o2})r_{o1}r_{o2}} \right] V_o = g_{m1}(V_{in})$$

$$\frac{V_o}{V_{in}} = \frac{-g_{m1}(1+g_{m2}r_{o2})r_{o1}r_{o2}}{r_{o2}} = -g_{m1}r_{o1}(1+g_{m2}r_{o2})$$

Output R



$$\textcircled{1} \quad +g_{m2}V_{gs2} + \frac{(1+V_{gs2})}{r_{o2}} = I_{test}$$

$$\textcircled{2} \quad +\frac{-V_{gs2}}{r_{o1}} - g_{m2}V_{gs2} + \frac{(-V_{gs2}-1)}{r_{o2}} = 0$$

$$V_{gs2} \left[\frac{1}{r_{o1}} + g_{m2} + \frac{1}{r_{o2}} \right] = \frac{-1}{r_{o2}}$$

$$V_{gs2} \left[\frac{r_{o2} + g_{m2}r_{o1}r_{o2} + r_{o1}}{r_{o1}r_{o2}} \right] = \frac{-1}{r_{o2}} \Rightarrow V_{gs2} = \frac{-r_{o1}}{r_{o1} + r_{o2} + g_{m2}r_{o1}r_{o2}}$$

plug back into ①

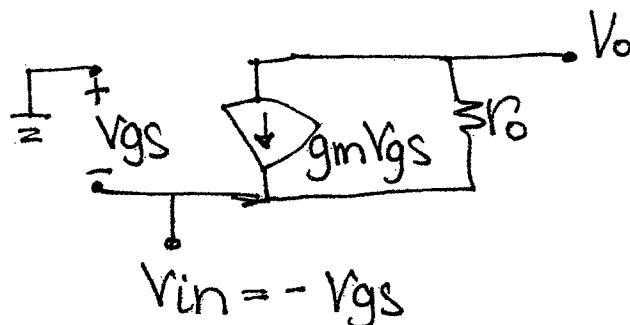
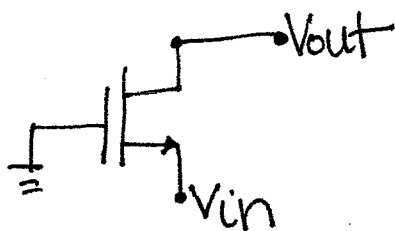
$$I_{test} = V_{gs2} \left(g_{m2} + \frac{1}{r_{o2}} \right) + \frac{1}{r_{o2}}$$

$$I_{test} = \frac{-r_{o1} [g_{m2}r_{o2} + 1]}{r_{o2} (r_{o1} + r_{o2} + g_{m2}r_{o1}r_{o2})} + \frac{(r_{o1} + r_{o2} + g_{m2}r_{o1}r_{o2})}{r_{o2} (r_{o1} + r_{o2} + g_{m2}r_{o1}r_{o2})}$$

$$I_{\text{test}} = \frac{r_{o2}}{r_{o2} (r_{o1} + r_{o2} + g_{m2} r_{o1} r_{o2})}$$

$$R_{\text{out}} = R_{\text{th}} = \frac{1}{I_{\text{test}}} = r_{o1} + r_{o2} + g_{m2} r_{o1} r_{o2}$$

CG:

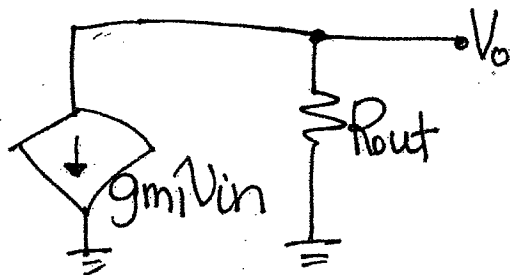


$$V_o = -g_m V_{gs} r_o = +g_m \underline{V_{in}} r_o$$

Intrinsic gain

$$\therefore R_{\text{out}} \approx (g_{m2} r_{o2}) \cdot r_{o1}$$

$$A_v \approx -g_{m1} r_{o1} (g_{m2} r_{o2})$$



voltage gain can be easily found as

$$A_v = \frac{v_o}{v_i} = -g_{m1}[R_{on} \parallel R_{op}]$$

Thus,

$$\textcircled{1} \quad A_v = -g_{m1}\{[(g_{m2}r_{o2})r_{o1}] \parallel [(g_{m3}r_{o3})r_{o4}]\} \quad (7.29)$$

For the case in which all transistors are identical,

$$\textcircled{1} \quad A_v = -\frac{1}{2}(g_m r_o)^2 = -\frac{1}{2}A_0^2 \quad (7.30)$$

By comparison to the gain expression in Eq. (7.18'), we see that using the cascode configuration for both the amplifying transistor and the current-source load transistor results in an increase in the magnitude of gain by a factor equal to A_0 .

