162 Chapter 3: Transmission Lines and Waveguides

Formulas for Effective Dielectric Constant, Characteristic Impedance, and Attenuation

The effective dielectric constant of a microstrip line is given approximately by

$$\epsilon_e = \frac{\epsilon_r + 1}{2} + \frac{\epsilon_r - 1}{2} \quad \frac{1}{\sqrt{1 + 12d/W}}.$$
 3.195

The effective dielectric constant can be interpreted as the dielectric constant of a homogeneous medium that replaces the air and dielectric regions of the microstrip, as shown in Figure 3.26. The phase velocity and propagation constant are then given by (3.193) and (3.194).

Given the dimensions of the microstrip line, the characteristic impedance can be calculated as

$$Z_{0} = \begin{cases} \frac{60}{\sqrt{\epsilon_{e}}} \ln \left(\frac{8d}{W} + \frac{W}{4d} \right) & \text{for } W/d \leq 1 \\ \frac{120\pi}{\sqrt{\epsilon_{e}} \left[W/d + 1.393 + 0.667 \ln \left(W/d + 1.444 \right) \right]} & \text{for } W/d \geq 1. \end{cases}$$

For a given characteristic impedance Z_0 and dielectric constant ϵ_r , the W/d ratio can be found as

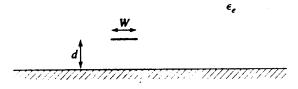
$$\frac{W}{d} = \begin{cases}
\frac{8e^{A}}{e^{2A} - 2} & \text{for } W/d < 2 \\
\frac{2}{\pi} \left[B - 1 - \ln(2B - 1) + \frac{\epsilon_{r} - 1}{2\epsilon_{r}} \left\{ \ln(B - 1) + 0.39 - \frac{0.61}{\epsilon_{r}} \right\} \right] & \text{for } W/d > 2, \\
3.197$$

where

FIGURE 3.26

$$A = \frac{Z_0}{60} \sqrt{\frac{\epsilon_r + 1}{2}} + \frac{\epsilon_r - 1}{\epsilon_r + 1} \left(0.23 + \frac{0.11}{\epsilon_r} \right)$$

$$B = \frac{377\pi}{2Z_0\sqrt{\epsilon_r}}$$



Equivalent geometry of quasi-TEM microstrip line, where the dielectric slab of thickness d and relative permittivity ϵ_r has been replaced with a homogeneous medium of effective relative permittivity, ϵ_r .