Final Exam Useful Information

This is the only reference material allowed at the final. Bring this page to the Final. You **may add** whatever you want to this page.

$C = \frac{Q}{V}$ $\quad$ $\text{farad} = \frac{\text{coul}}{\text{volt}} = \frac{\text{amp}\cdot\text{sec}}{\text{volt}}$ $\quad$ $v_C = \frac{1}{C}\cdot\int_{-\infty}^{t} i_C\,dt = \frac{1}{C}\cdot\int_{0}^{t} i_C\,dt + v_C(0)$ (initial voltage) $\quad$ $i_C = C\cdot\frac{d}{dt}v_C$

parallel: $C_{eq} = C_1 + C_2 + C_3 + \ldots$ $\quad$ **series:** $C_{eq} = \frac{1}{\frac{1}{C_1}+\frac{1}{C_2}+\frac{1}{C_3}+\ldots}$

$W_C = \frac{1}{2}\cdot C\cdot {V_C}^2$ $\quad$ Capacitor voltage **cannot** change instantaneously

$\text{henry} = \frac{\text{volt}\cdot\text{sec}}{\text{amp}}$ $\quad$ $i_L = \frac{1}{L}\cdot\int_{-\infty}^{t} v_L\,dt = \frac{1}{L}\cdot\int_{0}^{t} v_L\,dt + i_L(0)$ (initial current) $\quad$ $v_L = L\cdot\frac{d}{dt}i_L$

$W_L = \frac{1}{2}\cdot L\cdot {I_L}^2$ $\quad$ Inductor current **cannot** change instantaneously

Resonance: $\omega_o = \frac{1}{\sqrt{L_{eq}\cdot C_{eq}}}$

For all first order transients: $x(t) = x(\infty) + (x(0) - x(\infty))\cdot e^{-\frac{t}{\tau}}$ $\quad$ $\tau = R_{Th}\cdot C$ OR $\frac{L}{R_{Th}}$

Steady-state sinusoidal AC Impedances: $\mathbf{Z}_C = \frac{1}{j\cdot\omega\cdot C} = \frac{-j}{\omega\cdot C}$ $\quad$ $\mathbf{Z}_L = j\cdot\omega\cdot L$ $\quad$ $\omega = 2\cdot\pi\cdot f$

Bode Plots $\quad$ Poles come from denominator of transfer function, zeroes from numerator. $\quad$ Slopes: -20, 0, or +20 dB/decade

dB is $20\cdot\log_{10}(|\mathbf{H}(\omega)|)$

Second order transients
LaPlace Impedances: $\mathbf{Z}_C = \frac{1}{C\cdot s}$ $\quad$ $\mathbf{Z}_L = L\cdot s$ $\quad$ $\mathbf{H}(s) = \frac{\text{output}}{\text{input}}$

Overdamped $\quad$ $b^2 - 4\cdot k > 0$ $\quad$ s_1 and s_2 are real and negative

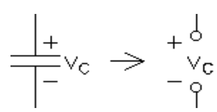
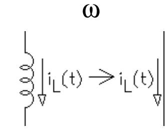
$X(t) = X(\infty) + B\cdot e^{s_1\cdot t} + D\cdot e^{s_2\cdot t}$ $\quad$ $X(0) = X(\infty) + B + D$ $\quad$ $\frac{d}{dt}X(0) = B\cdot s_1 + D\cdot s_2$

Critically damped $\quad$ $b^2 - 4\cdot k = 0$ $\quad$ $s_1 = s_2 = -\frac{b}{2} = s$ $\quad$ s_1 and s_2 are real, equal and negative

$X(t) = X(\infty) + B\cdot e^{s\cdot t} + D\cdot t\cdot e^{s\cdot t}$ $\quad$ $B = X(0) - X(\infty)$ $\quad$ $D = \frac{d}{dt}X(0) - B\cdot s$ $\quad$ | $\frac{d}{dt}i_L(0) = \frac{v_L(0)}{L}$

Underdamped $\quad$ $b^2 - 4\cdot k < 0$ $\quad$ $s = \alpha \pm j\omega$ $\quad$ complex s_1 and s_2

$X(t) = X(\infty) + e^{\alpha\cdot t}\cdot(B\cdot\cos(\omega\cdot t) + D\cdot\sin(\omega\cdot t))$ $\quad$ $B = X(0) - X(\infty)$ $\quad$ $D = \frac{\frac{d}{dt}X(0) - B\cdot\alpha}{\omega}$ $\quad$ | $\frac{d}{dt}v_C(0) = \frac{i_C(0)}{C}$