Example 7.4

It is required to design the cascode current-source of Fig. 7.10 to provide a current of 100 μA and an output resistance of 500 $\text{k}\Omega$. Assume the availability of a 0.18- μm CMOS technology for which $V_{DD} = 1.8 \text{ V}$, $V_{tp} = -0.5 \text{ V}$, $\mu_p C_{ox} = 90 \mu\text{A}/\text{V}^2$ and $V_A' = -5 \text{ V}/\mu\text{m}$. Use $|V_{OV}| = 0.3 \text{ V}$ and determine L and W/L for each transistor, and the values of the bias voltages V_{G3} and V_{G4} .

Solution

The output resistance R_o is given by

$$R_o = (g_{m3}r_{o3})r_{o4}$$

Assuming Q_3 and Q_4 are identical,

$$\begin{aligned} R_o &= (g_m r_o)r_o \\ &= \frac{|V_A|}{|V_{OV}|/2} \times \frac{|V_A|}{I_D} \end{aligned}$$

Using $|V_{OV}| = 0.3 \text{ V}$, we write

$$500 \text{ k}\Omega = \frac{|V_A|}{0.15} \times \frac{|V_A|}{0.1 \text{ mA}}$$

Thus we require

$$|V_A| = 2.74 \text{ V}$$

Now, since $|V_A| = |V_A'|L$ we need to use a channel length of

$$L = \frac{2.74}{5} = 0.55 \mu\text{m}$$

which is about three times the minimum channel length. With $|V_A| = 0.5 \text{ V}$ and $|V_{OV}| = 0.3 \text{ V}$,

$$V_{SG4} = 0.5 + 0.3 = 0.8 \text{ V}$$

and thus,

$$V_{G4} = 1.8 - 0.8 = 1.0 \text{ V}$$

To allow for the largest possible signal swing at the output terminal, we shall use the minimum required voltage across Q_4 , namely, $|V_{OV}|$ or 0.3 V. Thus,

$$V_{D4} = 1.8 - 0.3 = 1.5 \text{ V}$$

Since the two transistors are identical and are carrying equal currents,

$$V_{SG3} = V_{SG4} = 0.8 \text{ V}$$

Thus,

$$V_{G3} = 1.5 - 0.8 = +0.7 \text{ V}$$

We note that the maximum voltage allowed at the output terminal of the current source will be constrained by the need to allow a minimum voltage of $|V_{OV}|$ across Q_3 ; thus,

$$v_{D3\max} = 1.5 - 0.3 = +1.2 \text{ V}$$

To determine the required W/L ratios of Q_3 and Q_4 , we use

$$I_D = \frac{1}{2}(\mu_p C_{ox})\left(\frac{W}{L}\right)|V_{OV}|^2\left(1 + \frac{V_{SD}}{|V_A|}\right)$$

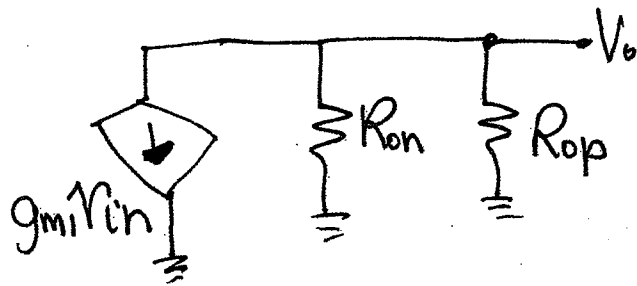
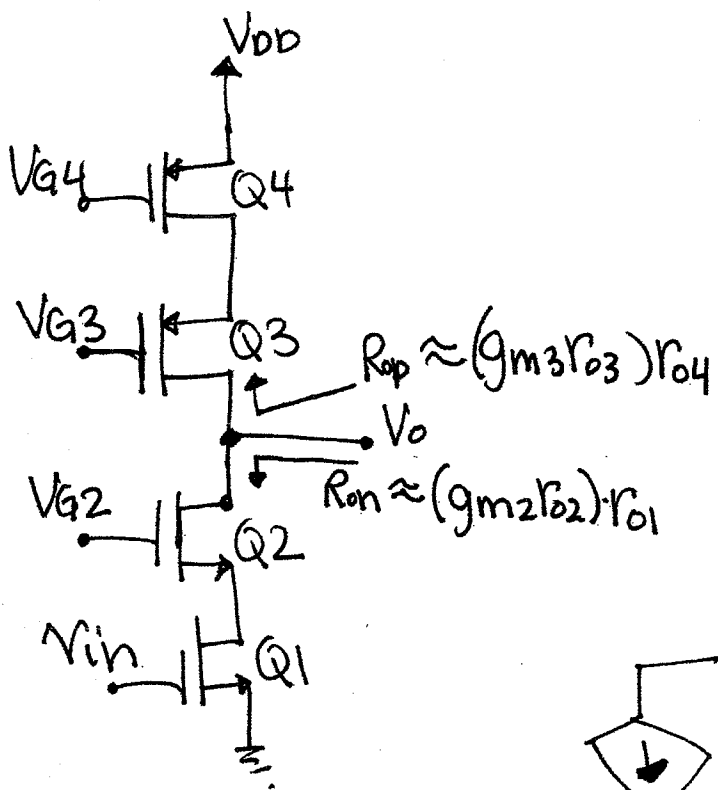
$$100 = \frac{1}{2} \times 90 \times \left(\frac{W}{L}\right) \times 0.3^2 \left(1 + \frac{0.3}{2.74}\right)$$

