

Problem 1 – (30 points)

SOLUTION

Use: ignore r_o , $|V_{BE}|=0.7$, $\beta=99$

$V_I = 20 + 0.01\sin(20t)$

For DC analysis, assume that the capacitors are open

(a) Solve for the DC currents:

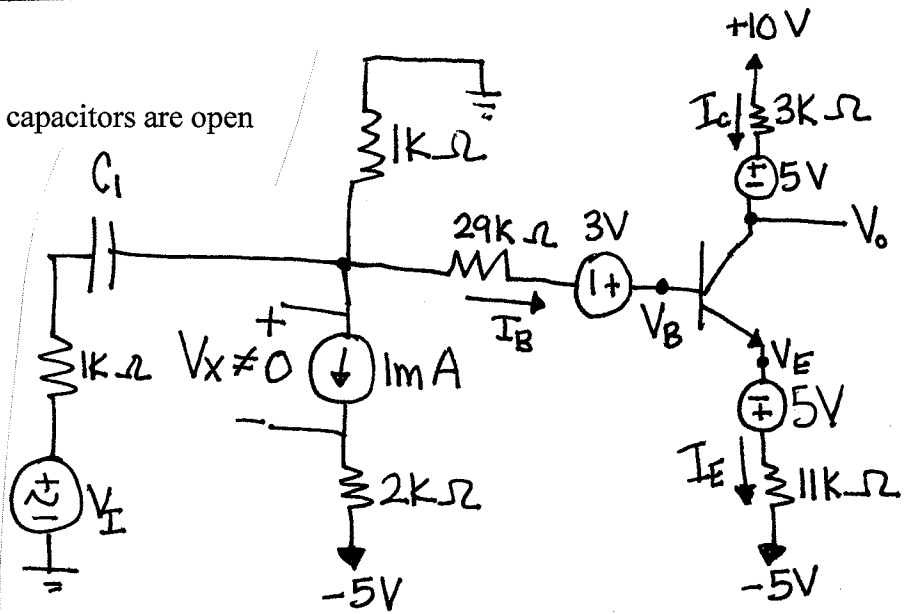
- a. I_B
- b. I_E
- c. I_C

(b) Solve for the DC voltages:

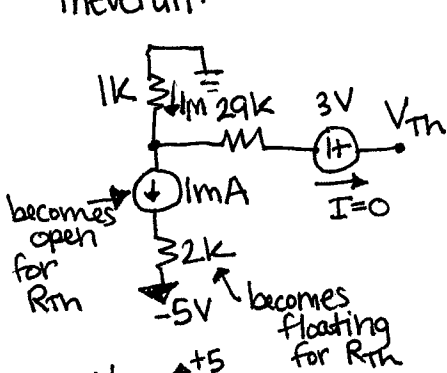
- a. V_B
- b. V_E
- c. V_o

(c) What region of operation is this transistor acting? **Active**

(d) Sketch the total instantaneous waveform observed for V_o if $V_o/V_I = -10V/V$.



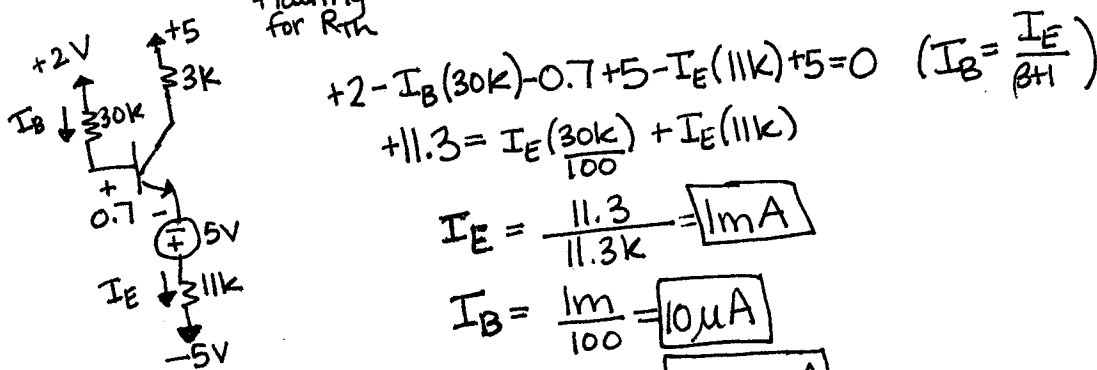
Thevenin:



$$-1k(1m) + 3 - V_{Th} = 0$$

$$V_{Th} = 3 - 1 = \underline{2V}$$

$$R_{Th} = 29k + 1k = \underline{30k}$$



$$+2 - I_B(30k) - 0.7 + 5 - I_E(11k) + 5 = 0 \quad (I_B = \frac{I_E}{\beta})$$

$$+11.3 = I_E \left(\frac{30k}{100} + 11k \right)$$

$$I_E = \frac{11.3}{11.3k} = \underline{1mA}$$

$$I_B = \frac{1m}{100} = \underline{10\mu A}$$

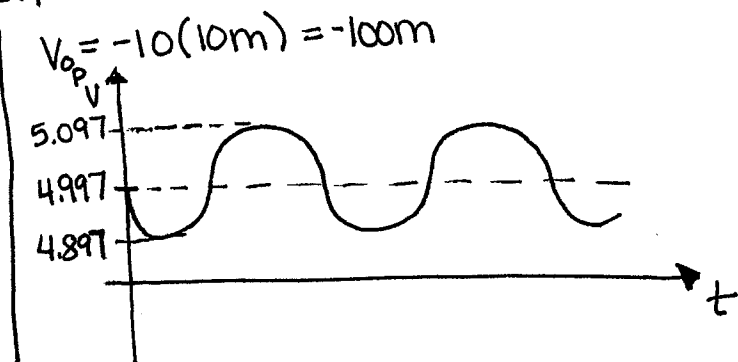
$$I_C = \frac{\beta I_E}{\beta + 1} = \underline{0.990mA}$$

$$V_B = 2 - I_B(30k) = \underline{+1.7V}$$

$$V_E = V_B - 0.7 = \underline{1.0V}$$

$$V_C = 5 - I_C(3k) \approx \underline{2V}$$

$V_C > V_B > V_E \therefore$ **ACTIVE**



Problem 2 – (30 points)

Use: ignore r_o and r_x , $|V_{BE}|=0.7$, $\beta=99$, $V_T=25\text{mV}$
 $V_I = 10 + 0.002\sin(20t)$

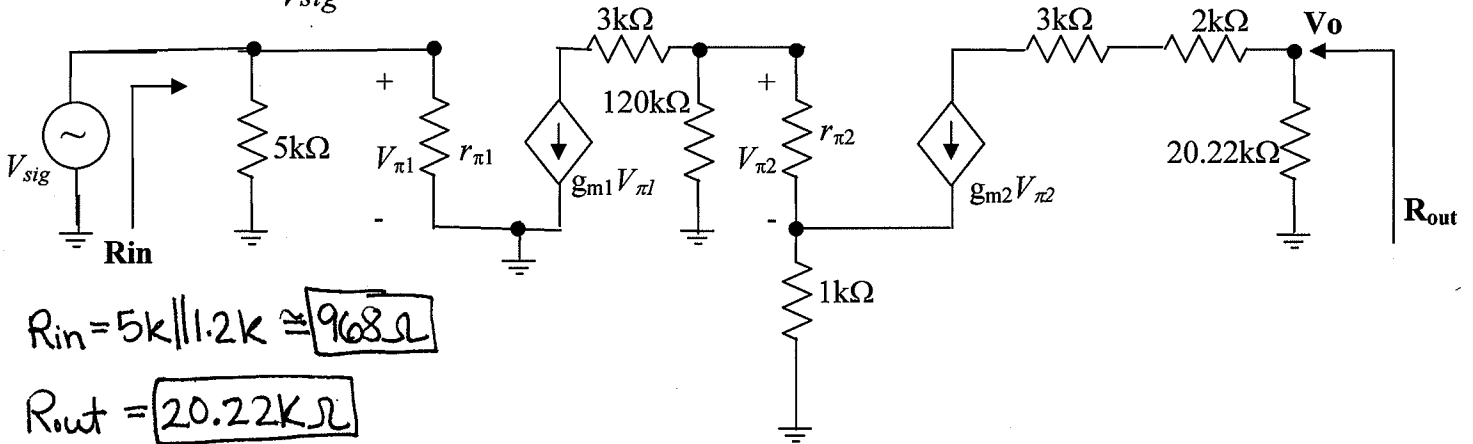
$r_{\pi 1}=1,200$ $g_{m2}=4.95\text{mA/V}$, and $I_{B2}=1.25\mu\text{A}$

$$g_{m1} = \frac{\beta}{r_{\pi}} = \frac{99}{1.2\text{k}} = 82.5\text{m}$$

$$r_{\pi 2} = \frac{\beta}{g_{m2}} = \frac{99}{4.95\text{m}} = 20\text{k}$$

For the following hybrid- π equivalent circuit below, find the following values:

- (a) R_{in} (input resistance –ignore only the input source, V_{sig} and include all other resistors)
- (b) R_{out} (output resistance-include **all** resistors {no load is connected})
- (c) midband gain, $\frac{V_o}{V_{sig}}$



$$R_{in} = 5\text{k} \parallel 1.2\text{k} \approx 968\Omega$$

$$R_{out} = 20.22\text{k}\Omega$$

$$V_o = -g_{m2} V_{\pi 2} \cdot 20.22\text{k}$$

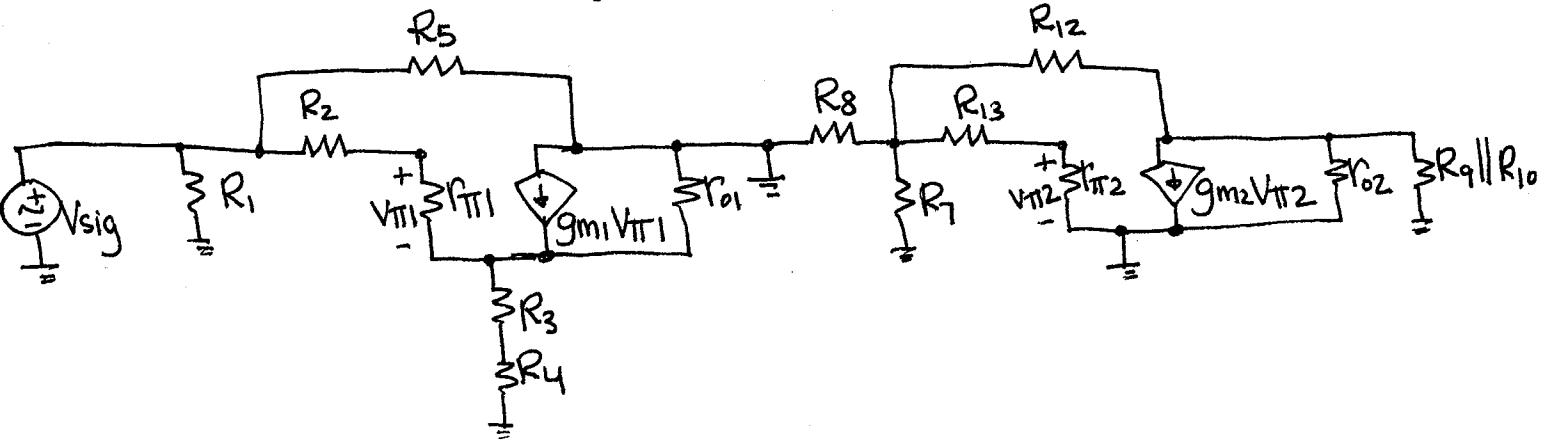
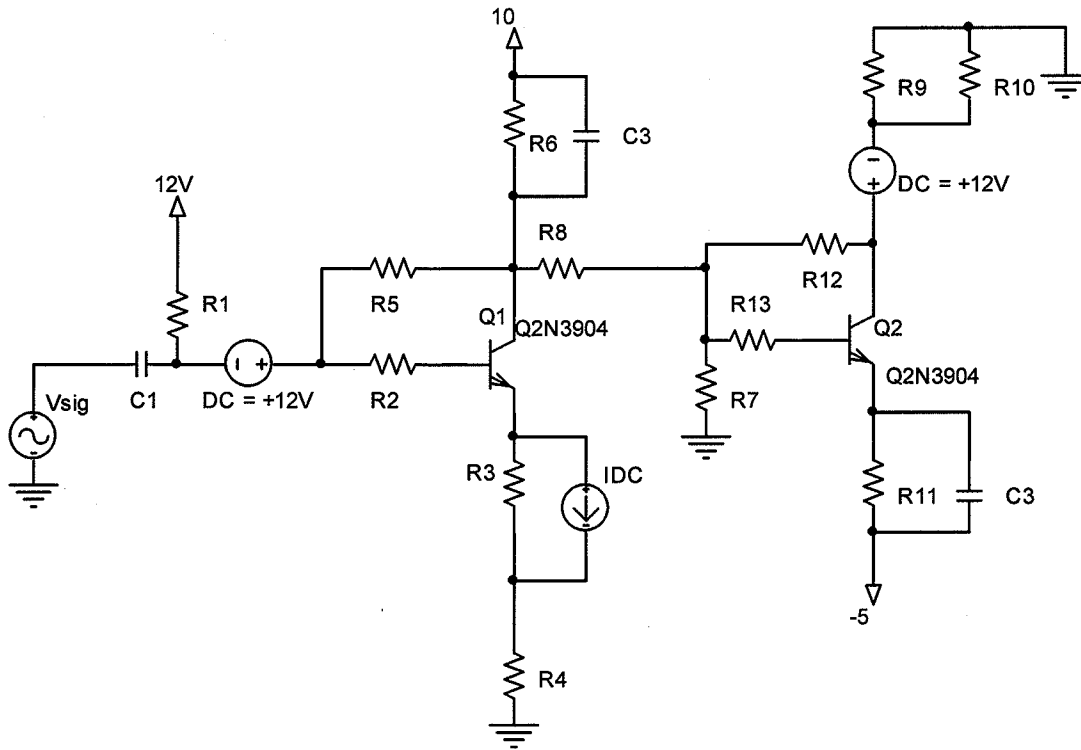
$$V_{\pi 2} = \left[\frac{-g_{m1} V_{\pi 1} (120\text{k})}{(120\text{k} + r_{\pi 2} + 1\text{k}(\beta+1))} \right] \cdot r_{\pi 2} = \frac{-82.5\text{m} V_{\pi 1} (120\text{k}) \cdot 20\text{k}}{240\text{k}}$$