Final Conditions, or "after a long time"  Replace capacitors with opens  Replace inductors with wires

AC Power

$V_{RMS} = \frac{V_p}{\sqrt{2}}$ $\quad$ All voltages and current below are RMS $\quad$ $pf = \cos(\theta) = \frac{P}{|\mathbf{S}|}$

$P = (|\mathbf{I_R}|)^2\cdot R = \frac{(|\mathbf{V_R}|)^2}{R}$ for resistors or $P = |\mathbf{V}|\cdot|\mathbf{I}|\cdot\cos(\theta) = |\mathbf{S}|\cdot pf$ $= (|\mathbf{I}|)^2\cdot|\mathbf{Z}|\cdot\underbrace{\cos(\theta)}_{pf} = \frac{(|\mathbf{V}|)^2}{|\mathbf{Z}|}\cdot\underbrace{\cos(\theta)}_{pf}$

capacitors -> - Q $\quad$ $Q_C = (|\mathbf{I_C}|)^2\cdot X_C = \frac{(|\mathbf{V_C}|)^2}{X_C}$ $\quad$ $X_C = -\frac{1}{\omega\cdot C}$ and is a negative number causes leading pf

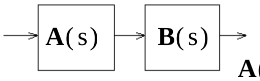
inductors -> + Q $\quad$ $Q_L = (|\mathbf{I_L}|)^2\cdot X_L = \frac{(|\mathbf{V_L}|)^2}{X_L}$ $\quad$ $X_L = \omega\cdot L$ and is a positive number causes lagging pf

or Q = Reactive "power" = $|\mathbf{V}|\cdot|\mathbf{I}|\cdot\sin(\theta)$ $\quad$ units: VAR, kVAR, etc. "volt-amp-reactive"

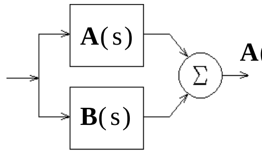
$\mathbf{S}$ = Complex "power" = $\mathbf{V}\cdot\overline{\mathbf{I}}$ (complex congugate) $= P + jQ = |\mathbf{V}|\,|\mathbf{I}|\,\underline{/\theta} = |\mathbf{S}|\,\underline{/\theta}$ $\quad$ units: VA, kVA, etc. "volt-amp"

S = Apparent "power" = $|\mathbf{S}| = |\mathbf{V}|\cdot|\mathbf{I}| = \sqrt{P^2 + Q^2}$ $\quad$ **Transformer:** $\frac{N_1}{N_2} = \frac{V_1}{V_2} = \frac{I_2}{I_1}$ $\quad$ $\mathbf{Z}_{eq} = \left(\frac{N_1}{N_2}\right)^2\cdot\mathbf{Z}_2$

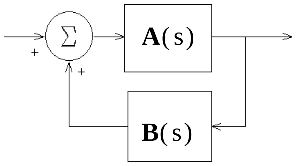
System Block Diagrams



$\mathbf{A}(s)\cdot\mathbf{B}(s)$



$\mathbf{A}(s)+\mathbf{B}(s)$

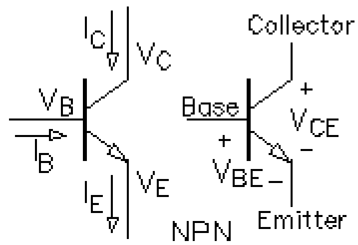


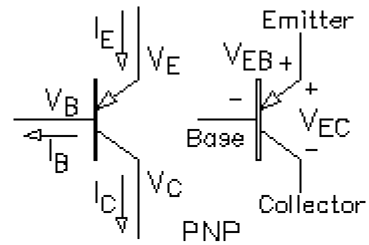
Standard feedback loop transfer function

$$\frac{\mathbf{A}(s)}{1-\mathbf{A}(s)\cdot\mathbf{B}(s)}$$

Transistors

PNP





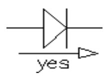
$v_{BE} = v_B - v_E$

$v_{CE} = v_C - v_E$

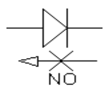
Replace v_{BE} with v_{EB} and v_{CE} with v_{EC} in equations below

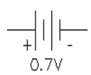
Diodes

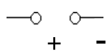
conducting not conducting

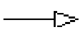


or





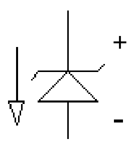




current

$V_d < 0.7V$ Check

LEDs: 2V



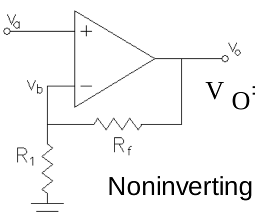
V_Z = zener voltage

Modes or regions of operation

(v_{BE} and v_{CE} are approximate)

