

Good

Name: Jason Wayment TA:

100
100

11/11/07

Partner(s): _____

	Pts	Grd
Lab 6 Biot-Savart		
Prelab		
Sketch and Define the System	10	10
Write and sketch the vectors R_s , R_p , R	10	10
Define the source	5	5
Write the integral to find H	15	15
Integrate and Fill in Chart	15	15
Write a program to find H and include with lab	20	20
Plot the magnetic field along y axis	15	15
Conclusion	10	10
Total	100	100

How much time was spent on this lab?

Comments:

Given a wire (thin) antenna oriented along the z-axis from $z_s = -L$ to L and a current distribution:

$$\vec{R}_s = x_s \hat{x} + y_s \hat{y} + z_s \hat{z}$$

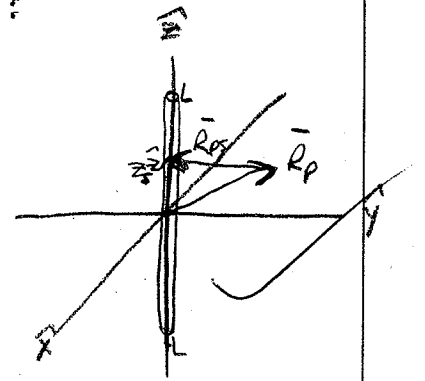
$$= z_s \hat{z} \quad \text{for thin (assume } r=0 \text{) wire}$$

$$\vec{R}_p = x_p \hat{x} + y_p \hat{y} + z_p \hat{z}$$

$$\vec{R}_{ps} = x_p \hat{x} + y_p \hat{y} + (z_p - z_s) \hat{z}$$

$$\hat{R}_{ps} = \frac{\vec{R}_{ps}}{\sqrt{x_p^2 + y_p^2 + (z_p - z_s)^2}}$$

$$|\vec{R}_{ps}| = \sqrt{x_p^2 + y_p^2 + (z_p - z_s)^2}$$



source = $\vec{I} dl$

$$H = \int \frac{d\vec{I} \times \vec{R}}{4\pi R^2} = \int_{-L}^L \frac{L I x_p \hat{y} dz_s}{4\pi (x_p^2 + y_p^2 + (z_p - z_s)^2)^{3/2}}$$

$$- \int_{-L}^L \frac{L I y_p \hat{x} dz_s}{4\pi (x_p^2 + y_p^2 + (z_p - z_s)^2)^{3/2}}$$

\hat{x}	$-\hat{y}$	\hat{z}
0	0	I
x_p	y_p	$z_p - z_s$

$$= -I y_p \hat{x} + I x_p \hat{y}$$

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Total	100	

How much time was spent on this lab?

3 hours

Comments:

Lab 5 Biot-Savart

$$A = \frac{b-a}{2h} + \frac{1}{2}$$

$$\int_a^b f(x) = h \left[\frac{f(a)}{2} + \frac{f(b)}{2} + \sum_{j=1}^{n-1} f(a+jh) \right] + \text{error} (h^3 f''')$$

$$A = \int_1^5 F(z) dz \quad \text{where } F(z) = z, z^2, z^3$$

F(z)	Matlab	Real	Error
z	12	12	0
z ²	41.334	124/3 = 41.33	-6.666E-5
z ³	156.06	625/4 = 156.25	0.19

F(z)	h size	Matlab	Error
z ³	1	162	5.75
z ³	0.01	156.0002	-0.2495
z ³	0.0001	156.0000	-0.25

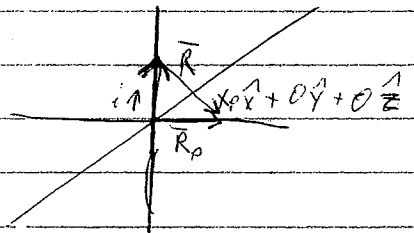
$$I = \cos(z) \hat{z}$$

$$R_s = z_s \hat{z}$$

$$R_p = x_p \hat{x} + y_p \hat{y} + z_p \hat{z}$$

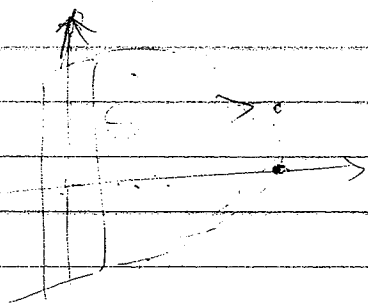
$$\bar{R}_{ps} = x_p \hat{x} + y_p \hat{y} + (z_p - z_s) \hat{z}$$

$$\int_{-L}^L \frac{\cos(z) \hat{z}}{4\pi (x_p^2 + y_p^2 + (z_p - z_s)^2)^{3/2}} dz_s$$



$$\begin{vmatrix} \hat{x} & -\hat{y} & \hat{z} \\ 0 & 0 & \cos(z) \\ x_p & y_p & z_p - z_s \end{vmatrix}$$

$$= y_p \cos(z) \hat{y} - x_p \cos(z) \hat{x}$$



F(z)	A _{analytical}	A _{numerical}	Error = (A _{analyt} - A _{num}) w/ h = 0.1
z	12	12	0
z ²	41.3334	41.33333333	-6.66667E-05
z ³	156.06	156.25	0.19

- expected since no change in slope

F(z)	h size	A _{analytical}	Error =
z ³	1	162	5.75
z ³	0.01	156.0006	-0.2494
z ³	0.0001	156	-0.25

Conclusion:

This was a useful lab because I got some much needed practice using Biot-Savart and learned a slick integration trick for Matlab which is now programmed for use w/ other problems.

I got the expected results both from my integration function table (above) and the plot of the H field strength vs. distance.

```
function [] = plotforbiot

% This function will plot the H vs distance along the y axis
% using the function BiotSavart
y = 0.5:0.1:100;
for n = 1:length(y)
    Hy(n) = biotsavart1 (-pi/2, pi/2, 0.1, 0, y(n), 0);
end

plot(y,Hy);

function [Hx] = biotsavart1(a,b,h, xp, yp, zp)
%
% This program will evaluate Biot-Savart analytically
% using the Trapezoidal method
% This program assumes a current on a thin wire oriented along the Z-axis
% from Lower Limit to Upper Limit

% Create a loop which will find X axis component
%%%%% Not needed for X axis %%%%%%%%%%%
% Because of cross product math, Xbar is negative
% increase = 0;
% for i = a:h:b-h
%     increase = increase - h*xp*(functt (i, xp, yp, zp)+functt(i+h, xp, yp, zp))/2;
% end
% % Print to screen the value
% Hy = increase;

% Create a loop which will find Y axis component
increase = 0;
for i = a:h:b-h
    increase = increase + h*yp*(functt (i, xp, yp, zp)+functt(i+h, xp, yp, zp))/2;
end
Hx = increase;

% Define the function to be integrated

function[dH] = functt(zs, xp, yp, zp)
I = cos(zs);
dH= I/(4*pi*(xp^2 + yp^2+abs((zp-zs)).^2).^3/2);
```

Magnetic strength vs. Distance from wire conductor