which yields

$$\frac{W}{L} = 22.3$$

EXERCISES

- D7.4** If in Example 7.4, L of each of Q_3 and Q_4 is halved while W/L is changed to allow I_D and V_{OV} to remain unchanged, find the new values of R_o and W/L . [Hint: In computing the required (W/L) , note that $|V_A|$ has changed.]
Ans. 125 k Ω ; 20.3
- 7.5** Consider the cascode amplifier of Fig. 7.11 with the dc component at the input, $V_I = 0.7 \text{ V}$, $V_{G2} = 1.0 \text{ V}$, $V_{G3} = 0.8 \text{ V}$, $V_{G4} = 1.1 \text{ V}$, and $V_{DD} = 1.8 \text{ V}$. If all devices are matched (i.e., if $k_{n1} = k_{n2} = k_{p3} = k_{p4}$), and have equal $|V_I|$ of 0.5 V, what is the overdrive voltage at which the four transistors are operating? What is the allowable voltage range at the output?
Ans. 0.2 V; 0.5 V to 1.3 V
- 7.6** The cascode amplifier in Fig. 7.11 is operated at a current of 0.2 mA with all devices operating at $|V_{OV}| = 0.2 \text{ V}$. All devices have $|V_A| = 2 \text{ V}$. Find g_m , the output resistance of the amplifier, R_{on} , and the output resistance of the current source, R_{op} . Also find the overall output resistance and the voltage gain realized.
Ans. 2 mA/V; 200 k Ω , 200 k Ω ; 100 k Ω ; -200 V/V



$$\therefore A_v = -g_{m1}(R_{on} \parallel R_{op})$$

$$\text{current} = 0.2 \text{ mA}$$

$$|V_{ov}| = 0.2 \text{ V for all}$$

$$|V_A| = 2 \text{ V}$$

Find g_{m1} , R_{out} , A_v

$$g_{m1} = \frac{2I_D}{V_{ov}} = \frac{2(0.2 \text{ mA})}{0.2} = 2 \text{ mA/V}$$

$$r_o = \frac{|V_A|}{I_D} = \frac{2}{.2 \text{ mA}} = 10 \text{ k}\Omega$$

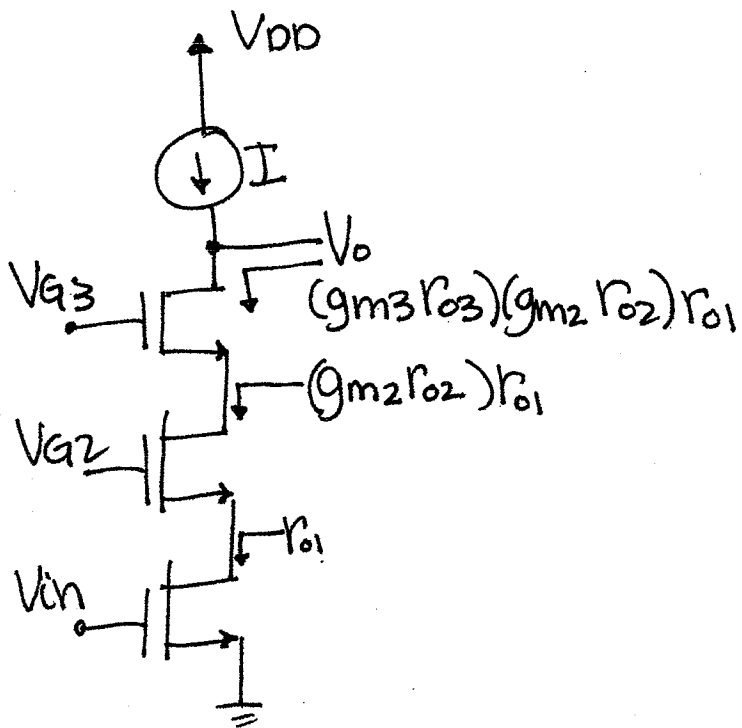
$$R_{on} = (g_{m2} r_{o2}) r_{o1} = 2 \text{ mA} (10 \text{ k})^2 = 200 \text{ k}\Omega$$

$$R_{op} = (g_{m3} r_{o3}) r_{o4} = 200 \text{ k}$$

$$R_{out} = R_{on} \parallel R_{op}$$

$$A_v = -g_{m1} (R_{on} \parallel R_{op}) = -2 \text{ mA} (200 \text{ k} \parallel 200 \text{ k}) = -200 \text{ V}$$

Double Cascoding



Folded Cascode