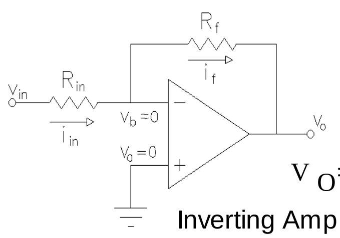
Cutoff (off)	Active (partially on)	Saturation (fully on)
$v_{BE} < 0.7V$	$v_{BE} \simeq 0.7V$	$v_{BE} \simeq 0.7V$
$i_B = 0$	$i_B > 0$	$i_B > 0$
	$v_{CE} \geq 0.2V$	$v_{CE} \simeq 0.2V$
$i_C = 0$	$i_C = \beta i_B = \alpha i_E$ $\alpha \simeq 1$ controlled by the transistor	$i_C < \beta i_B$ limited by something outside of the transistor

Op-amps



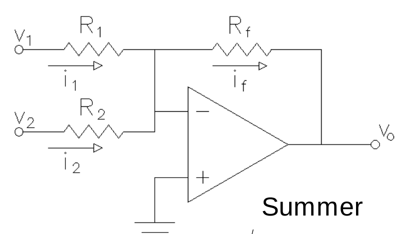
$$V_O = \left(\frac{R_f}{R_1}+1\right)\cdot Va$$

Noninverting Amp



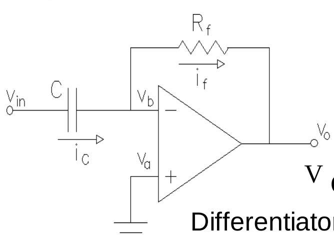
$$V_O = -\frac{R_f}{R_{in}}\cdot V_{in}$$

Inverting Amp



Summer

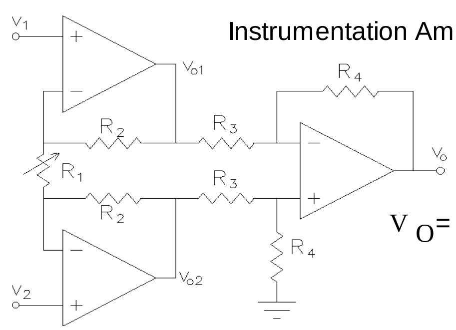
$$V_O = -\left(\frac{R_f}{R_1}\cdot V_1+\frac{R_f}{R_2}\cdot V_2\right)$$



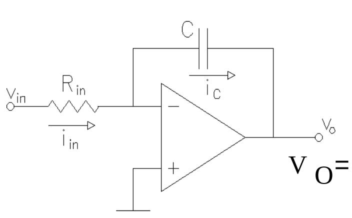
$$V_O = -R_f\cdot C\cdot\frac{d}{dt}V_{in}$$

Differentiator

Instrumentation Amp

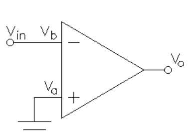


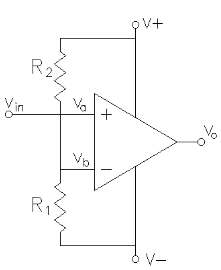
$$V_O = \left(1+\frac{2\cdot R_2}{R_1}\right)\cdot\frac{R_4}{R_3}\cdot\left(V_2-V_1\right)$$

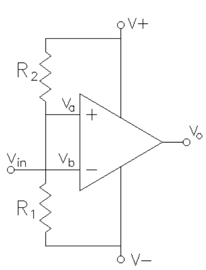


$$V_O = -\frac{1}{R_{in}\cdot C}\cdot\left(\int V_{in}\,dt\right)$$

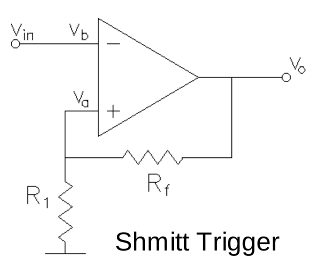
Integrator



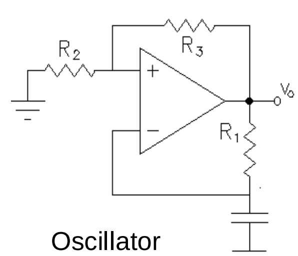




Comparators



Shmitt Trigger



Oscillator