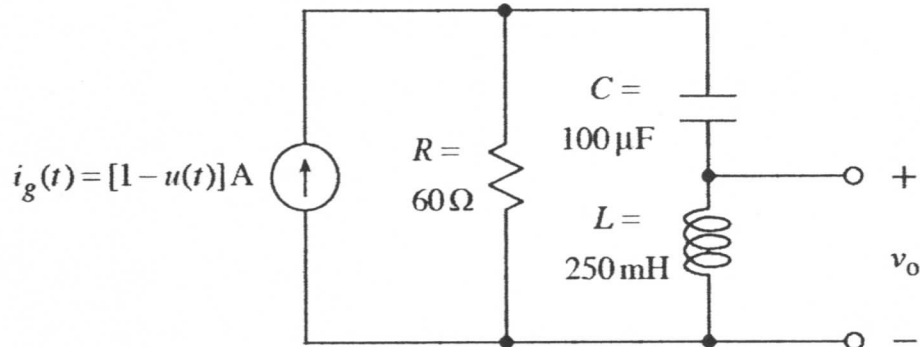


Ex:

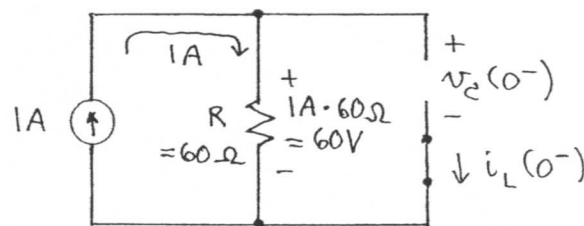


Note: The 1A in the $i_g(t)$ source is always on.

- Write the Laplace transform $I_g(s)$ of $i_g(t)$.
- Write the Laplace transform $V_o(s)$ of $v_o(t)$. Be sure to include the effects of initial conditions, if they are nonzero.
- Write a numerical time-domain expression for $v_o(t)$ where $t \geq 0$.

SOL'N: a) $\mathcal{L} \{ 1 - u(t) \text{ A} \} = \frac{1}{s} - \frac{1}{s} = 0$

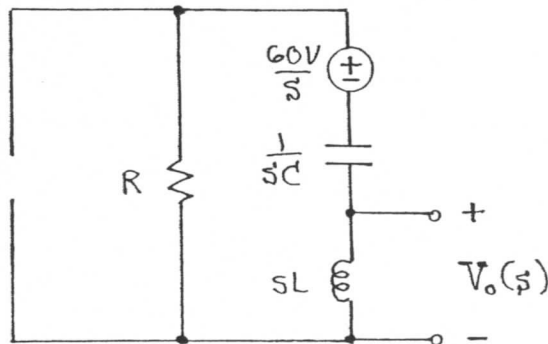
- b) We find initial conditions at $t=0^-$. We have a 1A DC input, and we treat L as a wire and C as an open circuit.



Because of the open-circuit C, $i_L(0^-) = 0 \text{ A}$. All of the 1A flows thru R, creating 60V across R, which appears across C.

$$v_c(0^-) = 60 \text{ V}$$

Using a series V-source, (we could use a parallel I-source instead), we have the following circuit model:



This is a V-divider.

$$V_o(s) = -\frac{60V}{s} \frac{sL}{sL + R + \frac{1}{sC}}$$

or

$$V_o(s) = -60V \frac{\beta\left(\frac{1}{4}\right)}{s^2\left(\frac{1}{4}\right) + 60s + \frac{1}{100\mu}}$$

or

$$V_o(s) = \frac{-60s}{s^2 + 240s + 40k}$$

or

$$V_o(s) = \frac{-60s}{(s + \underset{a}{120})^2 + \underset{w}{160}^2}$$

c) The denominator indicates we will have a decaying cosine and perhaps a decaying sine. Thus, we write the numerator of $V_o(s)$ as follows:

$$-60s = A(s + 120) + B(160)$$

To match the coefficient of s , we must have

$$A = -60.$$

With this value of A , we ^{have} an extra $-60(120)$ that we use B to cancel out.

$$-60(120) + B(160) = 0$$

or

$$B = \frac{60(120)}{160} = 45$$

$$\text{Thus, } V_o(s) = -60 \frac{s+120}{(s+120)^2 + 160^2} + 45 \frac{160}{(s+120)^2 + 160^2}.$$

$$v_o(t) = \left[-60 e^{-120t} \cos(160t) + 45 e^{-120t} \sin(160t) \right] u(t) \text{ V}$$