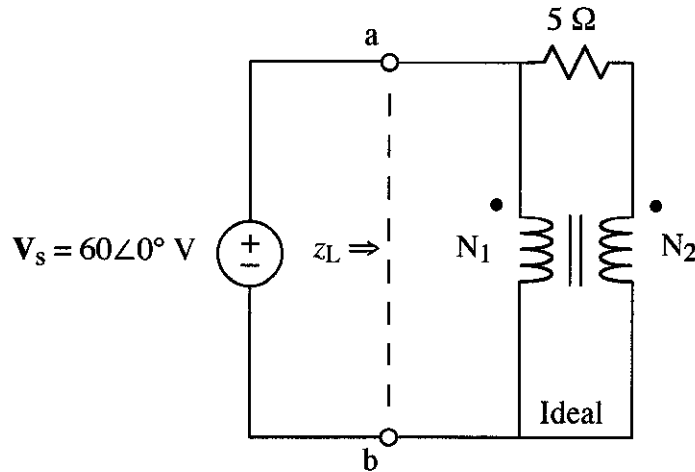
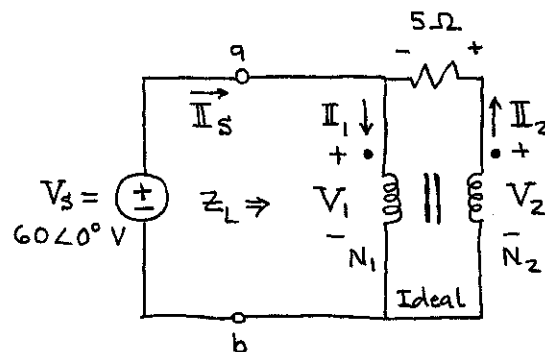


Ex:



Given  $N_1/N_2 = 9$ , calculate the impedance,  $z_L$ , seen by the voltage source in the above transformer circuit.

Sol'n: We begin by labeling the transformer  $V$ 's and  $I$ 's.



Note: The + signs for  $V_1$  and  $V_2$  are at the dots.  $I_1$  flows into the dot, and  $I_2$  flows out of the dot.

Now we use Ohm's law to find  $z_L$  as  $z_L = V_s / I_s$ .

From a current summation at the node to the left of the  $5\Omega$  resistor, we have

$$-I_s + I_1 - I_2 = 0A. \quad (1)$$

Since one node is always redundant for current summations, this is the only current summation equation for the circuit.

We do, however, have that  $I_2$  flows thru the  $5\Omega$  resistor, giving a voltage drop with the polarity indicated on the above circuit diagram.

This  $V$ -drop is part of the voltage loop on the right side which yields the following eq'n:

$$V_1 + I_2 \cdot 5\Omega - V_2 = 0V \quad (2)$$

We also have the voltage loop on the left:

$$V_s - V_1 = 0V \quad \text{or} \quad V_s = V_1 \quad (3)$$

Now we use the ideal transformer eq'ns:

$$\frac{V_1}{V_2} = \frac{N_1}{N_2} \quad \frac{I_1}{I_2} = \frac{N_2}{N_1}$$

Eg'n (2) becomes (also using  $V_1 = V_S$ )

$$I_2 \cdot 5\Omega = V_2 - V_1$$

$$= V_1 \frac{N_2}{N_1} - V_1$$

$$I_2 \cdot 5\Omega = V_1 \left( \frac{N_2}{N_1} - 1 \right)$$

$$I_2 = \frac{V_1 \left( \frac{N_2}{N_1} - 1 \right)}{5\Omega} = \frac{V_S \left( \frac{N_2}{N_1} - 1 \right)}{5\Omega}$$

$$I_2 = \frac{60\angle 0^\circ \text{ V} \cdot \left( \frac{1}{9} - 1 \right)}{5\Omega}$$

$$= 12\angle 0^\circ \text{ A} \cdot \left( -\frac{8}{9} \right)$$

$$I_2 = -\frac{32}{3}\angle 0^\circ \text{ A} = -10.67\angle 0^\circ \text{ A}$$

Eg'n (1) becomes

$$I_S = I_1 - I_2$$

$$= I_2 \frac{N_2}{N_1} - I_2$$

$$= I_2 \left( \frac{N_2}{N_1} - 1 \right)$$

$$= I_2 \left( \frac{1}{9} - 1 \right)$$

$$I_S = I_2 \left( -\frac{8}{9} \right)$$

Now we compute  $z_L = \frac{V_s}{I_s}$ .

$$z_L = \frac{V_s}{I_s} = \frac{V_s}{I_2 \left(-\frac{8}{9}\right)} = \frac{\cancel{V_s}}{\frac{\cancel{V_s} \left(\frac{N_2}{N_1} - 1\right) \left(\frac{N_2}{N_1} - 1\right)}{5 \Omega}} \quad \nearrow \quad -\frac{8}{9}$$

$$z_L = \frac{5 \Omega}{\left(\frac{N_2}{N_1} - 1\right)^2} = \frac{5 \Omega}{\left(-\frac{8}{9}\right)^2}$$

$$z_L = 5 \Omega \cdot \frac{9^2}{8^2} = 5 \Omega \cdot \frac{81}{64}$$

$$z_L = 6.3 \Omega$$