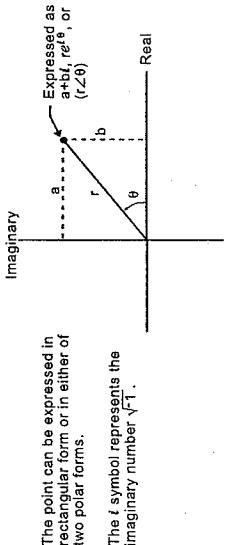


## Entering Complex Numbers

You can enter complex numbers in the point form ( $(a, b)$ ) where  $a$  is the real part and  $b$  is the imaginary part. You can also enter complex numbers in rectangular form  $a+bi$ .

### Overview of Complex Numbers

A complex number has real and imaginary components that identify a point in the complex plane. These components are measured along the real and imaginary axes, which are similar to the  $x$  and  $y$  axes in the real plane.



As shown below, the form that you can enter depends on the current Angle mode.

You can use the form:		When the Angle mode setting is:
a+bi		Radian or Degree
re <sup>iθ</sup>		Radian only (In Degree angle mode, this form causes a Domain error.)
(r∠θ)		Radian or Degree

Use the following methods to enter a complex number.

To enter the:	Do this:
Rectangular form	Substitute the applicable values or variable names for $a$ and $b$ . $a \boxed{+} b \boxed{\times} [i]$
	For example: $\frac{2+3i}{2-3i}$

**Note:** To get the  $i$  symbol, press  $\boxed{\text{2nd}}$  [ $i$ ], do not simply type an alphabetic  $i$ .

$\frac{2+3i}{2-3i}$	$2+3i$
<small>2nd MATH</small>	<small>Frac</small>

**Important:** Do not use the  $re^{i\theta}$  polar form in Degree angle mode. It will cause a Domain error.

**Note:** To get the  $e$  symbol, press: TI-89:  $\boxed{[e^x]}$ , TI-92 Plus:  $\boxed{[e^x]}$   
Do not simply type an alphabetic  $e$ .

**Tip:** To get the  $\angle$  symbol, press  $\boxed{\text{2nd}} \boxed{[\angle]}$ .

**Tip:** To enter  $\theta$  in degrees for  $r\angle\theta$ , you can type a  $^\circ$  symbol (such as  $45^\circ$ ). To get the  $^\circ$  symbol, press  $\boxed{\text{2nd}} \boxed{[^\circ]}$ . You should not use degrees for  $re^{i\theta}$ .

**To enter the:** **Do this:**  
Polar form  
 $re^{i\theta}$   
– or –  
 $(r\angle\theta)$

Substitute the applicable values or variable names for  $r$  and  $\theta$ , where  $\theta$  is interpreted according to the Angle mode setting.

**TI-89:**  
 $\boxed{\text{2nd}} \boxed{[R]} \boxed{[e^x]} \boxed{\times} [i] \boxed{+} [\theta] \boxed{\times} [\theta]$   
– or –  
 $\boxed{\text{2nd}} \boxed{[\theta]}$

**TI-92 Plus:**  
 $R \boxed{[2nd]} \boxed{[e^x]} \boxed{\times} [i] \boxed{+} [\theta] \boxed{\times} [\theta]$

For example:

$$\begin{aligned} & \frac{1}{4} \pi \\ & = 2 \cdot e^{i \frac{\pi}{4}} \\ & = \left[ 2 \angle \frac{\pi}{4} \right] \end{aligned}$$

$\boxed{\text{2nd}} \boxed{[\pi/4]}$   $\boxed{\text{2nd}} \boxed{[e^x]}$   $\boxed{[i]}$   $\boxed{+}$   $\boxed{[\theta]}$   $\boxed{\times}$   $\boxed{[\theta]}$

Results are shown in rectangular form, but you can select polar form.

**If Complex Format is:** **The TI-89 / TI-92 Plus:**  
REAL Will not display complex results unless you:  
• Enter a complex number.

You can enter a complex number at any time, regardless of the Complex Format mode setting. However, the mode setting determines how results are displayed.

**If Complex Format is:** **The TI-89 / TI-92 Plus:**  
RATIONAL Will not display complex results unless you:  
• Use a complex function such as cFactor(), cSolve(), or cZero().  
• If complex results are displayed, they will be shown in either a+bi or re<sup>iθ</sup> form.

**POLAR** Displays complex results as a+bi.  
Displays complex results as:  
• re<sup>iθ</sup> if the Angle mode = Radian  
– or –  
• (r∠θ) if the Angle mode = Degree

## Using Complex Variables in Symbolic Calculations

**Note:** For best results in calculations such as **cSolve()** and **cZeros()**, use Method 1.

Regardless of the Complex Format mode setting, undefined variables are treated as real numbers. To perform complex symbolic analysis, you can use either of the following methods to set up a complex variable.

**Method 1:** Use an underscore  $_$  (TI-89:  $\boxed{\diamond}$   $\boxed{[}_-$  TI-92 Plus:  $\boxed{2nd}$   $\boxed{[}_-$ ) as the last character in the variable name to designate a complex variable. For example:

$z_$  is treated as a complex variable (unless  $z$  already exists, in which case it retains its existing data type).

```

■ imag(z)          0
■ imag(z_)        imag(z_)
■ imag(z_)        imag(z_)
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```

**Method 2:** Define a complex variable. For example:

$x+yi \rightarrow z$

Then  $z$  is treated as a complex variable.

```

■ imag(z)          0
■ x + y · i → z  x + y · i
■ imag(z)          y
■ imag(z)          y
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```

## Complex Numbers and Degree Mode

**Note:** If you use Degree angle mode, you must make polar entries in the form  $(r\angle\theta)$ . In Degree angle mode, an  $re^{i\theta}$  entry causes an error.

Radian angle mode is recommended for complex number calculations. Internally, the TI-89 / TI-92 Plus converts all entered trig values to radians, but it does not convert values for exponential, logarithmic, or hyperbolic functions.

In Degree angle mode, complex identities such as  $e^{(i\theta)} = \cos(\theta) + i \sin(\theta)$  are not generally true because the values for  $\cos$  and  $\sin$  are converted to radians, while those for  $e^()$  are not. For example,  $e^{(i45)} = \cos(45) + i \sin(45)$  is treated internally as  $e^{(i45)} = \cos(\pi/4) + i \sin(\pi/4)$ . Complex identities are always true in Radian angle mode.