$$V_{\pi 1} = V_{sig}$$

$$\frac{V_o}{V_{sig}} = -4.95\text{m} \cdot 20.22\text{k} \cdot \frac{(-82.5\text{m})(120\text{k}) \cdot 20\text{k}}{(240\text{k})} = 82.6 \frac{\text{V}}{\text{V}}$$

Problem 3 – (15 points)

For the circuit shown below, **draw** the AC small-signal equivalent circuit (use hybrid- π or model T). Make sure that everything is labeled in terms of the transistor number. (e.g. g_{m1} , $v_{\pi 2}$, etc.). **Include r_o** for all transistors. $v_{sig}=0.001\sin(10t)$ AC. Assume that the capacitors act as a short.



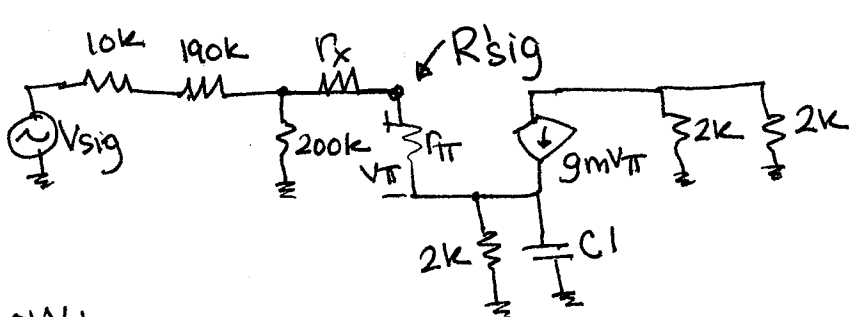
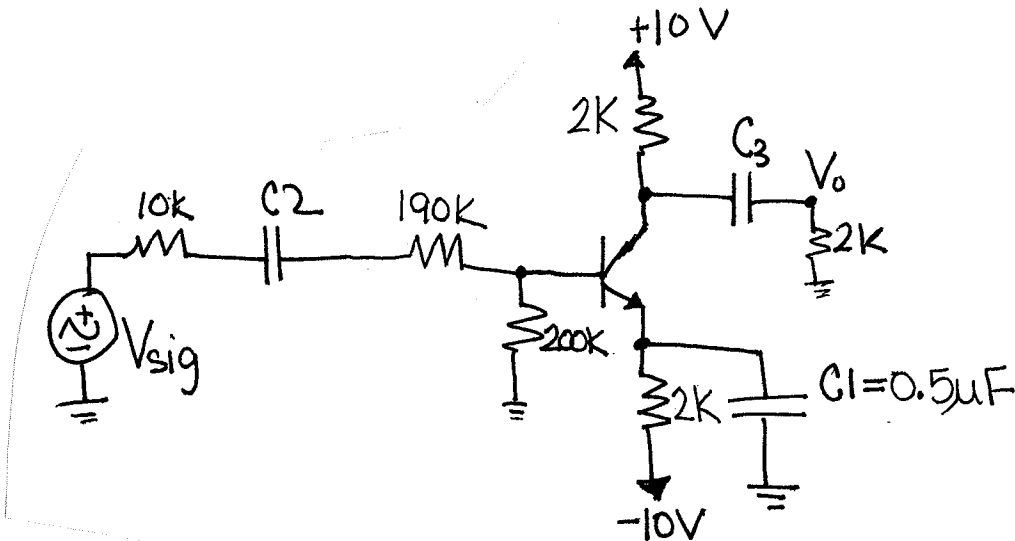
Problem 4 – (15 points)

