

## Entering and Using Complex Numbers

### Complex-Number Modes

The TI-83 displays complex numbers in rectangular form and polar form. To select a complex-number mode, press **[MODE]**, and then select either of the two modes.

- $a+bi$  (rectangular-complex mode)
- $re^{\theta i}$  (polar-complex mode)



On the TI-83, complex numbers can be stored to variables. Also, complex numbers are valid list elements.

In Real mode, complex-number results return an error, unless you entered a complex number as input. For example, in Real mode  $\ln(-1)$  returns an error; in  $a+bi$  mode  $\ln(-1)$  returns an answer.

**Real mode**      **a+bi mode**

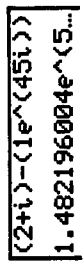
$\ln(-1)$	↓	$\ln(-1)$
ERR:NONREAL ANS Quit 2:Goto	↓	$\ln(-1)$ 3.141592654i

### Entering Complex Numbers

Complex numbers are stored in rectangular form, but you can enter a complex number in rectangular form or polar form, regardless of the mode setting. The components of complex numbers can be real numbers or expressions that evaluate to real numbers; expressions are evaluated when the command is executed.

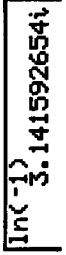
### Interpreting Complex Results

Complex numbers in results, including list elements, are displayed in either rectangular or polar form, as specified by the mode setting or by a display conversion instruction (page 2-19). In the example below,  $re^{\theta i}$  and Degree modes are set.



### Rectangular-Complex Mode

Rectangular-complex mode recognizes and displays a complex number in the form  $a+bi$ , where  $a$  is the real component,  $b$  is the imaginary component, and  $i$  is a constant equal to  $\sqrt{-1}$ .



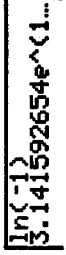
To enter a complex number in rectangular form, enter the value of  $a$  (real component), press **[+]** or **[-]**, enter the value of  $b$  (imaginary component), and press **[2nd]** **[i]** (constant).

real component(+ or -)imaginary component*i*



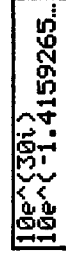
### Polar-Complex Mode

Polar-complex mode recognizes and displays a complex number in the form  $re^{\theta i}$ , where  $r$  is the magnitude,  $e$  is the base of the natural log,  $\theta$  is the angle, and  $i$  is a constant equal to  $\sqrt{-1}$ .



To enter a complex number in polar form, enter the value of  $r$  (magnitude), press **[2nd]** **[e^x]** (exponential function), enter the value of  $\theta$  (angle), press **[2nd]** **[i]** (constant), and then press **[=]**.

magnitudee^(angle*i*)



# MATH CPX (Complex) Operations

## MATH CPX Menu

To display the MATH CPX menu, press **MATH** **D** **D**.

MATH NUM	PRB	PRB
1: conj(		Returns the complex conjugate
2: real(		Returns the real part
3: imag(		Returns the imaginary part
4: angle(		Returns the polar angle
5: abs(		Returns the magnitude (modulus)
6: ▶Rect		Displays the result in rectangular form
7: ▶Polar		Displays the result in polar form

## conj(

conj( (conjugate) returns the complex conjugate of a complex number or list of complex numbers.

conj( $a+bi$ ) returns  $a-bi$  in  $a+bi$  mode.

conj( $re^{i\theta}$ ) returns  $re^{-i\theta}$  in  $re^{i\theta}$  mode.

conj(3+4i) 3-4i  
 $\left[ \begin{array}{l} \text{conj}(3e^{i4}) \\ 3e^{-i2.283185307} \dots \end{array} \right]$

## real(

real( (real part) returns the real part of a complex number or list of complex numbers.

real( $a+bi$ ) returns  $a$ .

real( $re^{i\theta}$ ) returns  $r \cos(\theta)$ .

real(3+4i) 3  
 $\left[ \begin{array}{l} \text{real}(3e^{i4}) \\ -1.960930863 \end{array} \right]$

## imag(

imag( (imaginary part) returns the imaginary (non-real) part of a complex number or list of complex numbers.

imag( $a+bi$ ) returns  $b$ .

imag( $re^{i\theta}$ ) returns  $r \sin(\theta)$ .

imag(3+4i) 4  
 $\left[ \begin{array}{l} \text{imag}(3e^{i4}) \\ -2.270407486 \end{array} \right]$

## angle(

angle( returns the polar angle of a complex number or list of complex numbers, calculated as  $\tan^{-1}(b/a)$ , where  $b$  is the imaginary part and  $a$  is the real part. The calculation is adjusted by  $+\pi$  in the second quadrant or  $-\pi$  in the third quadrant.

angle( $a+bi$ ) returns  $\tan^{-1}(b/a)$ .

angle( $re^{i\theta}$ ) returns  $\theta$ , where  $-\pi < \theta < \pi$ .

angle(3+4i) .927295218  
 $\left[ \begin{array}{l} \text{angle}(3e^{i4}) \\ -2.283185307 \end{array} \right]$

## abs(

abs( (absolute value) returns the magnitude (modulus),  $\sqrt{\text{real}^2 + \text{imag}^2}$ , of a complex number or list of complex numbers.

abs( $a+bi$ ) returns  $\sqrt{a^2+b^2}$ .

abs( $re^{i\theta}$ ) returns  $r$  (magnitude).

abs(3+4i) 5  
 $\left[ \begin{array}{l} \text{abs}(3e^{i4}) \\ 5 \end{array} \right]$

## ▶Rect

▶Rect (display as rectangular) displays a complex result in rectangular form. It is valid only at the end of an expression. It is not valid if the result is real.

complex result ▶Rect returns  $a+bi$ .

$\left[ \begin{array}{l} (-2) \text{▶Rect} \\ 1.414213562i \end{array} \right]$

## ▶Polar

▶Polar (display as polar) displays a complex result in polar form. It is valid only at the end of an expression. It is not valid if the result is real.

complex result ▶Polar returns  $re^{i\theta}$ .

$\left[ \begin{array}{l} (-2) \text{▶Polar} \\ 1.414213562e^{i1} \dots \end{array} \right]$