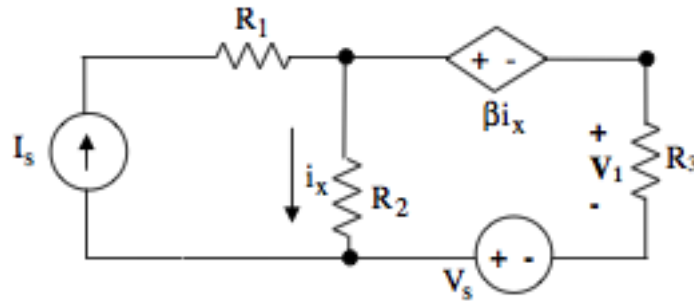
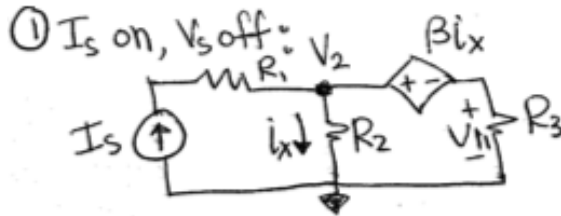


Ex:



Using superposition, derive an expression for v_1 that contains no circuit quantities other than i_s , v_s , R_1 , R_2 , R_3 , and β , where $\beta < 0$.

SOL'N:



node-V:

$$-I_s + \frac{V_2}{R_2} + \frac{V_2 - \beta i_x}{R_3} = 0$$

$$i_x = \frac{V_2}{R_2}$$

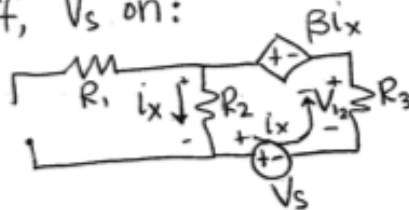
$$-I_s + \frac{V_2}{R_2} + \frac{V_2}{R_3} - \frac{\beta \cdot V_2}{R_3 \cdot R_2} = 0$$

$$V_2 \left(\frac{1}{R_2} + \frac{1}{R_3} - \frac{\beta}{R_2 R_3} \right) = I_s$$

$$V_2 = \frac{I_s (R_2 R_3)}{R_2 + R_3 - \beta} \Rightarrow +V_2 - \beta \left(\frac{V_2}{R_2} \right) - V_1 = 0$$

$$V_1 = \left(1 - \frac{\beta}{R_2} \right) \left(\frac{I_s R_2 R_3}{R_2 + R_3 - \beta} \right)$$

② I_s off, V_s on:



V-loop: $-i_x R_3 + \beta i_x - i_x R_2 - V_s = 0$

$$i_x = \frac{-V_s}{R_2 + R_3 - \beta} \Rightarrow V_2 = -i_x R_3$$

$$\therefore V_1 = \frac{+V_s R_3}{R_2 + R_3 - \beta}$$

$$V_1 = V_1 + V_2 = \left(1 - \frac{\beta}{R_2} \right) \left(\frac{I_s R_2 R_3}{R_2 + R_3 - \beta} \right) + \frac{V_s R_3}{R_2 + R_3 - \beta}$$