Use: $g_m=990\mu A/V$, $\beta=99$, $V_T=25mV$. Ignore r_o and use $r_x=50\Omega$. Use $f_T=7.86MHz$ and the attached datasheet to determine the parasitic capacitance.

Assume C_1 yields the highest pole value.

- (a) What frequency pole value does C_1 create? (express the answer in rad/sec.)
 (b) What is the frequency range for this circuit (Hint: Find the high frequency value)?

2k to 625k rad/sec



$$r_{\pi} = \frac{\beta}{g_m} = \frac{99}{990\mu} = 100k$$

LOW:

$$C_1: \frac{1}{C_1 \cdot \text{Req}} = \frac{1}{0.5\mu \cdot [2k \parallel \frac{r_{\pi} + 200k \parallel 200k}{\beta + 1}]} = \boxed{2k \frac{\text{rad}}{\text{sec}}}$$

High:

$$C_{in} = C_{\pi} + C_{\mu}(1 + g_m \cdot R_L') \quad \text{where } C_{\pi} = 8p \Rightarrow C_{\mu} = \frac{g_m}{2\pi f_T} - C_{\pi}$$

$$C_{in} = 8p + 12p(1 + 990\mu \cdot 2k \parallel 2k) \approx 32p$$

$$C_{\mu} = \frac{990\mu}{2\pi \cdot 7.86M} - 8p$$

$$C_{\mu} = 12p$$

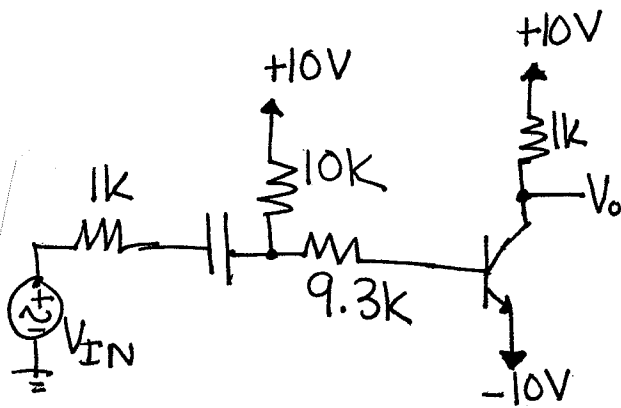
$$\omega_H = \frac{1}{32p (R'_{sig})} \quad \text{where } R'_{sig} = r_{\pi} \parallel (r_x + 100k) \approx 50k$$

$$\omega_H \approx \boxed{625k \frac{\text{rad}}{\text{sec}}}$$

Problem 5 – (10 points)

$|V_{BE}|=0.7$, $\beta=100$, $V_T=25\text{mV}$, ignore r_o , and r_x , $v_{sig}=\{2+0.1\sin(\omega t)\}$ Volts. Assume that the capacitor acts as an open for DC operation and short for AC operation. Assume saturation for the transistor. Use the attached datasheet.

What is β_{forced} ?



$$V_{CESAT} = 0.2 \text{ V}$$

$$V_E = -10$$

$$V_B = -9.3$$

$$\frac{10 + 9.3}{19.3 \text{ k}} = I_B = 1 \text{ mA}$$

$$-10 + 0.2 + I_C (1 \text{ k}) - 10 = 0$$

$$I_C = \frac{+20 - 0.2}{1 \text{ k}} = 19.8 \text{ mA}$$

$$\beta_{\text{forced}} = \frac{I_C}{I_B} = \frac{19.8 \text{ m}}{1 \text{ m}} = \boxed{19.8} < \beta = 100$$

$$\text{check } V_C = 10 - 19.8 \text{ m} (1 \text{ k}) = -9.8 \text{ V}$$

$$-9.8 = V_C < V_B = -9.3 > V_E = -10 \quad \checkmark$$

NPN General Purpose Amplifier

(continued)

Electrical Characteristics

$T_A = 25^\circ\text{C}$ unless otherwise noted

2N3904 / MMBT3904 / PZT3904

Symbol	Parameter	Test Conditions	Min	Max	Units
--------	-----------	-----------------	-----	-----	-------

OFF CHARACTERISTICS

V_{BRICEO}	Collector-Emitter Breakdown Voltage	$I_C = 1.0\text{ mA}, I_E = 0$	40		V
V_{BRICBO}	Collector-Base Breakdown Voltage	$I_C = 10\ \mu\text{A}, I_E = 0$	60		V
V_{BREBEO}	Emitter-Base Breakdown Voltage	$I_E = 10\ \mu\text{A}, I_C = 0$	6.0		V
I_{BL}	Base Cutoff Current	$V_{CE} = 30\text{ V}, V_{EB} = 3\text{ V}$		50	nA
I_{CEX}	Collector Cutoff Current	$V_{CE} = 30\text{ V}, V_{EB} = 3\text{ V}$		50	nA

ON CHARACTERISTICS*

h_{FE}	DC Current Gain	$I_C = 0.1\text{ mA}, V_{CE} = 1.0\text{ V}$	40		
		$I_C = 1.0\text{ mA}, V_{CE} = 1.0\text{ V}$	70		
		$I_C = 10\text{ mA}, V_{CE} = 1.0\text{ V}$	100	300	
		$I_C = 50\text{ mA}, V_{CE} = 1.0\text{ V}$	60		
		$I_C = 100\text{ mA}, V_{CE} = 1.0\text{ V}$	30		
$V_{CE(sat)}$	Collector-Emitter Saturation Voltage	$I_C = 10\text{ mA}, I_B = 1.0\text{ mA}$ $I_C = 50\text{ mA}, I_B = 5.0\text{ mA}$		0.2 0.3	V V
$V_{BE(sat)}$	Base-Emitter Saturation Voltage	$I_C = 10\text{ mA}, I_B = 1.0\text{ mA}$ $I_C = 50\text{ mA}, I_B = 5.0\text{ mA}$	0.65	0.85 0.85	V V

SMALL SIGNAL CHARACTERISTICS

f_T	Current Gain - Bandwidth Product	$I_C = 10\text{ mA}, V_{CE} = 20\text{ V},$ $f = 100\text{ MHz}$	300		MHz
C_{obo}	Output Capacitance	$V_{CB} = 5.0\text{ V}, I_E = 0,$ $f = 1.0\text{ MHz}$		4.0	pF
C_{ibo}	Input Capacitance	$V_{EB} = 0.5\text{ V}, I_C = 0,$ $f = 1.0\text{ MHz}$		8.0	pF
NF	Noise Figure	$I_C = 100\ \mu\text{A}, V_{CE} = 5.0\text{ V},$ $R_B = 1.0\text{ k}\Omega, f = 10\text{ Hz to }15.7\text{ kHz}$		5.0	dB

CTT

E 2280 Midterm #3

Name _____

Scores:

Prob 1 _____ of a possible 30pts

Prob 2 _____ of a possible 30pts

Prob 3 _____ of a possible 15pts

Prob 4 _____ of a possible 15pts

Prob 5 _____ of a possible 10pts

Total _____ of a possible 100 pts